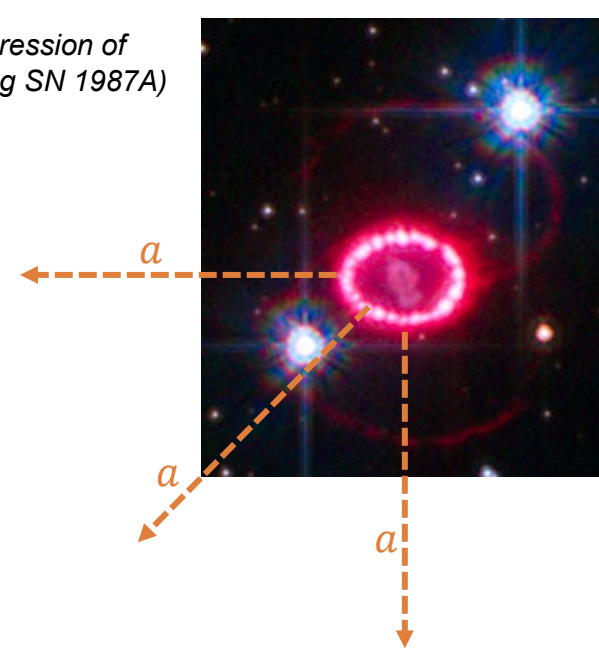


*("artist's" impression of  
axions leaving SN 1987A)*



# Searches for axionlike particles from supernovae beyond tree-level

Eike Ravensburg (prev. Müller),  
Postdoc @ University of Southern Denmark (SDU) Odense

# Axionlike particles

- **ALPs** are **naturally light, weakly interacting** pseudoscalar particles that appear in many BSM theories
- Both axions and ALPs are pseudo-Goldstone bosons of chiral  $U(1)$  theories (hence “axion-like”)
- At low energies  $E \ll \Lambda$ , all these models are described by the same *effective field theory* (EFT):

$$\mathcal{L} \supset -\frac{1}{2}a(\square + m_a^2)a + \frac{1}{4}g_{a\gamma}a F_{\mu\nu}F^{\mu\nu} + \sum_{\ell} \hat{g}_{a\ell}(\partial^\mu a)\bar{\ell}\gamma_5\gamma_\mu\ell + \sum_N g_{aN}\frac{\partial_\mu a}{2m_N}N\gamma^\mu\gamma_5N$$

Mass (free parameter,  
not related to couplings)

Photon coupling

Lepton couplings

Non-relativistic  
nucleon couplings

- Are all these couplings independent? **No**, Quantum effects mix them!  
For collider phenomenology, see, e.g., Bauer et al.: 1708.00443, 2012.12272

- If you are interested in the phenomenology of one of these couplings, others might be unavoidable

# Axionlike particles: (Photophilic) ALPs

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# Supernovae – a great lab for new physics

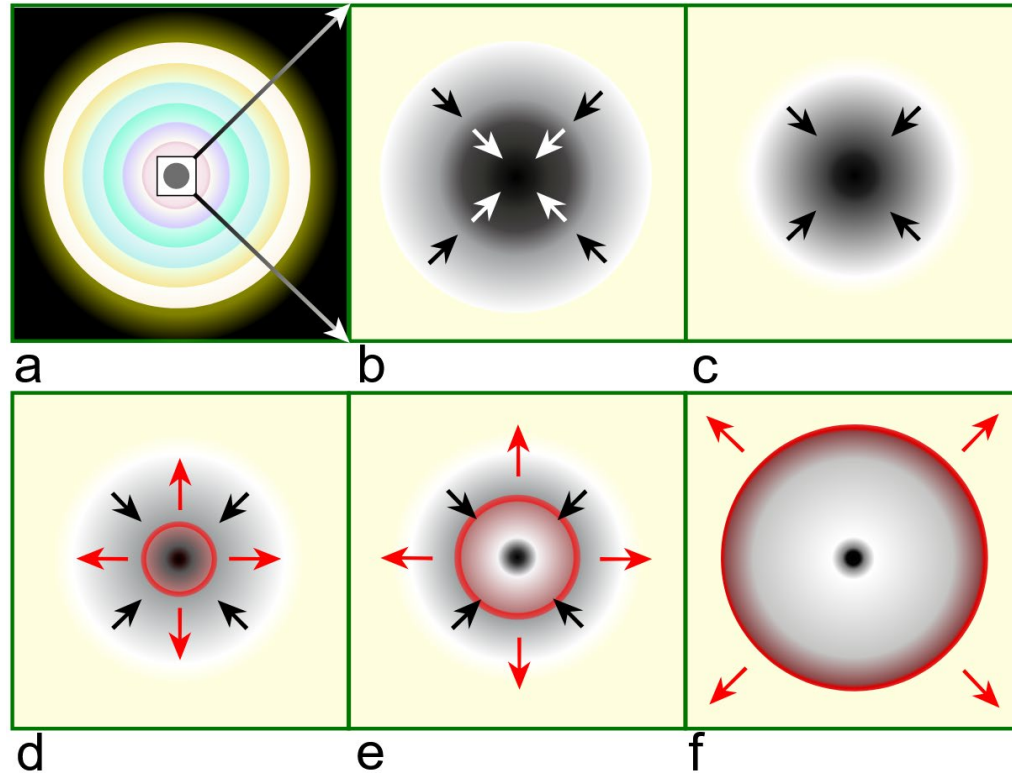
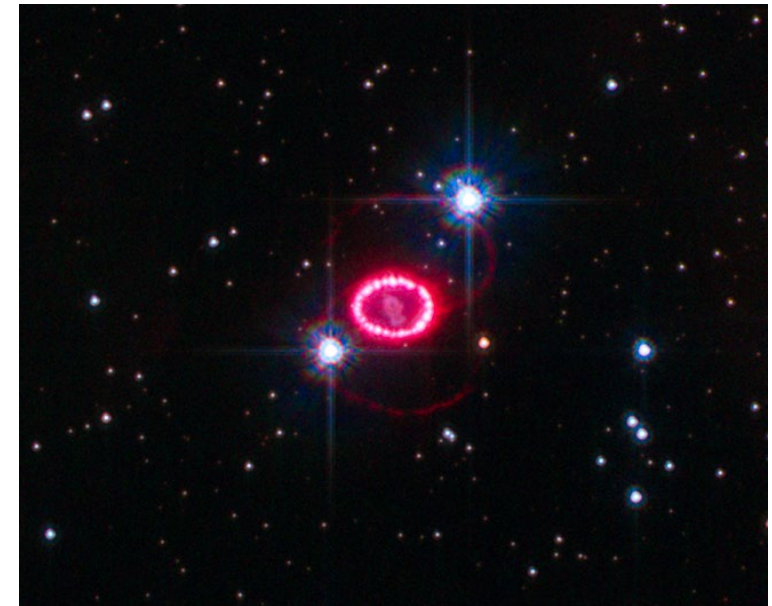
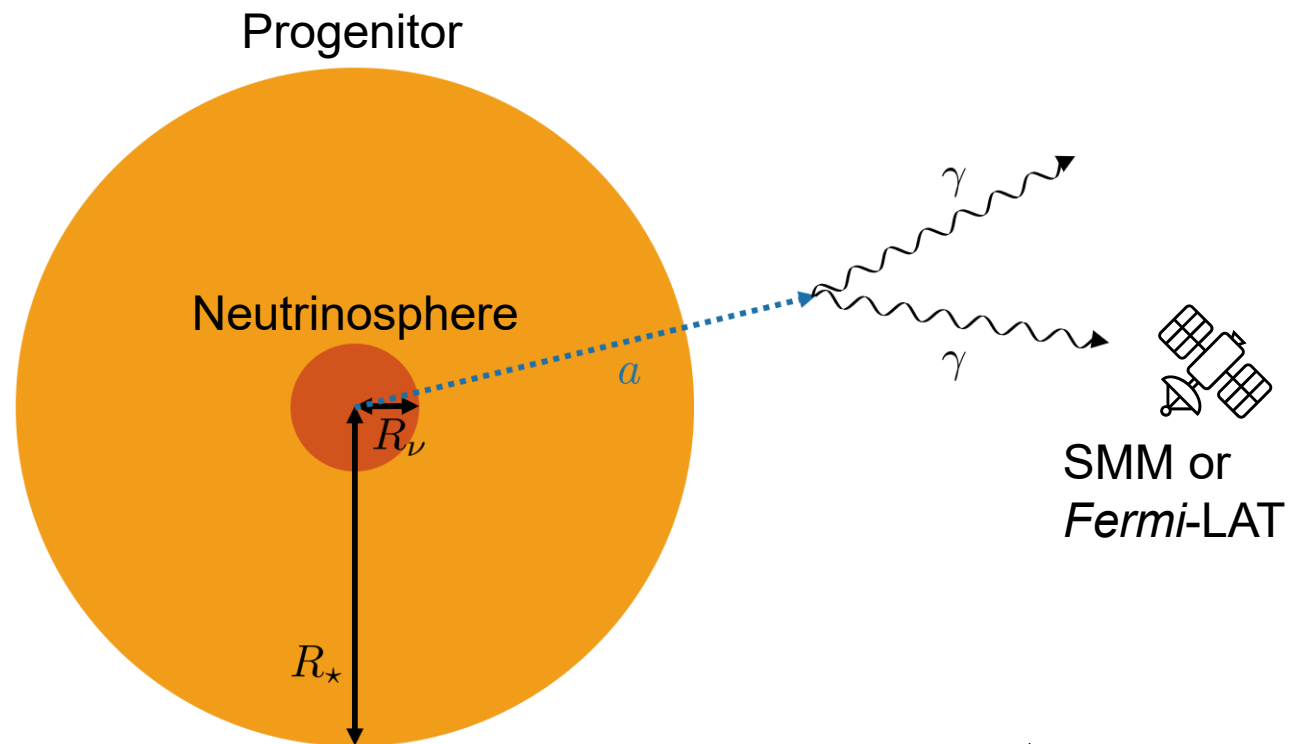


Illustration by R.J. Hall taken from Wikipedia, based on Janka et al.,  
Physics Reports. 442 (1–6): 38–74

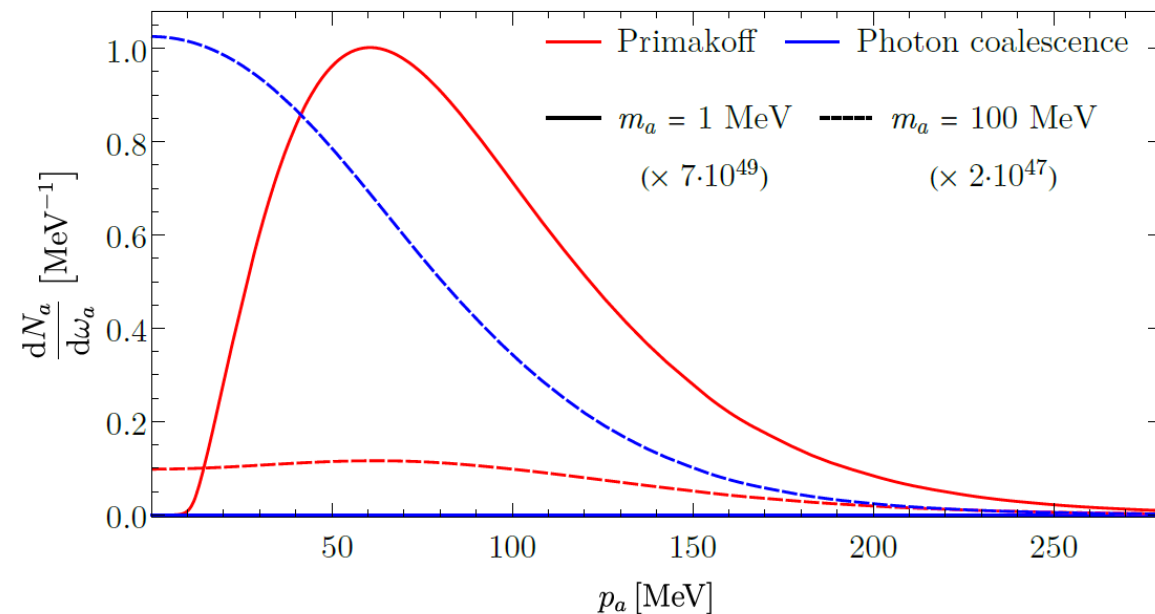


SN 1987A remnant as seen by  
the Hubble telescope

# SN-ALP decay: $\gamma$ -ray signals



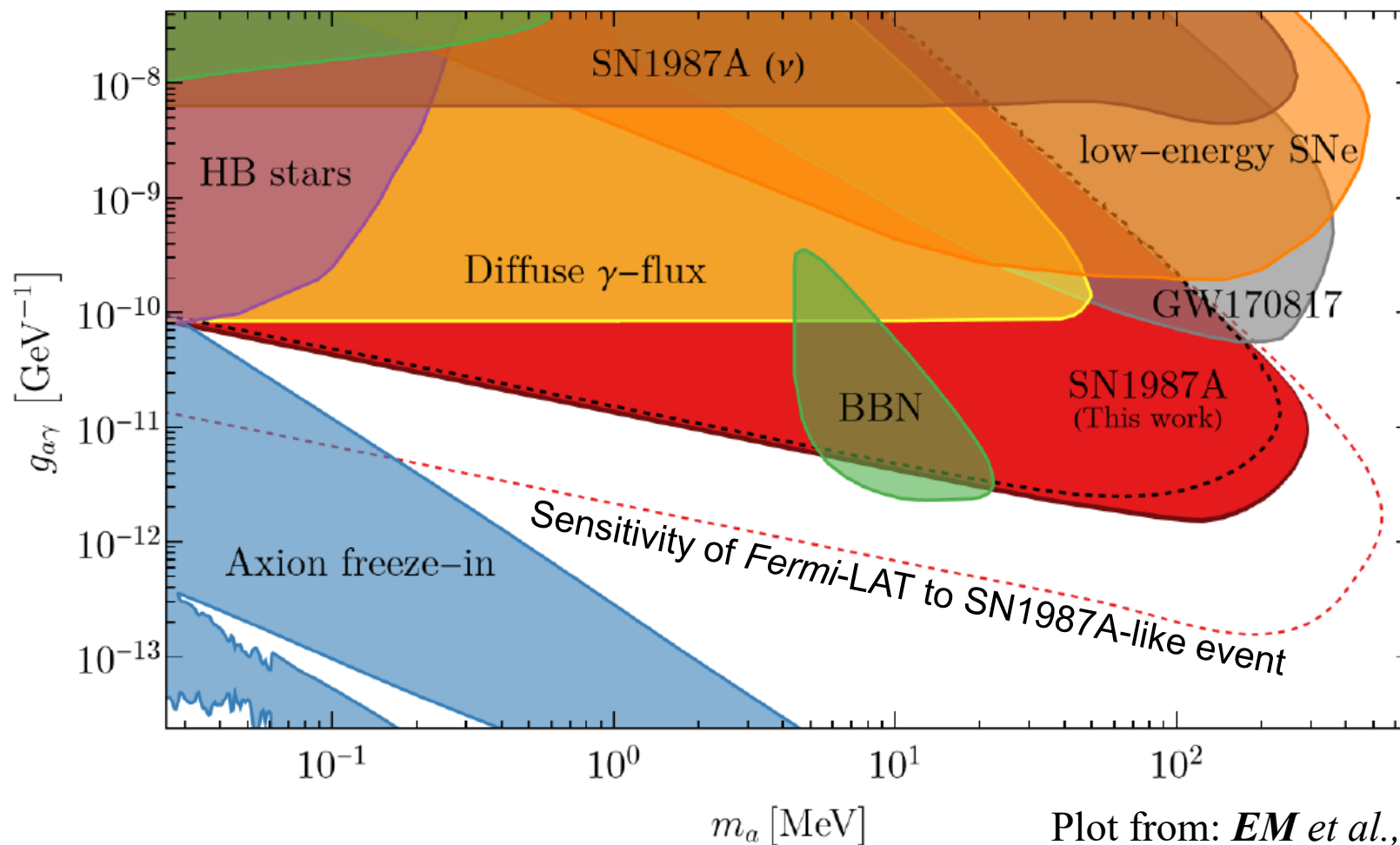
Spectrum of massive ALPs from a SN1987A-like event



$$F_\gamma = \text{BR}_{a \rightarrow \gamma\gamma} \int_{m_a}^{\infty} d\omega_a \int_{-1}^1 dc_\alpha \int_0^{\infty} dL 2 \cdot \frac{dN_a/d\omega_a}{4\pi R_{\text{SN}}^2} \cdot \frac{\omega_a^2 - p_a^2}{2(\omega_a - c_\alpha p_a)^2} \cdot \frac{\exp[-L/\ell_a(\omega_a)]}{\ell_a(\omega_a)} \cdot \Theta_{\text{cons.}}(\omega_a, c_\alpha, L)$$

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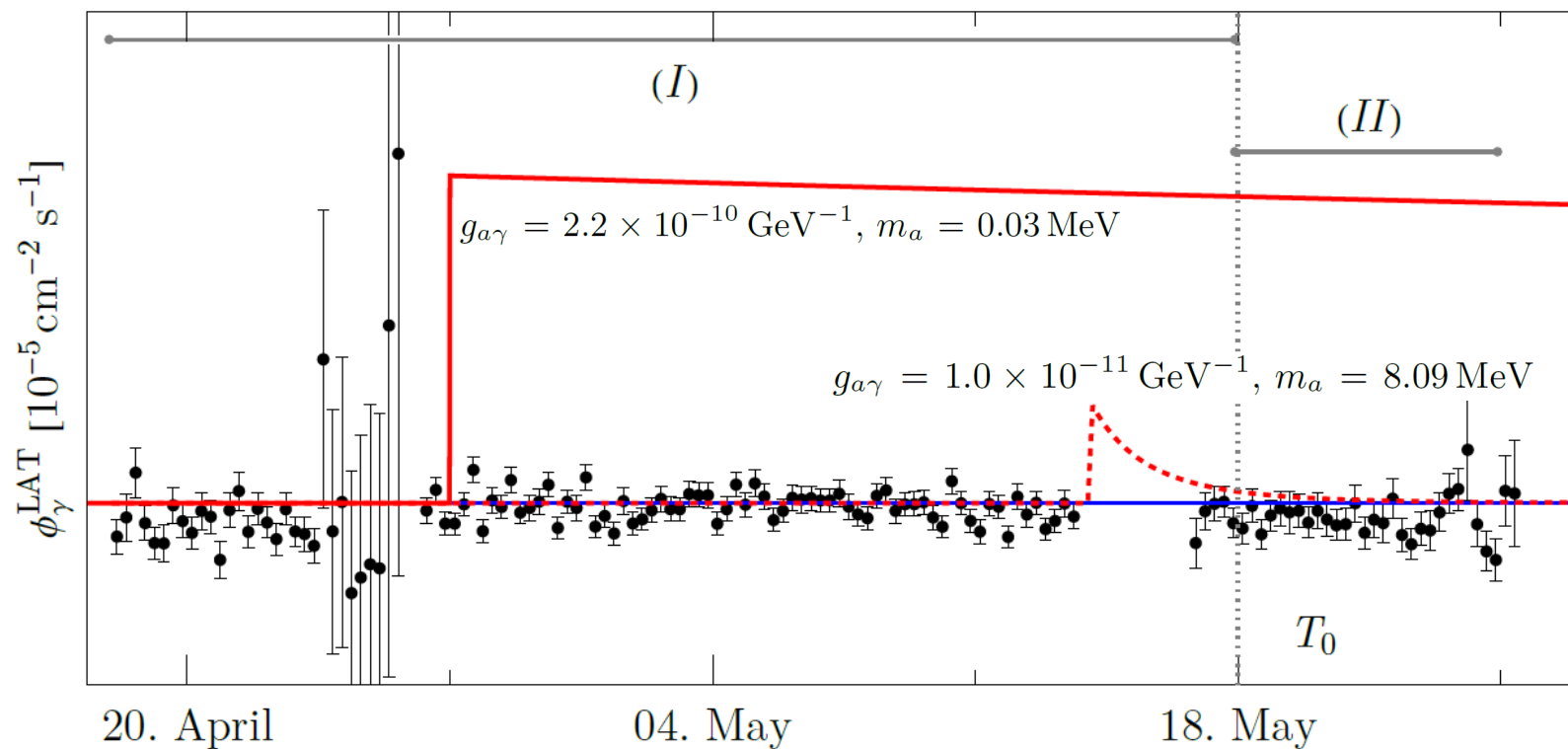
No  $\gamma$ -rays above background were observed by the Solar Maximum Mission after SN 1987A:



Plot from: *EM et al., JCAP 07 (2023) 056*

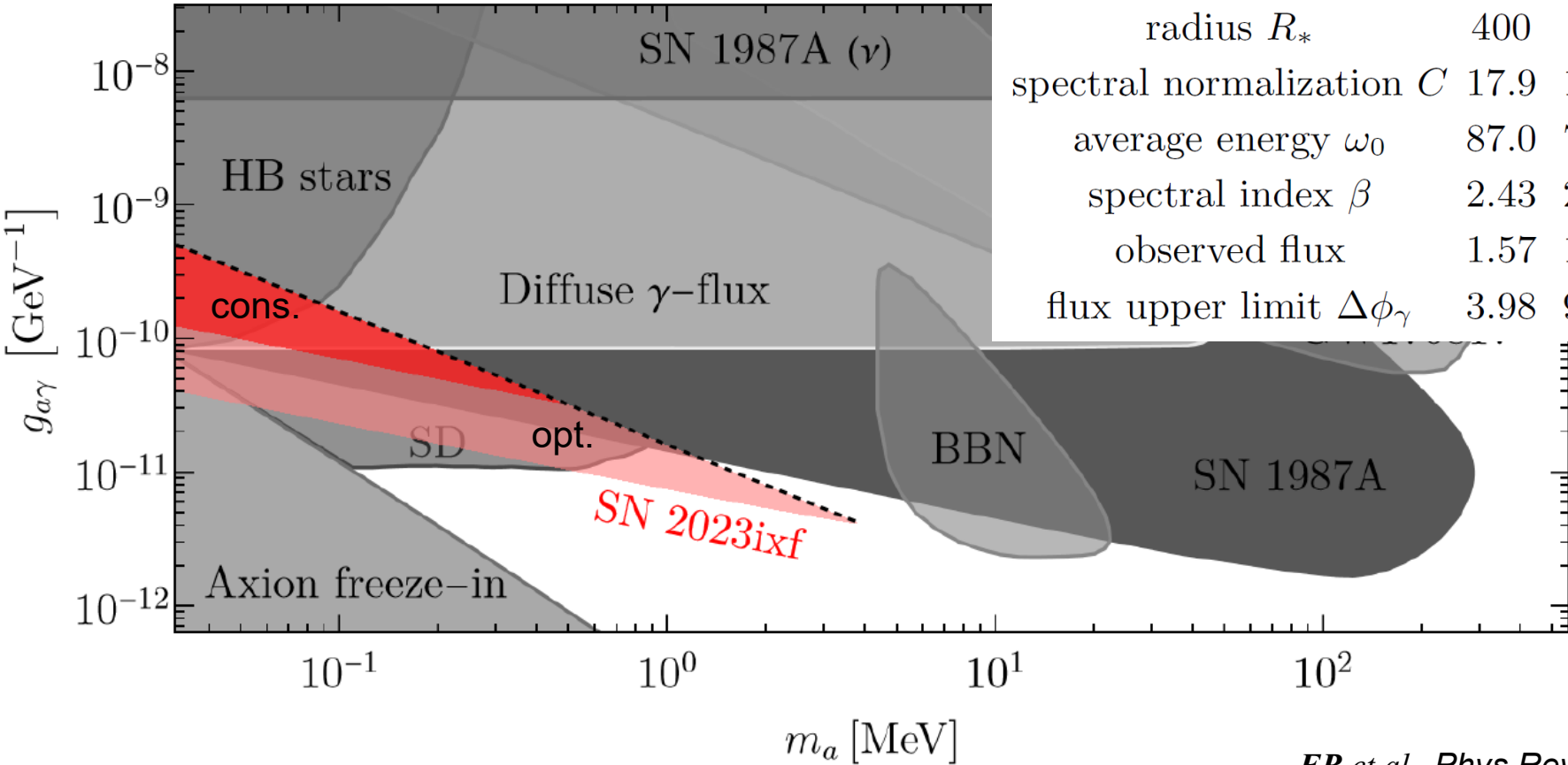
# SN-ALP decay: $\gamma$ -ray signals from beyond the Galaxy

On May 18<sup>th</sup> 2023, SN 2023ixf was observed at an estimated distance of  $\sim 7$  Mpc (more than 100x further away than SN 1987A). This is what *Fermi*-LAT could have seen:



# SN-ALP decay: $\gamma$ -ray signals from beyond the Galaxy

...but nothing was observed:



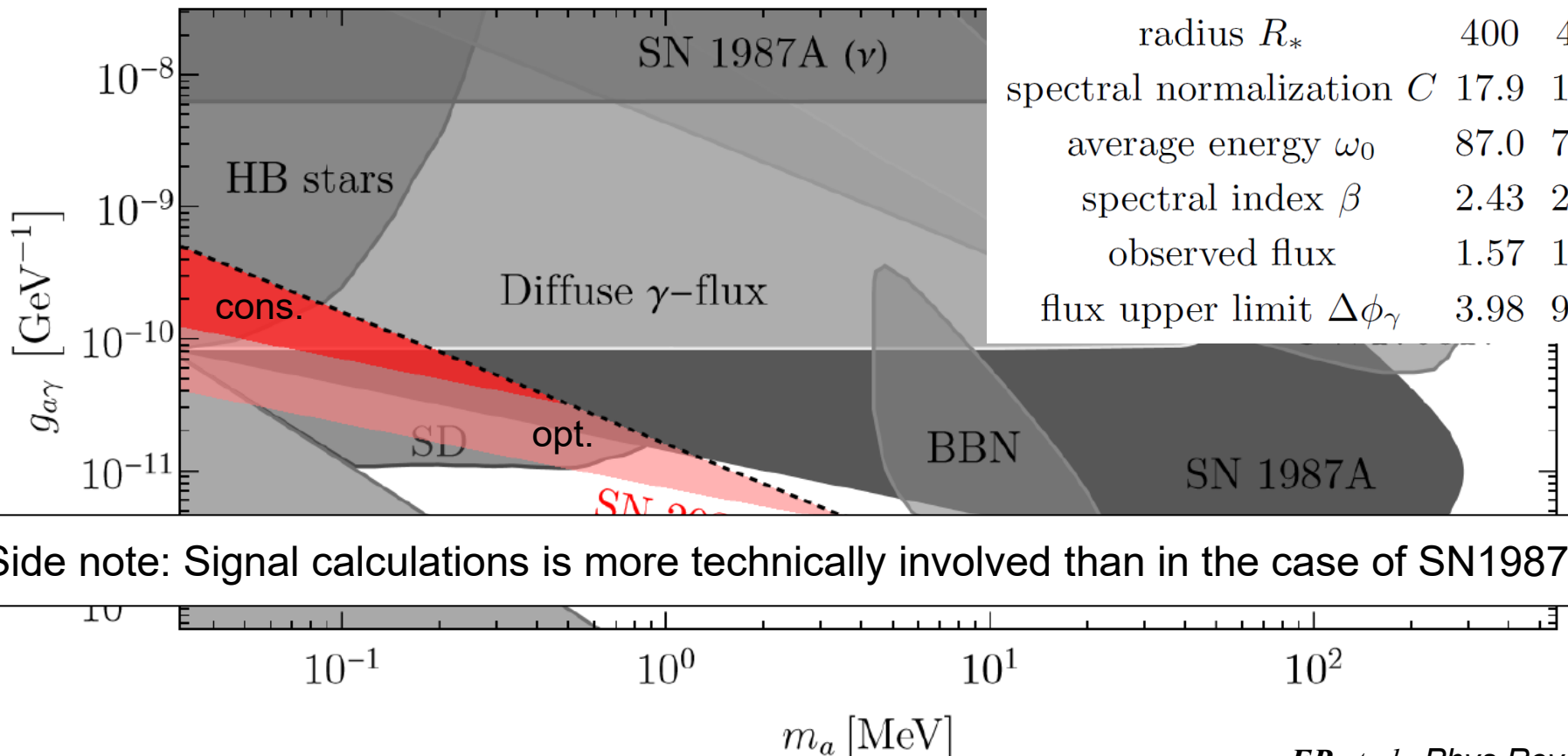
Parameter	opt.	cons.	Unit
distance $R_{\text{SN}}$	6.70	7.00	Mpc
mass $M$	13	9	$M_{\odot}$
radius $R_*$	400	420	$R_{\odot}$
spectral normalization $C$	17.9	1.36	$10^{48} \text{ MeV}^{-1}$
average energy $\omega_0$	87.0	71.2	MeV
spectral index $\beta$	2.43	2.86	1
observed flux	1.57	1.47	$10^{-5} \text{ cm}^{-2} \text{ s}^{-1}$
flux upper limit $\Delta\phi_{\gamma}$	3.98	9.10	$10^{-8} \text{ cm}^{-2} \text{ s}^{-1}$



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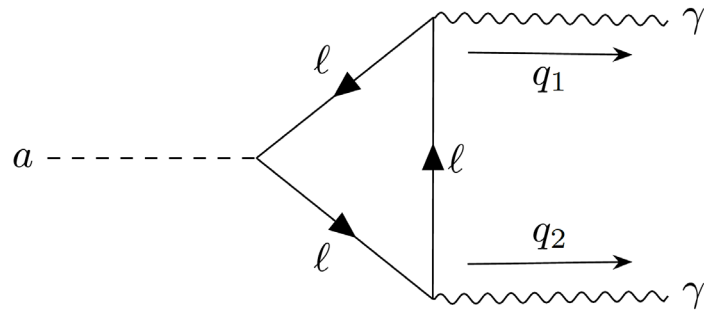
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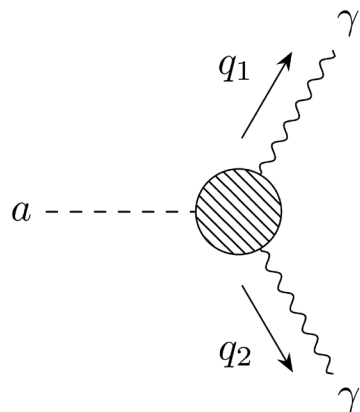
$$\mathcal{L}_{1\text{-loop}} \supset -\frac{1}{2} a(\square + m_a^2)a + \sum_{\ell} \hat{g}_{a\ell} (\partial^\mu a) \bar{\ell} \gamma_5 \gamma_\mu \ell$$

# Effective photon coupling

Couplings between ALPs and gauge bosons are not induced by RGE running!  
Still, the full lepton loop can nevertheless yield an effective photon vertex:



$$= i \frac{e^2 \hat{g}_{a\ell}}{2\pi^2} \underbrace{\left[ 1 + 2m_\ell^2 C_0(q_1^2, q_2^2, (q_1 + q_2)^2, m_\ell^2, m_\ell^2, m_\ell^2) \right]}_{= i g_{a\gamma}^{\text{eff}}(q_1, q_2)} q_1^\alpha q_2^\beta \varepsilon^{\mu\nu\alpha\beta}$$

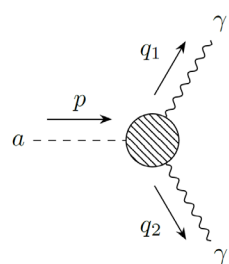


$$= i \boxed{g_{a\gamma}^{\text{eff}}(q_1, q_2)} q_1^\alpha q_2^\beta \varepsilon^{\mu\nu\alpha\beta}$$

R. Ferreira, D. Marsh, *EM*, JCAP 11 (2022) 057

# The effective ALP-photon coupling

Known for a while: the effective coupling *on-shell*, i.e., in a decay process



$$g_{a\gamma}^{(D)} \equiv g_{a\gamma}^{\text{eff}}(q_1^2 = q_2^2 = 0, p^2 = m_a^2) = \frac{2\alpha}{\pi} \hat{g}_{ae} \left[ 1 - \frac{4m_e^2}{m_a^2} f^2 \left( \frac{4m_e^2}{m_a^2} \right) \right]$$

$$= -\frac{\alpha \hat{g}_{ae}}{6\pi} \left( \frac{m_a}{m_e} \right)^2 + \mathcal{O} \left( \frac{m_a}{m_e} \right)^4$$

$$f(\tau) = \begin{cases} \arcsin \left( \frac{1}{\sqrt{\tau}} \right) & \text{for } \tau \geq 1 \\ \frac{1}{2} \left[ \pi + i \log \left( \frac{1 + \sqrt{1 - \tau}}{1 - \sqrt{1 - \tau}} \right) \right] & \text{for } \tau < 1 \end{cases}$$

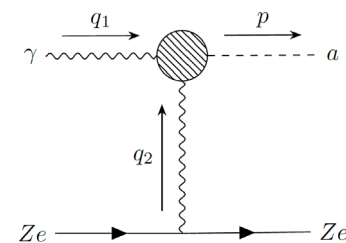
Bauer, Neubert, Thamm,  
JHEP 12 (2017) 044

This effective coupling vanishes for massless ALPs, but it is only the right coupling for on-shell photons!

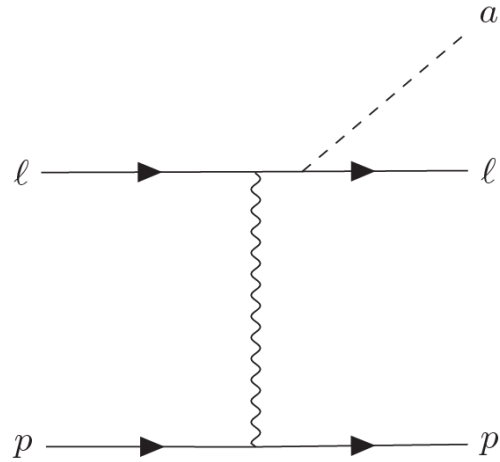
If a photon in the t-channel is off-shell, we get the effective Primakoff coupling:

$$g_{a\gamma}^{(P)} \equiv g_{a\gamma}^{\text{eff}}(q_1^2 = 0, q_2^2 = t, p^2 = m_a^2) = \frac{2\alpha}{\pi} \hat{g}_{ae} \left\{ 1 + \frac{4m_e^2}{m_a^2 - t} \left[ f^2 \left( \frac{4m_e^2}{t} \right) - f^2 \left( \frac{4m_e^2}{m_a^2} \right) \right] \right\}$$

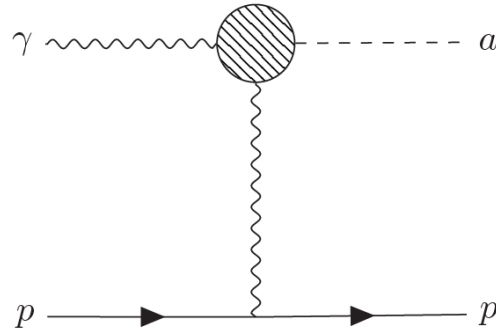
$$= \frac{2\alpha}{\pi} \hat{g}_{ae} \left[ 1 + \frac{4m_e^2}{m_a^2 - t} f^2 \left( \frac{4m_e^2}{t} \right) \right] + \mathcal{O} \left( \frac{m_a}{m_e} \right)^2$$



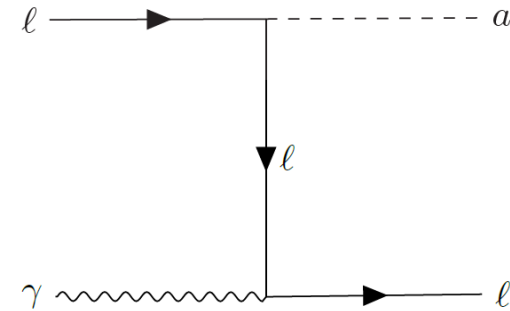
# Leptonic ALPs produced in SNe



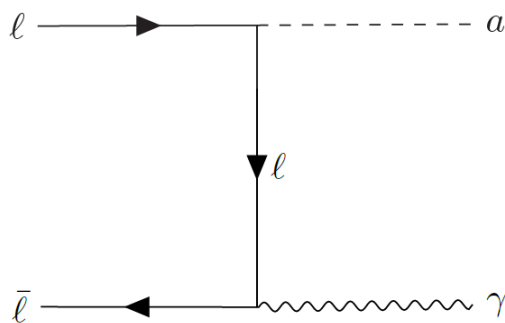
(a) Bremsstrahlung



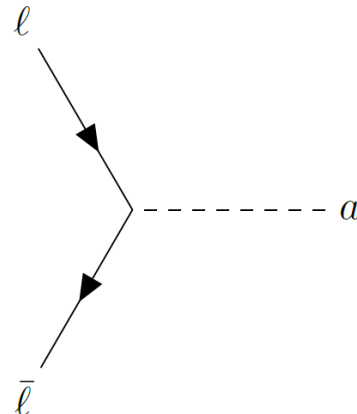
(b) Primakoff process



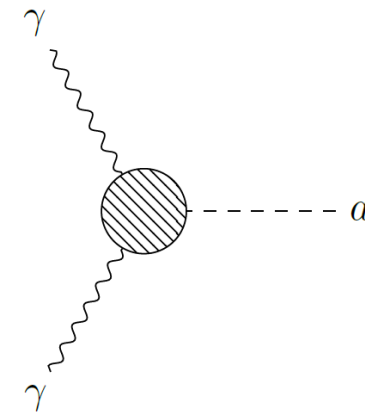
(c) Compton



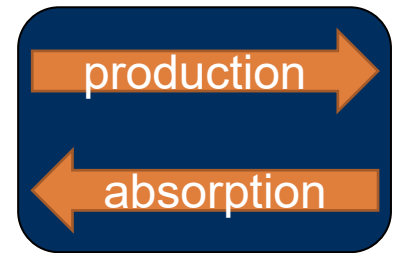
(d) Pair annihilation



(e) Lepton fusion



(f)  $\gamma\gamma$ -coalescence



# ALPs from a SN plasma

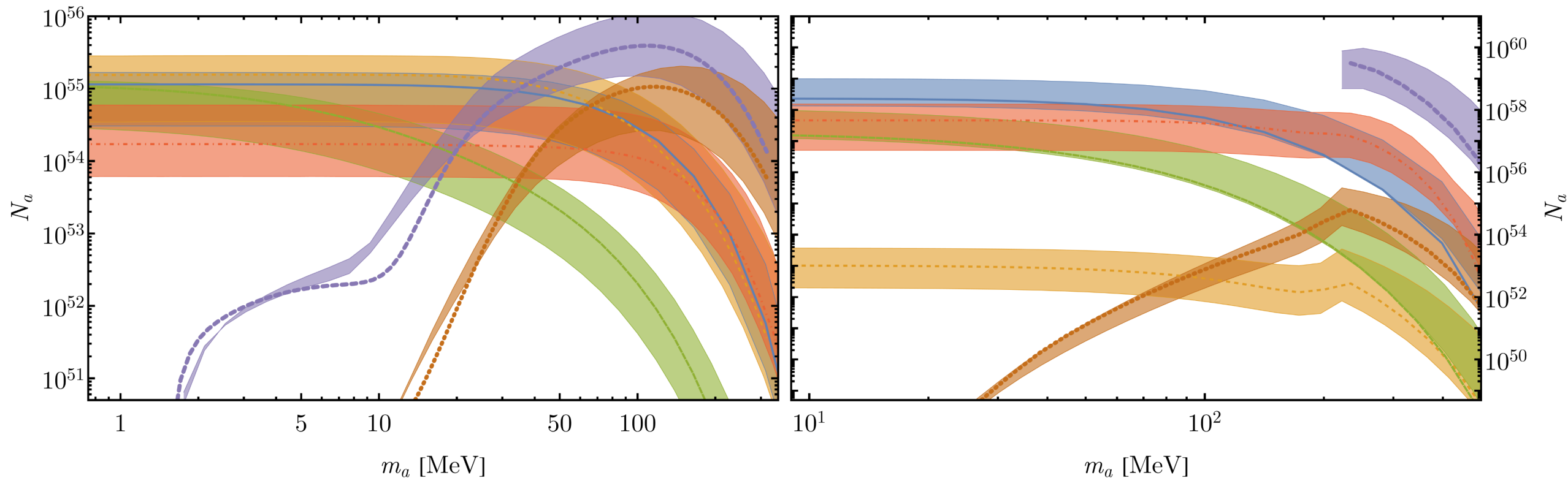
The spectral rate of change in the number density of ALPs (“production spectrum”) can be calculated as the integrated collision term of the Boltzmann equation:

$$\frac{d^2 n_a}{dt d\omega_a} = \left[ \prod_i \int \frac{d^3 \mathbf{p}_i}{(2\pi)^3 2E_i} f_i(E_i) \right] \left[ \prod_{j \neq a} \int \frac{d^3 \mathbf{p}'_j}{(2\pi)^3 2E'_j} [1 \pm f_j(E'_j)] \right] \\ \times (2\pi)^4 \delta^{(4)} \left( \sum_i p_i - \sum_j p'_j \right) S \frac{|\mathbf{p}'_a|}{4\pi^2} |\mathcal{M}|^2,$$

for every relevant production process  $\{i\} \rightarrow \{j\} + a$ .

# Leptonic ALPs produced in SNe

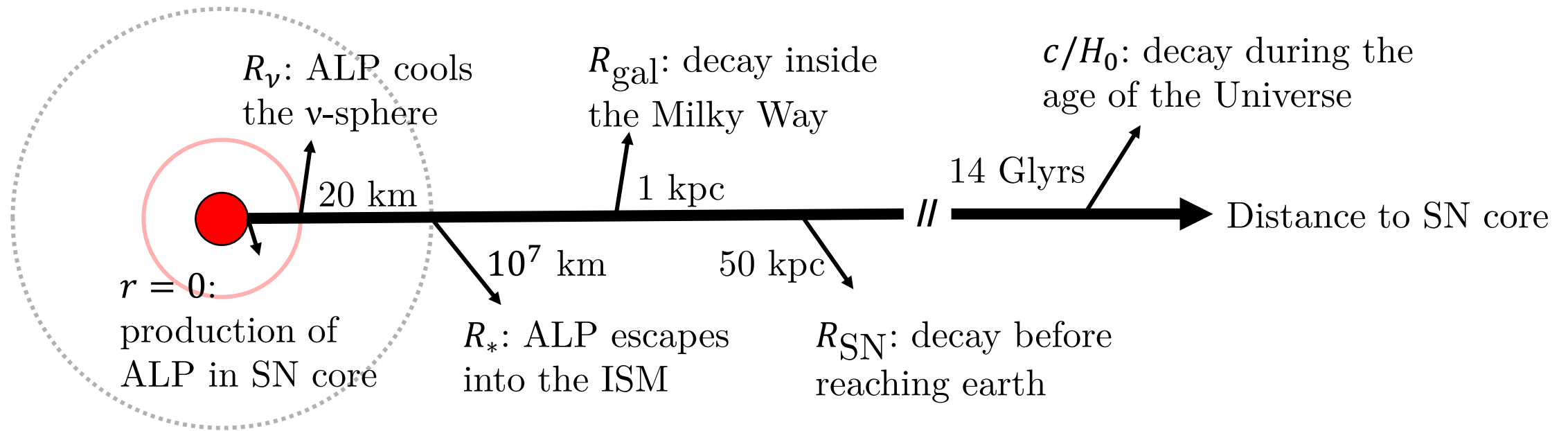
Shading corresponds to three different SN simulations: Agile-Boltztran (solid line, Fischer et al., PRD 104 (2021) 103012) and Garching SN Archive (upper/lower shading for hottest/coldest model of R. Bollig et al., Phys. Rev. Lett. 125 (2020) 051104)



$$\hat{g}_{ae} = 10^{-10} \text{MeV}^{-1}$$

$$\hat{g}_{a\mu} = 10^{-10} \text{MeV}^{-1}$$

# ALPs from SNe: Observables (incomplete list)



Anomalous cooling

$$L_a < L_\nu$$

Explosion energy of the mantle

$$E_{\text{mantle}}^a < E_{\text{mantle}}^{\text{obs}}$$

Galactic positrons

$$\text{BR}_{a \rightarrow e^+e^-} N_a < \langle \delta N_{\text{pos}}^{\text{bkg.}} \rangle$$

Gamma-ray burst from nearby SNe

$$F_\gamma < \langle \delta F_\gamma^{\text{bkg.}} \rangle$$

Diffuse gamma rays from all past SNe

$$n_\gamma^a < n_\gamma^{\text{obs}}$$



# ALPs from SNe: Observables

**Cooling bound**, from the duration of the neutrino burst of SN 1987A

*See also Lucente & Carena,  
Phys.Rev.D 104 (2021) 10, 103007*

$$L_a = \int_0^{R_\nu} dr 4\pi r^2 \lambda^2(r) \int_{m_a/\lambda}^\infty d\omega_a \omega_a \frac{d^2 n_a}{dt d\omega_a}(r, \omega_a) \cdot \mathcal{T}(r, R_{\text{far}}, \omega_a)$$

**Decay bound**, from the non-observation of gamma-rays following core-collapse SNe

*See also Jaeckel et al., Phys.Rev.D 98  
(2018) 5, 055032; Hoof & Schulz,  
JCAP 03 (2023) 054; EM et al.,  
JCAP 07 (2023) 056*

$$F_\gamma = \text{BR}_{a \rightarrow \gamma\gamma} \int_{m_a}^\infty d\omega_a \int_{-1}^1 dc_\alpha \int_0^\infty dL 2 \cdot \frac{dN_a/d\omega_a}{4\pi R_{\text{SN}}^2} \cdot \frac{\omega_a^2 - p_a^2}{2(\omega_a - c_\alpha p_a)^2} \cdot \frac{\exp[-L/\ell_a(\omega_a)]}{\ell_a(\omega_a)} \cdot \Theta_{\text{cons.}}(\omega_a, c_\alpha, L)$$

**Explosion energy bound**, from the observed kinetic energy of the SN explosion

*See also Caputo et al., Phys.Rev.Lett.  
128 (2022) 22, 221103*

$$E_{\text{mantle}} = \int dt \int_0^{R_\nu} dr \int_{m_a/\lambda}^\infty d\omega_a 4\pi r^2 \lambda \omega_a \frac{dn_a}{dt d\omega_a}(r, t, \omega_a) T(r, t, \omega_a) \left[ 1 - \exp\left(-\frac{R_* - r}{\ell_a(\lambda \omega_a)}\right) \right]$$

# ALPs from SNe: Observables

**511 keV-line bound**, from Galactic positrons annihilating into X-rays

$$N_{\text{pos}} = \int d\omega_a \text{BR}_{a \rightarrow e^+e^-} \frac{dN_a}{d\omega_a} [\exp(-R_*/\ell_a) - \exp(-R_{\text{Gal}}/\ell_a)]$$

*See also Calore et al., Phys. Rev. D 104 (2021) 043016; De La Torre Luque et al. Phys.Rev.D 109 (2024) 10, 103028*

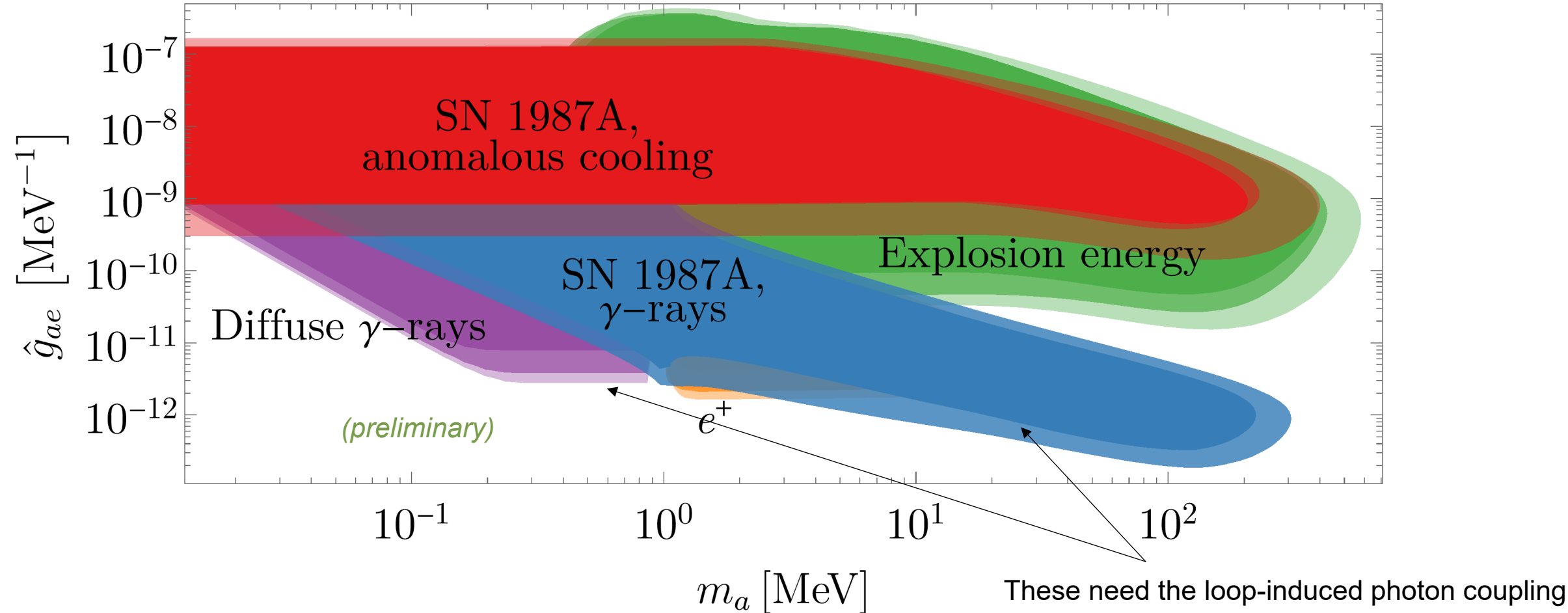
**Diffuse gamma-ray bound**, from all past SNe

$$\frac{d\phi_\gamma}{d\omega_\gamma} \simeq \frac{1}{2\pi} \int_0^\infty dz (1+z) n'_{\text{cc}}(z) \int_{\omega_\gamma^z}^\infty d\omega_a \frac{f_{\text{D}}(\omega_a)}{\omega_a} \frac{dN_a}{d\omega_a}$$

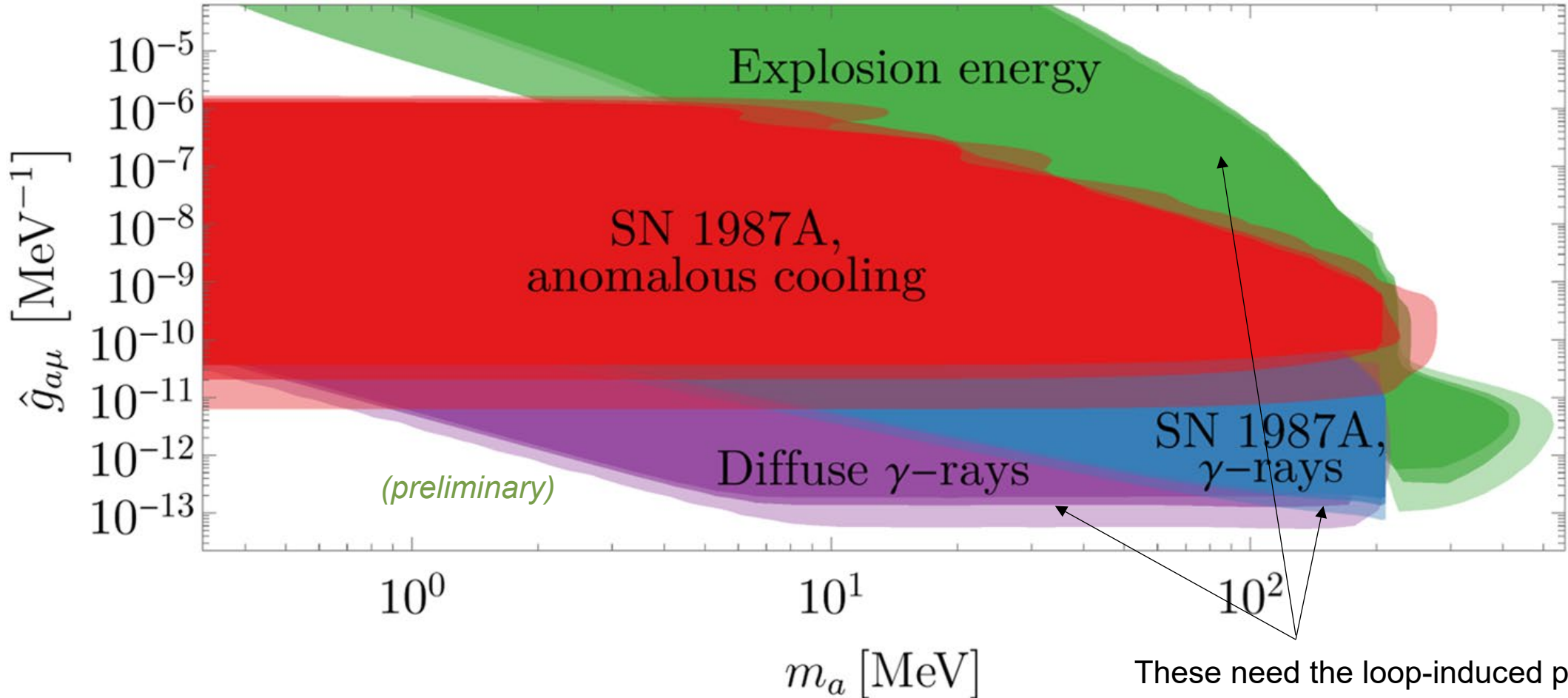
*See also Calore et al., Phys.Rev.D 102 (2020) 12, 123005; Caputo et al., Phys.Rev.D 105 (2022) 3, 035022*

(In fact, the diffuse flux is calculated in a much more cumbersome way, soon to be published, but for light-enough ALPs the above approximation holds.)

# Leptonic ALPs from SNe: Results (electrons)



# Leptonic ALPs from SNe: Results (muons)



These need the loop-induced photon coupling

# Axionlike particles: “QCD ALPs”

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# “QCD ALPs” have photon couplings!

→ ALPs that interact with gluons and/or quarks (but are not the QCD axion!)

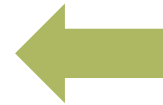
→ Interesting for phenomenology: low-energy couplings to nucleons and pions are very efficient in SNe

$$\mathcal{L}_{\text{nuc}} = \frac{\partial^\mu a}{2f_a} \left[ C_p \bar{p} \gamma^\mu \gamma_5 p + C_n \bar{n} \gamma^\mu \gamma_5 n \right. \\ \left. + \frac{C_{a\pi N}}{f_\pi} (i\pi^+ \bar{p} \gamma^\mu n - i\pi^- \bar{n} \gamma^\mu p) \right. \\ \left. + C_{aN\Delta} \left( \bar{p} \Delta_\mu^+ + \overline{\Delta_\mu^+} p + \bar{n} \Delta_\mu^0 + \overline{\Delta_\mu^0} n \right) \right]$$

$$C_p(c_g, c_u, c_d) = -0.47 c_g + 0.88 c_u - 0.39 c_d - 0.038 c_s \\ - 0.012 c_c - 0.009 c_b - 0.0035 c_t,$$

$$C_n(c_g, c_u, c_d) = -0.02 c_g + 0.88 c_d - 0.39 c_u - 0.038 c_s \\ - 0.012 c_c - 0.009 c_b - 0.0035 c_t.$$

Grilli di Cortona, et al., JHEP 01 (2016) 034



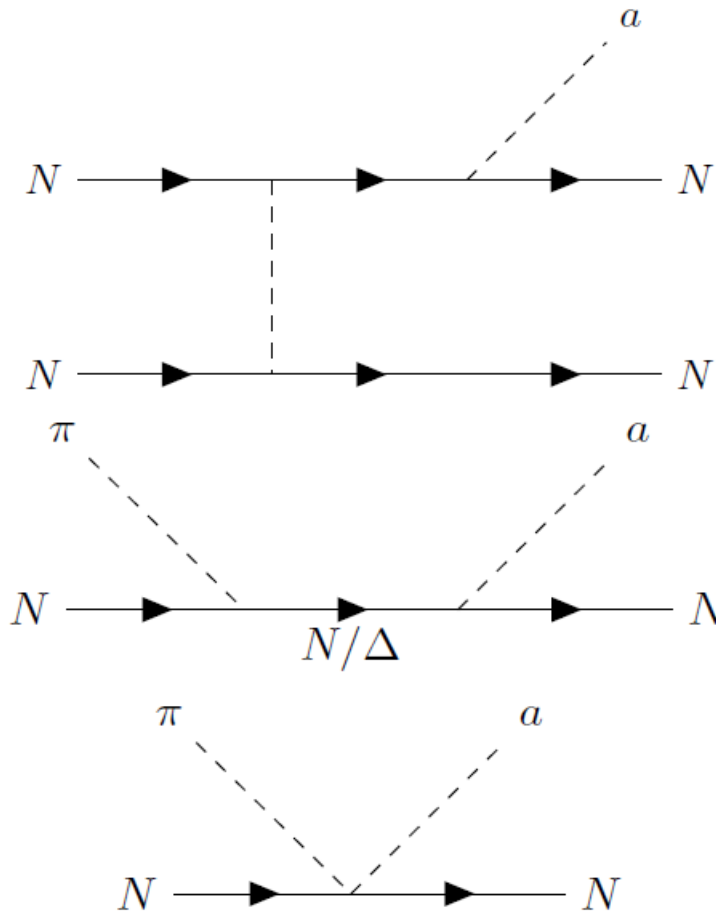
Couplings to quarks and gluons:  $c_u, c_d, c_g$



$$g_{a\gamma} = \frac{\alpha}{2\pi f_a} \left\{ -1.92 c_g - \frac{m_a^2}{m_\pi^2 - m_a^2} \left[ c_g \frac{m_d - m_u}{m_d + m_u} + (c_u - c_d) \right] \right\}$$

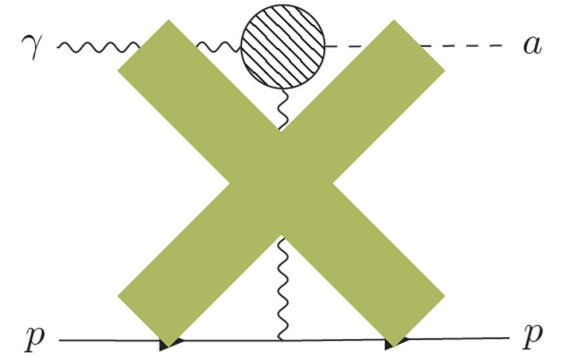
In general, there is an “irreducible” photon coupling as well!

# “QCD ALPs” produced in SNe

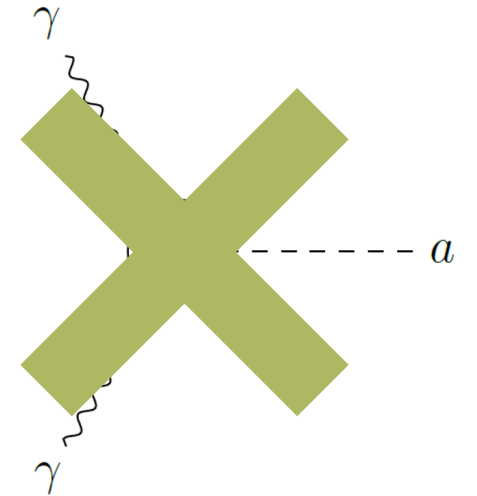


Nucleon-nucleon Bremsstrahlung

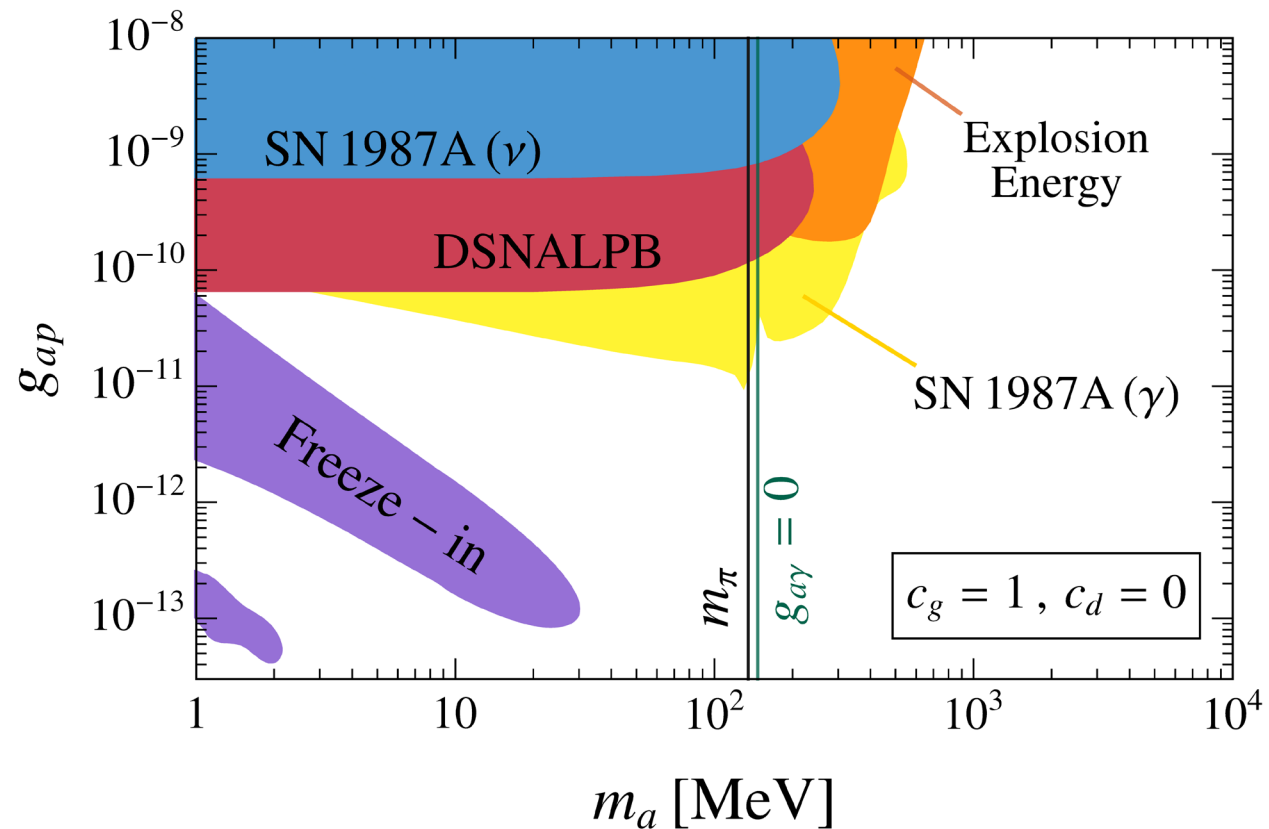
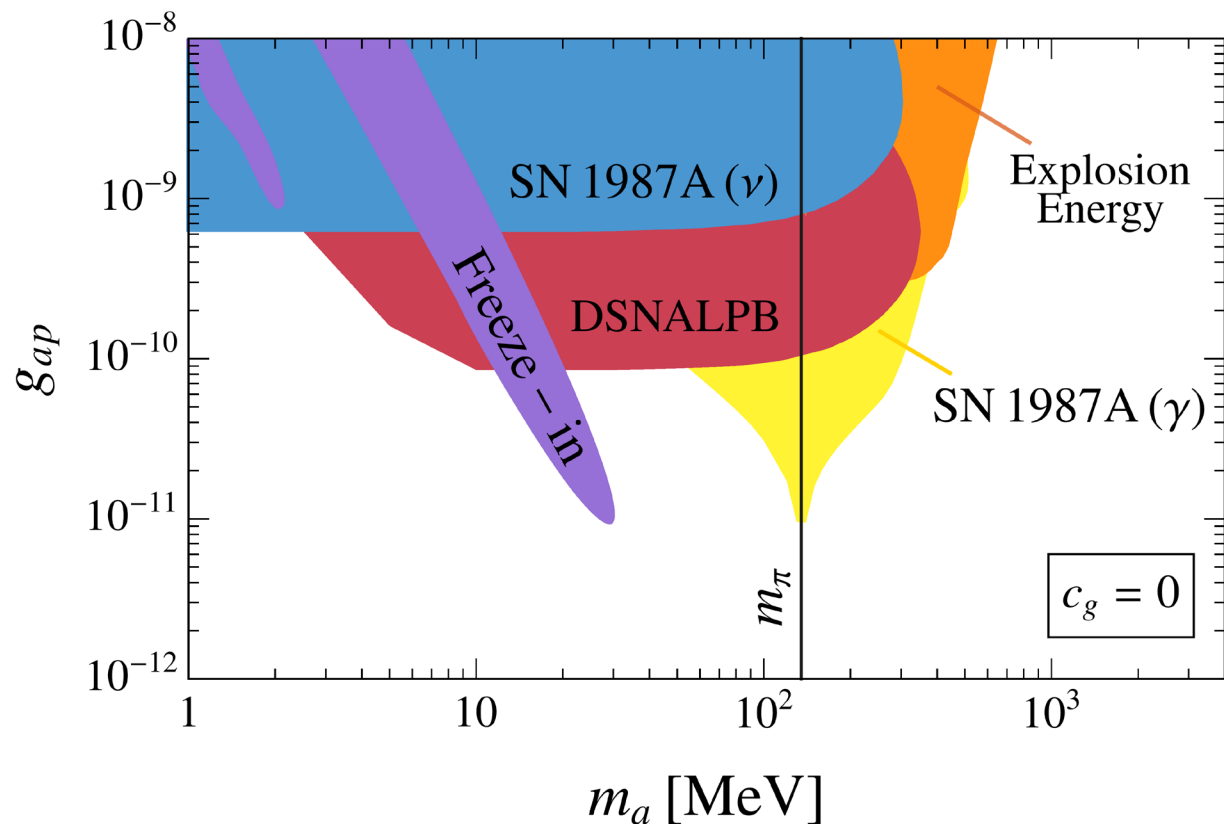
Pion-axion conversion



Production via “irreducible” photon interaction is negligible here



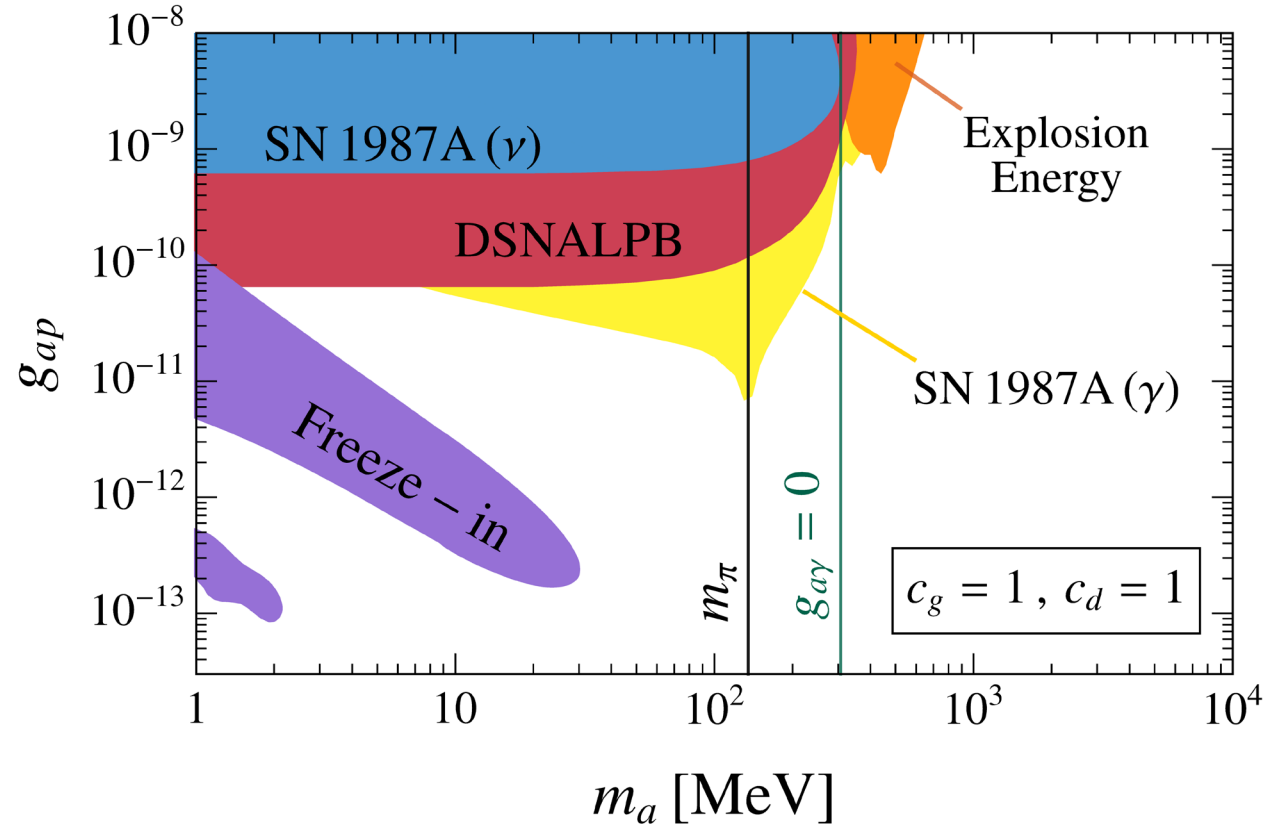
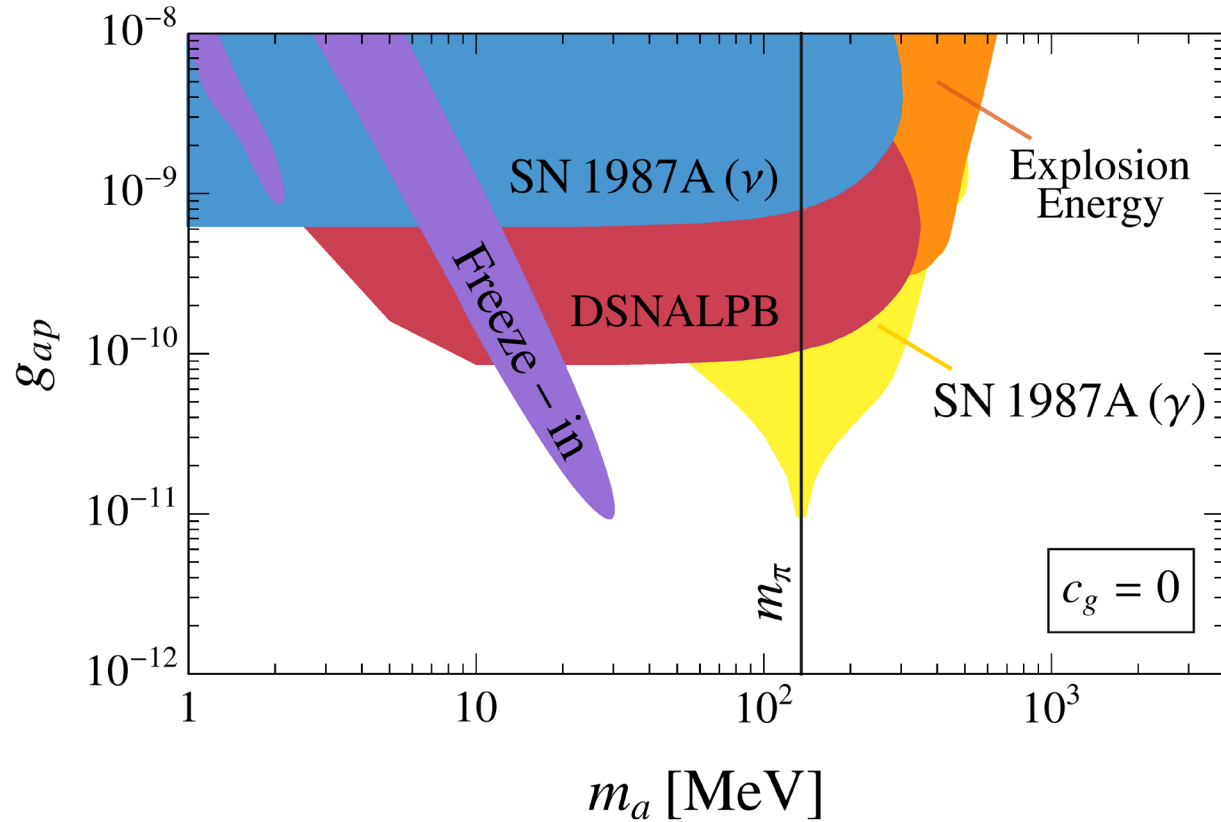
# “QCD ALPs” from SNe: Results



Lella, **ER**, et al., *Phys.Rev.D* 110 (2024) 4, 043019



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Lella, *ER*, et al., *Phys.Rev.D* 110 (2024) 4, 043019

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- ALPs are naturally light, weakly interacting pseudoscalar particles that appear in many BSM theories
- Both axions and ALPs are pseudo-Goldstone bosons of chiral  $U(1)$  theories (hence “axion-like”)
- At low energies  $E \ll \Lambda$ , all these models are described by the same effective field theory (EFT):

$$\mathcal{L} \supset -\frac{1}{2}a(\square + m_a^2)a + \frac{1}{4}g_{a\gamma}a F_{\mu\nu}F^{\mu\nu} + \sum_{\ell} \hat{g}_{a\ell}(\partial^\mu a)\bar{\ell}\gamma_5\gamma_\mu\ell + \sum_N g_{aN}\frac{\partial_\mu a}{2m_N}N\gamma^\mu\gamma_5N$$

Mass (free parameter,  
not related to couplings)

Photon coupling

Lepton couplings

Non-relativistic  
nucleon couplings

- Are all these couplings independent? No, Quantum effects mix them!  
For collider phenomenology, see, e.g., Bauer et al.: 1708.00443, 2012.12272

- If you are interested in the phenomenology of one of these couplings, others might be unavoidable

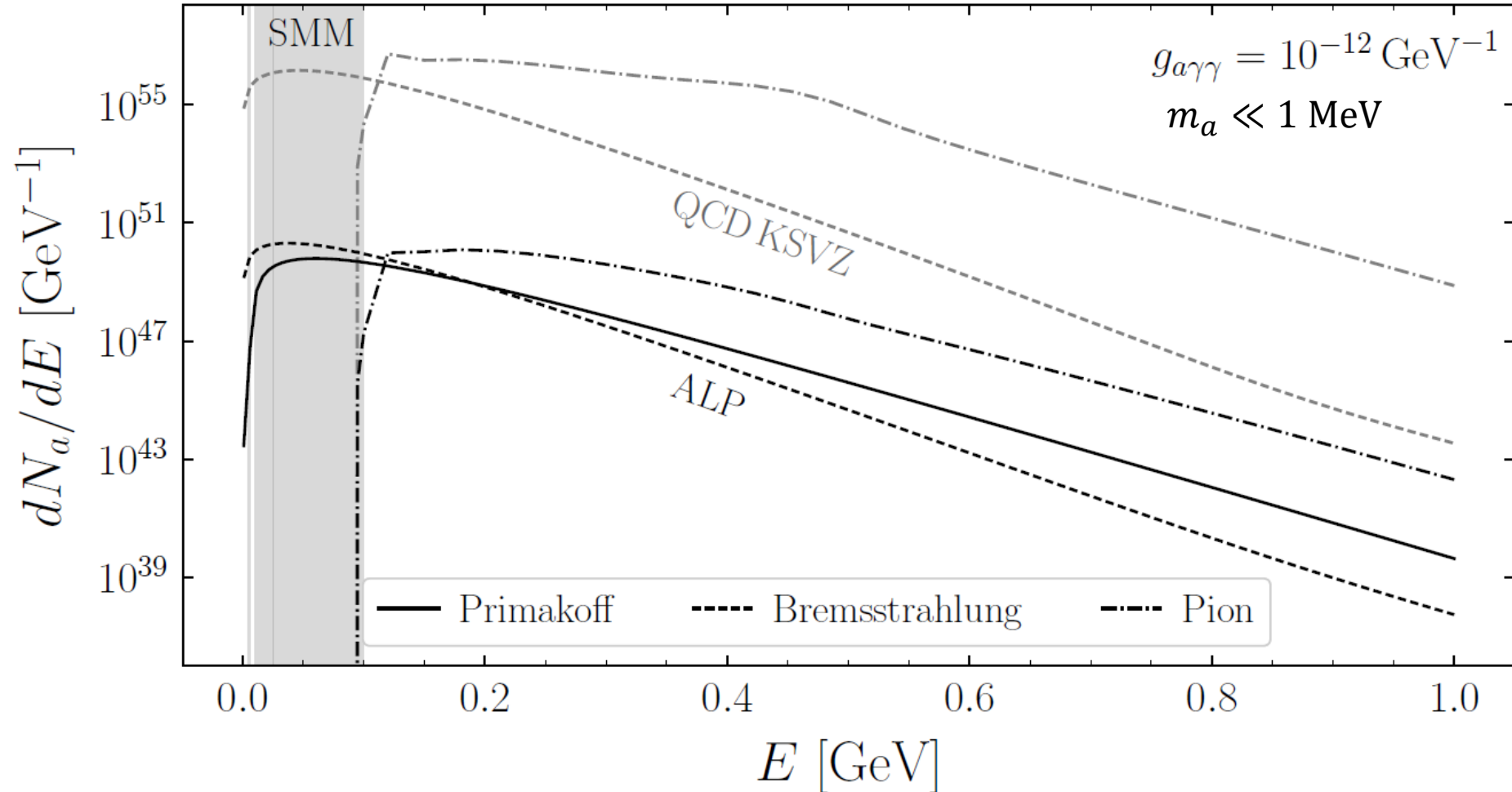
# Standard ALP production

RG-induced running couplings to nucleons and pions:

$$C_p \simeq C_n \simeq 10^{-4} \frac{2\pi f_a}{\alpha} g_{a\gamma}$$

Even though these are small, the resulting QCD processes seemingly dominate ALP production!

→ This should be included in all ALP-studies  
(after a careful check)



# Axionlike particles: One-loop effects for astro-phenomenology

Studying the phenomenology of	...you cannot ignore	Disclaimer
ALP-lepton couplings $g_{ae}, g_{a\mu}, g_{a\tau}$	ALP-photon coupling $g_{a\gamma}$ (structure factor (not RG running))	For high-energetic ALPs with $E \gtrsim m_\ell$ ; Probably also $g_{aN}, g_{a\pi}, \dots$
ALP-photon coupling $g_{a\gamma}$	ALP-QCD couplings $g_{aN}, g_{a\pi}, \dots$ (via RG running)	For ALP-production in SNe at least (with a high density of nuclear matter)
ALP-QCD couplings $g_{aN}, g_{a\pi}, \dots$	ALP-photon coupling $g_{a\gamma}$ (construction of IR EFT)	Yields observable signals

# Conclusion & Outlook

- There are many observables to look for, and predicting them is numerically quite costly
- Even in phenomenological EFT models, higher-order QFT effects play an important role
  - **Effective ALP couplings are not independent!** And corrections are important in SNe
- Stay tuned for our comprehensive results for leptonic ALPs and technical improvements
- Upcoming: search for the time signature of ALP-induced gamma-ray bursts from nearby SNe

(following first steps in *EM*, P. Carenza, C. Eckner, A. Goobar, *Phys.Rev.D* 109 (2024) 2, 2) & loop-induced detection in neutrino detectors

**Thanks for your attention!**

# Back-up slides

# ALPs from SNe: Observables

→ Among the technical advances in our recent work: anisotropic ALP-absorption probability

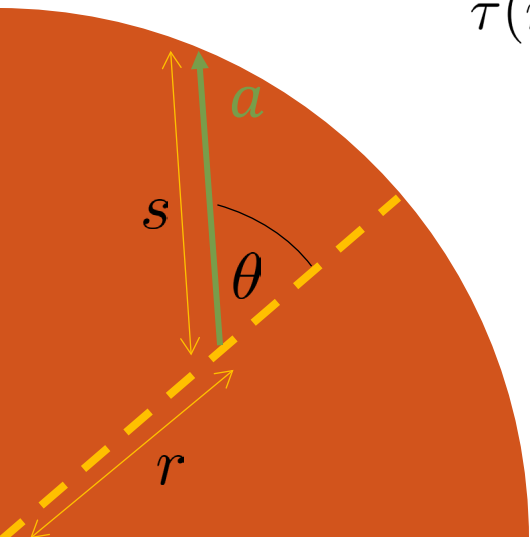
→ In the **Cooling bound** and **Explosion energy bound**, the transmissivity is given as an angular average

$$T(r, t, \omega_a) = \frac{1}{2} \int_{-1}^1 d \cos \theta e^{-\tau(r, t, \omega_a, \cos \theta)}$$

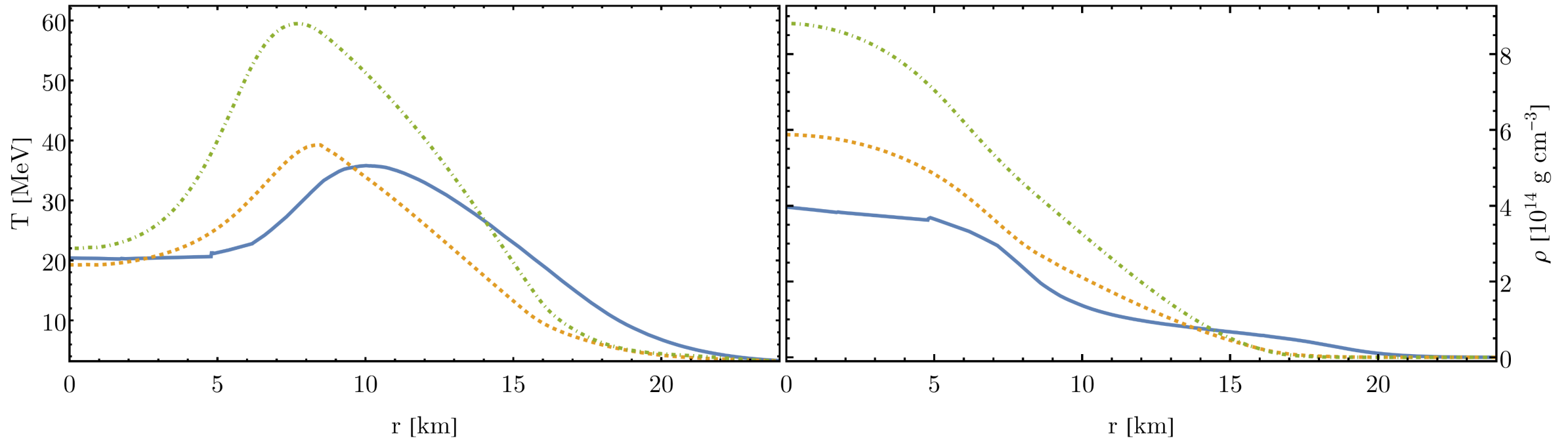
with the optical depth

$$\tau(r, \omega_a, \cos \theta) = \frac{1}{2\pi^2} \int_0^{s_{\max}} ds \frac{\omega_a^2 - m_a^2}{\exp[\omega_a/T(r'(s))] - 1} \left[ \frac{d^2 n_a}{dt d\omega_a}(r'(s), \omega_a) \right]^{-1},$$

$$\text{with } r'(s) = \sqrt{r^2 + s^2 + 2rs \cos \theta}, \quad s_{\max} = \sqrt{R_{\text{far}}^2 - (1 - \cos^2 \theta)r^2} - r \cos \theta$$



# Supernovae – a great lab for new physics



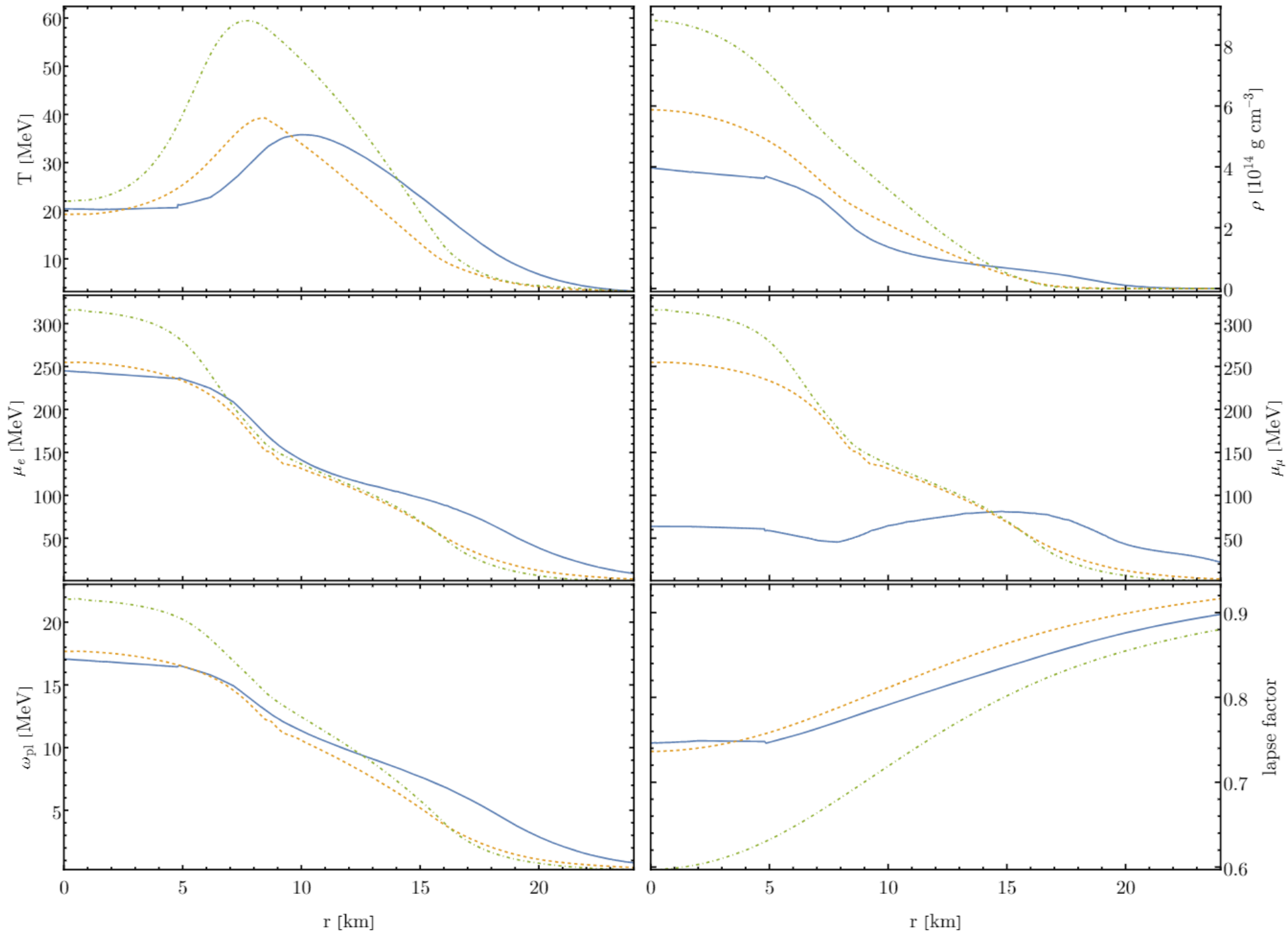
Blue line: “Agile-Boltztran” SN simulation,  
Fischer et al., PRD 104 (2021) 103012  
Green and orange lines: models of the  
“Garching SN Archive”, R. Bollig et al., Phys.  
Rev. Lett. 125 (2020) 051104

Hot and dense plasma  
→ even weakly interacting particles are produced

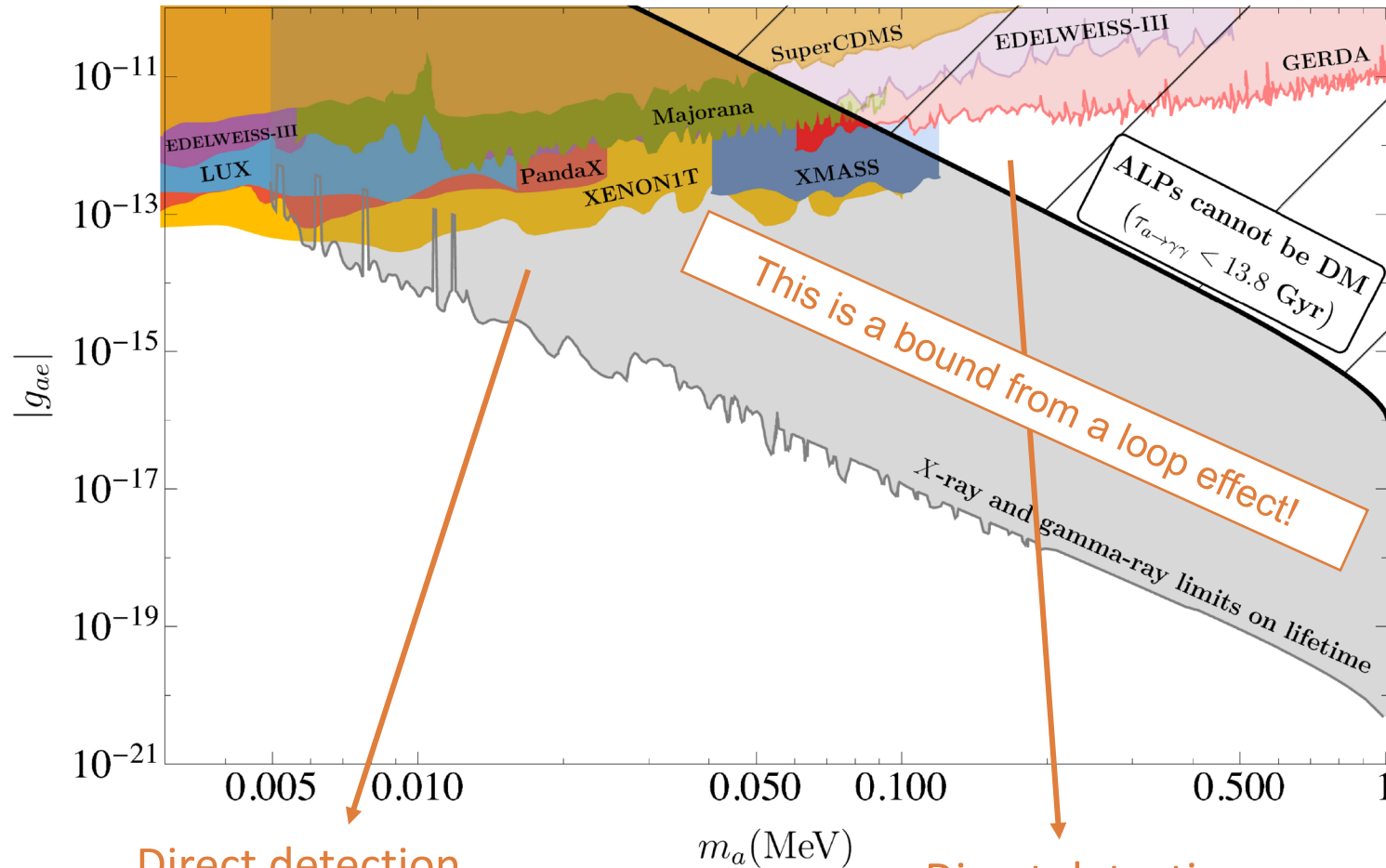
... and they can escape!



# Supernova models from simulations



# ALPs decay into photons



Photophobic ALPs decay at one-loop level with a lifetime of

$$\tau_{a \rightarrow \gamma\gamma} \simeq 13.8 \text{ Gyr} \left( \frac{1.2 \cdot 10^{-12}}{g_{ae}} \right)^2 \left( \frac{100 \text{ keV}}{m_a} \right)^7$$

Ricardo Z. Ferreira, M. C. David Marsh, and **EM**

Phys. Rev. Lett. 128, 221302

See also Pospelov et al. 2008, Arias et al. 2012 for earlier work on this

Direct detection limits are superseded here

Direct detection limits do not apply here

# ALP-electron interactions in a plasma

→ Calculating the bremsstrahlung matrix element with a pseudoscalar ALP-electron interaction yields:

$$\begin{aligned} |\mathcal{M}_{\text{brems}}^{\text{scalar}}|^2 &= (g_{ae})^2 f(m_e^{\text{eff}}, \dots) \\ &\equiv (2m_e \hat{g}_{ae})^2 f(m_e^{\text{eff}}, \dots) \end{aligned}$$

Taking plasma effects into account

→ On the other hand, since the pseudoscalar and derivative interactions lead (in vacuum) to the same matrix element:

$$|\mathcal{M}_{\text{brems}}^{\text{derivative}}|^2 = 4p_e^2 \hat{g}_{ae}^2 f(m_e^{\text{eff}}, \dots) = (2m_e^{\text{eff}} \hat{g}_{ae})^2 f(m_e^{\text{eff}}, \dots)$$

Therefore, apparently  $\mathcal{M}_{\text{brems}}^{\text{derivative}} \neq \mathcal{M}_{\text{brems}}^{\text{scalar}}$  in a plasma. Why is that?

$$\mathcal{L}_{\text{QCD}} = \sum_q \bar{q} (i\not{D} - m_q e^{i\theta_q \gamma_5}) q - \frac{1}{4} G^{a\mu\nu} G_{\mu\nu}^a + \theta \frac{g_s^2}{32\pi^2} G^{a\mu\nu} \tilde{G}_{\mu\nu}^a$$

$$\bar{\theta} = \theta + \theta_q$$

# The original axion

*The landscape of QCD axion models, di Luzio et al., 2003.01100*

## The strong CP problem

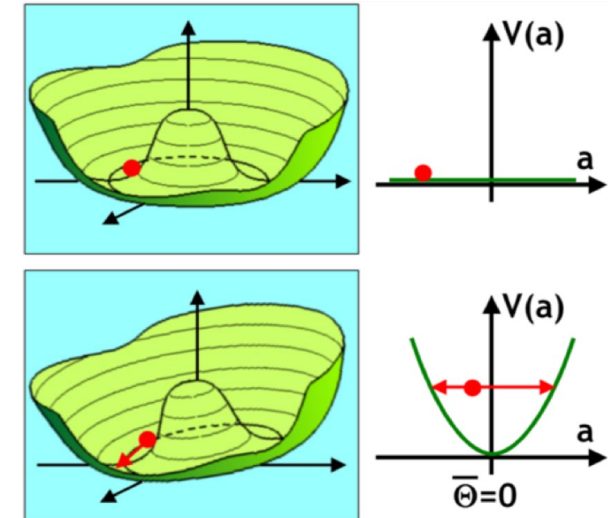
The neutron has no observable electric dipole moment:

$$d_n \lesssim 10^{-26} e \text{ cm}$$

However,  $d_n$  can be calculated from QCD:

$$d_n \simeq 10^{-16} \bar{\theta} e \text{ cm},$$

where a priori  $\bar{\theta} \in [0, 2\pi)$ , but is experimentally found to be very close to zero  $\rightarrow$  fine-tuning problem



Credit: S. Hannestad

## Peccei-Quinn solution

Implement a new, chiral  $U(1)_{PQ}$  symmetry that allows  $\bar{\theta}$  to dynamically relax to zero

The pseudo-Goldstone boson of the spontaneously broken  $U(1)_{PQ}$  is the **axion**

$$\mathcal{L}_a = \frac{g_s^2}{32\pi^2} \frac{a}{f_a} G\tilde{G}$$

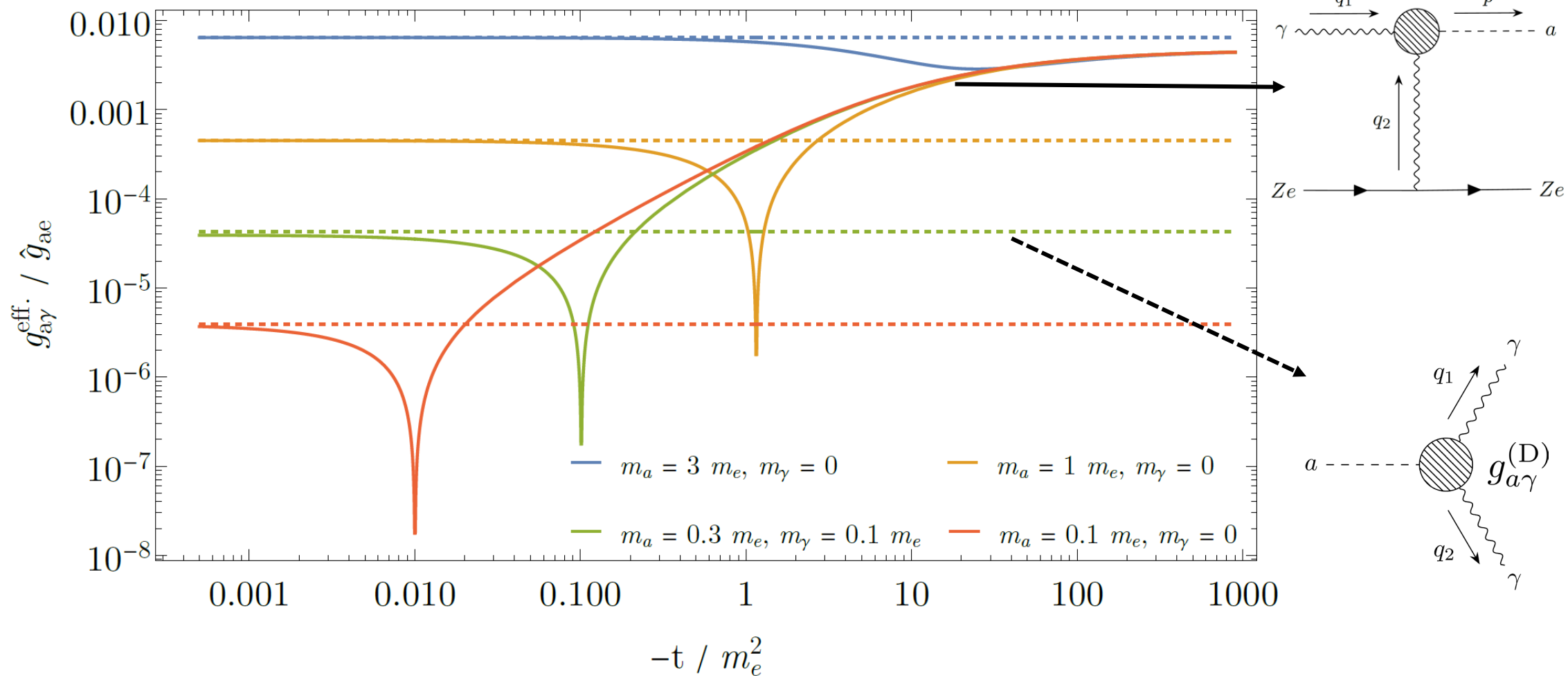
# Running photon coupling

For leptonic ALPs (here  $\ell = e$ ), derive the **renormalization group equations**:

$$\begin{aligned}
 \mu \frac{de}{d\mu} &= -\epsilon e + \frac{1}{12\pi^2} e^3 \\
 \mu \frac{d\hat{g}_{ae}}{d\mu} &= -\epsilon \hat{g}_{ae} + \frac{3}{16\pi^2} e^2 g_{a\gamma} \\
 \mu \frac{dg_{a\gamma}}{d\mu} &= -\epsilon g_{a\gamma} + \frac{1}{6\pi^2} e^2 g_{a\gamma}
 \end{aligned}
 \quad \longrightarrow \quad
 \begin{aligned}
 \alpha(\mu) &\equiv \frac{e^2(\mu)}{4\pi} = \alpha_0 \left( 1 - \frac{\alpha_0}{3\pi} \ln \frac{\mu^2}{\mu_0^2} \right)^{-1} \\
 \hat{g}_{ae}(\mu) &= \hat{g}_{ae}^\Lambda - \frac{9}{8} \frac{g_{a\gamma}^\Lambda}{g_{a\gamma}} \left[ 1 - \frac{\alpha(\mu)}{\alpha(\Lambda)} \right] \\
 g_{a\gamma}(\mu) &= g_{a\gamma}^\Lambda \frac{\alpha(\mu)}{\alpha(\Lambda)}
 \end{aligned}$$

→ There is **no RG-induced running photon coupling** for leptonic ALPs  
 (This is also true in the full SM)

# The effective ALP-photon coupling



$$t = q_2^2 = (p - q_1)^2$$