Probing neutrino nonradiative decay with supernova neutrinos

PILAR IVÁÑEZ BALLESTEROS (she/her)

PhD supervisor: DR. M. C. VOLPE

APC – UNIVERSITÉ PARIS CITÉ

Outline

1. Standard SN neutrino emission

2. Neutrino decay in matter
   - SN1987A

   [P.I.B. and Volpe, arXiv:2410.11517]

3. Neutrino decay in vacuum:

   [P.I.B. and Volpe, PLB847 (2023) 138252]
   - SN1987A
   - DSNB [P.I.B. and Volpe, PRD107 (2023) 023017]

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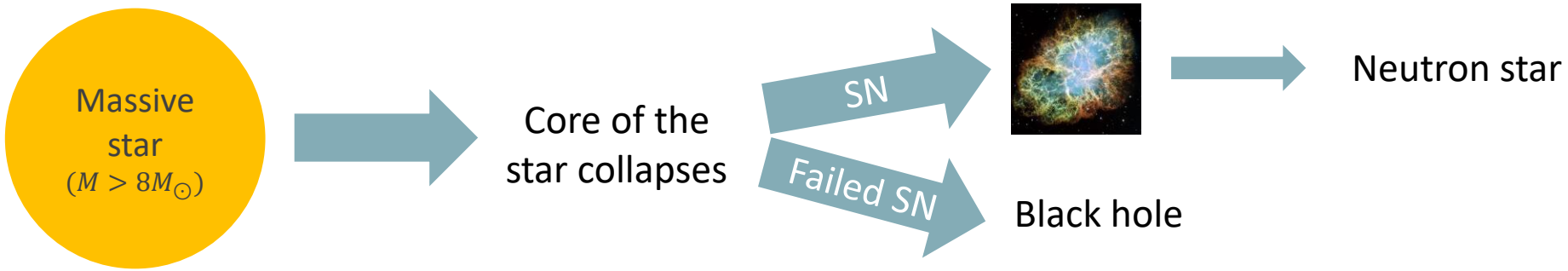
Supernova neutrinos



- **Powerful source of neutrinos**: $\sim 10^{53}$ erg emitted in all flavours (99% of gravitational binding energy!)

  ➡ interesting information can be obtained if we detect these neutrinos!

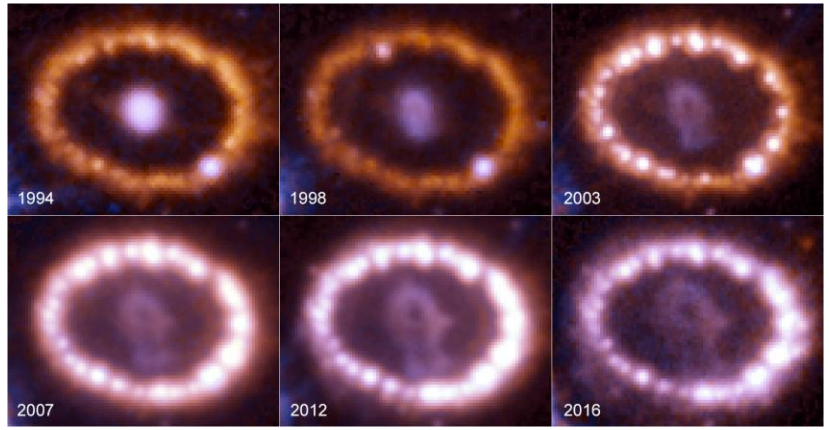
- We are sensitive to galactic supernova, BUT these are <u>rare events</u> (1-3 per century)

- Only detection was **SN1987A** (50 kpc away)

  ↳ <u>24 events</u> detected by Kamiokande-II, IMB, and Baksan
  [Hirata *et al.*, 1987] [Bionta *et al.*, 1987] [Alekseyev *et al.*, 1988]

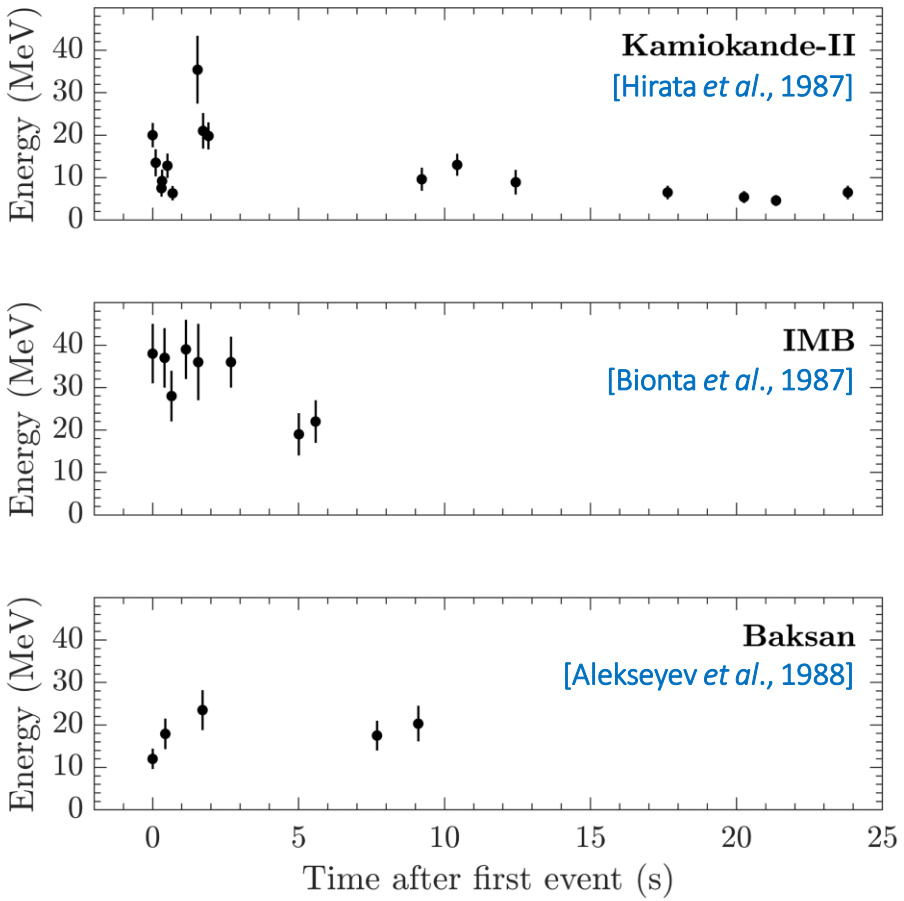
❖ **Diffuse Supernova Neutrino Background** (DSNB):

flux of all neutrinos and antineutrinos emitted by past supernovae



Evolution of SN 1987A. Hubble Space Telescope
https://www.esa.int/About_Us/ESAC/The_evolution_of_SN_1987A

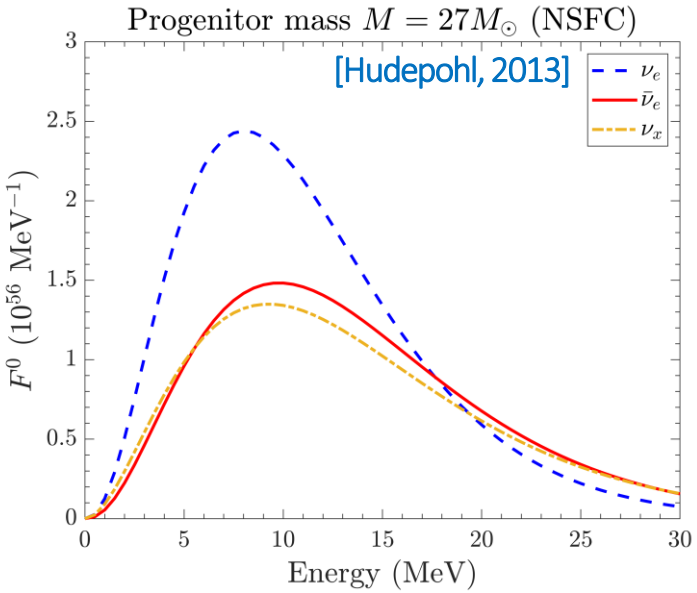
SN1987A

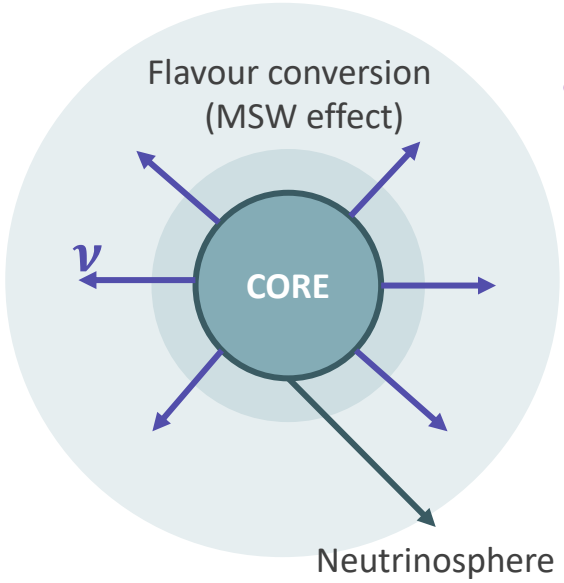


- First and only detection of SN neutrinos
- Explosion of a blue supergiant located at the Large Magellanic Cloud (~ 50 kpc)
- **24 $\bar{\nu}_e$ events** detected via Inverse Beta Decay
  - K-II (2.14 kton): 11 events (above 7.5 MeV)
  - IMB (6.8 kton): 8 events
  - Baksan (0.28 kton): 5 events
- Total energy associated to $\bar{\nu}_e$ events: $\sim \mathbf{5 \times 10^{52}}$**erg**
- $\bar{\nu}_e$ spectra agreed with $\boldsymbol{T = 4}$ **MeV**

Standard neutrino emission from a single collapse

- Emission depends on: outcome of the collapse, progenitor characteristics…
- Flux at the neutrinosphere, $\phi^0_{\nu_\alpha}$:
  - It can be parametrised by a **power-law distribution**: $\mathcal{L}_{\nu_\alpha}$, $\langle E_{\nu_\alpha} \rangle$, α_{ν_α} [Keil *et al.*, 2003]
  - Luminosity of $\mathcal{L}_{\nu_\alpha} \sim 10^{52}$ erg
  - $\langle E_{\nu_\alpha} \rangle$: average energy $(\sim 9 - 18 \text{ MeV}) \rightarrow \langle E_{\nu_e} \rangle < \langle E_{\bar{\nu}_e} \rangle < \langle E_{\nu_x} \rangle$
  - $\alpha_{\nu_\alpha} \sim 2 - 3$





- Flavour effects inside supernova:
  - **Mikheev-Smirnov-Wolfenstein (MSW) effect**: describes the **flavour transformations** due to the ν-matter interactions. [Wolfenstein, 1978] [Mikheev and Smirnov, 1986]

    MSW effect inside SN is assumed to be adiabatic $\rightarrow \phi_{\bar{\nu}_l} = \phi^0_{\bar{\nu}_e}$; $\phi_{\bar{\nu}_i} = \phi_{\bar{\nu}_h} = \phi^0_{\nu_x}$
  - Other effects still under study: shock wave effects, ν–ν interactions… see e.g. the review Volpe (2023)

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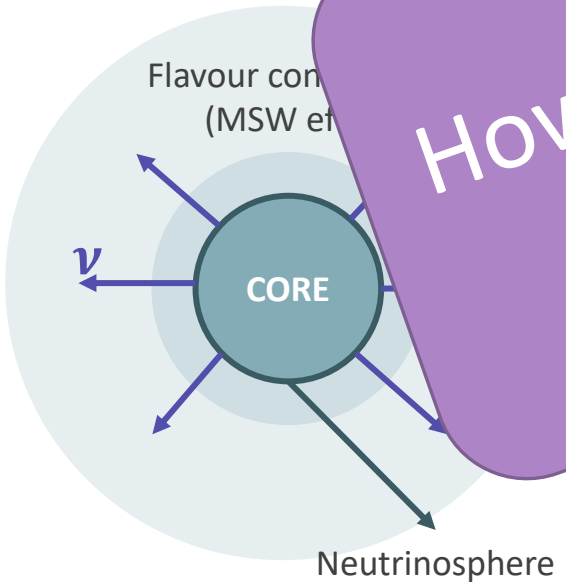
  - $\alpha_{\nu_\alpha} \sim 2 - 3$

How does **neutrino decay** (in matter or vacuum) affect this picture?



(MSW) effect: describes the **flavour transformations**
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   [P.I.B. and Volpe, arXiv:2410.11517]

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   - SN1987A
   - DSNB

Neutrino decay to Majorons in supernovae

We consider interactions between neutrinos and massless Majorons, J:

$$\mathcal{L} \propto \sum_{i,j} g_{ij} \bar{\nu}_i \gamma_5 \nu_j J$$

- Coupling matrix diagonal in mass basis: $\boldsymbol{g_{ij} \propto m_i \delta_{ij}}$ [Schechter and Valle, 1982]
- Interactions of neutrinos with the medium: $V_{\nu_e} = V_{CC} + V_{NC}, \quad V_{\nu_x} = V_{NC}$

$$V_{CC} = \sqrt{2} G_F n_B \left(Y_e + Y_{\nu_e}\right) \text{ and } V_{NC} = \sqrt{2} G_F n_B \left(-\frac{1}{2} Y_N + Y_{\nu_e}\right)$$

  - $\boldsymbol{\tilde{g}_{ij}}$**: non-diagonal:**

    Processes like $\nu^{\pm} \rightarrow \nu^{\mp} + J$ are allowed and can affect the neutrino emission

Limits to coupling of neutrinos and massless Majorons from SNe: see e.g. [Choi *et al.*, 1988], [Berezhiani and Smirnov, 1989], [Farzan, 2003], …

- Energy-loss argument: $\mathcal{L}_J < 5 \times 10^{52} \text{erg/s} \rightarrow 3 \times 10^{-7} \lesssim g_{\alpha\beta} \lesssim 2 \times 10^{-5}$ excluded
- Deleptonization argument: $Y_L(t_{\text{bounce}}) \geq 0.375 \rightarrow g_{ee} \lesssim 2 \times 10^{-6}$

} [Kachelriess *et al.*, 2000]

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Limits to coup… …mirnov, 1989], [Farzan, 2003], …

- Energy-loss …
- Deleptonizat… …*et al.*, 2000]

CAN WE OBTAIN INFORMATION ON THE NEUTRINO-MAJORON COUPLINGS USING A **LIKELIHOOD ANALYSIS** OF SN1987A DATA?

Decay of (anti)neutrinos

Hamiltonian: $H_{\rm tot} = \underbrace{H_0}_{\text{vacuum}} + \underbrace{\sum_{i,j} \bar{\nu}_i V_{ij} \nu_j}_{\text{medium}} + \underbrace{g_{ij} \bar{\nu}_i \gamma_5 \nu_j J}_{\text{interaction}}$

[Kachelriess *et al.*, 2000]
[P.I.B. and Volpe, arXiv:2410.11517]

Coupling matrix in matter, $\tilde{g}_{ij}$, is non-diagonal and $\boldsymbol{\tilde{g}_{ij} \approx g_{\alpha'\beta'}}$ **at very high densities**

- Decay rate for $\nu_\alpha^{\pm} \to \nu_\beta^{\mp} + J$ (helicity flipping)

$$\Gamma_{\alpha\beta} = \frac{g_{\alpha\beta}^2}{16\pi}(V_\alpha - V_\beta)$$

Decay is **only allowed for** $\boldsymbol{V_\alpha - V_\beta > 0}$

→ for the profiles* we considered, only **satisfied by $\bar{\nu}$ decay**: $\bar{\nu}_\alpha \to \nu_\beta + J$

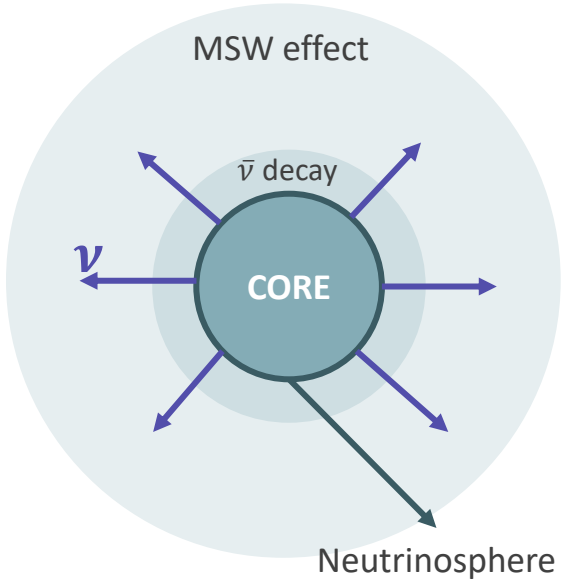
- Survival probability: (in general, a function of time and energy)

$$N_{\bar{\nu}_\alpha}(E, \boldsymbol{t}) = \exp\left\{ - \int_{\boldsymbol{R_{E,\bar{\nu}_\alpha}(t)}}^{\boldsymbol{R_{T,\bar{\nu}_\alpha}(t)}} \frac{\boldsymbol{dr'}}{\boldsymbol{v(E, r', t)}} \boldsymbol{\Gamma_{\bar{\nu}_\alpha}(r', t)} - \int_{R_{T,\bar{\nu}_\alpha}(t)}^{\infty} dr' \Gamma_{\bar{\nu}_\alpha}(r', t) \right\}$$

$R_{E,\bar{\nu}_\alpha}$ and $R_{T,\bar{\nu}_\alpha}$ are the energy- and transport-spheres

- $\boldsymbol{\bar{\nu}_\alpha}$ fluxes after decay:

$$\boldsymbol{\phi^d_{\bar{\nu}_\alpha}(E, t) = N_{\bar{\nu}_\alpha}(E, t) \phi^0_{\bar{\nu}_\alpha}(E, t)}$$



*We used SN profiles and fluxes from the 1D simulations by the Garching group. https://wwwmpa.mpa-garching.mpg.de/ccsnarchive/archive.html These models agree well with SN1987A data. [Fiorillo *et al.* (2023)]

Limits to ν-Majoron coupling

- **2D unbinned likelihood analysis** of SN1987A time-independent data:

g_{11}, m_1 **(NO):**

$$g_{22} = g_{11}\sqrt{1 + \frac{\Delta m^2_{21}}{m^2_1}}$$

$$g_{33} = g_{11}\sqrt{1 + \frac{\Delta m^2_{31}}{m^2_1}}$$

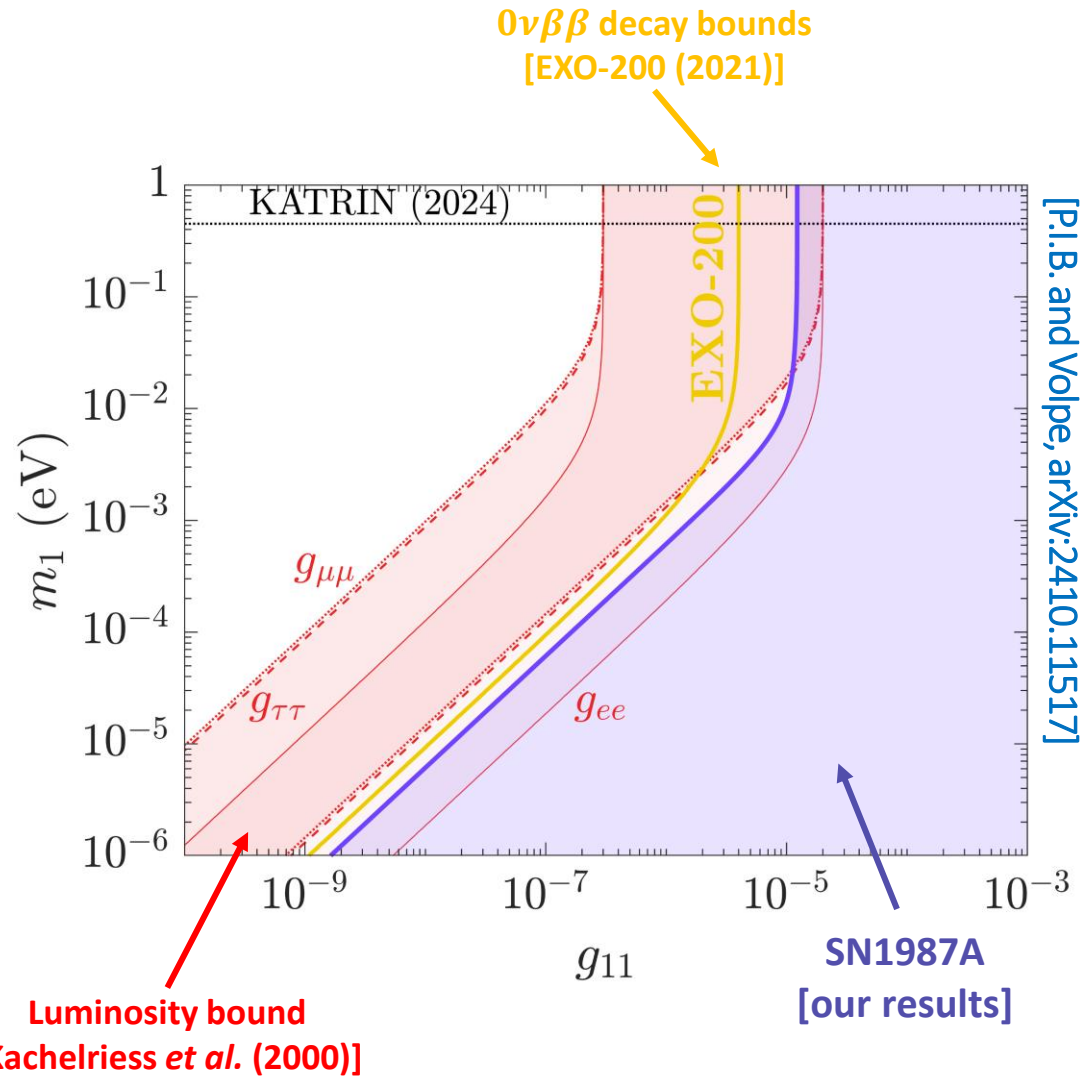
Using profiles and fluxes from the model **1.44SFHx**
https://wwwmpa.mpa-garching.mpg.de/ccsnarchive/archive.html
[Fiorillo *et al.* (2023)]

- Luminosity bound: $\mathcal{L}_J < 5 \times 10^{52}$ erg/s

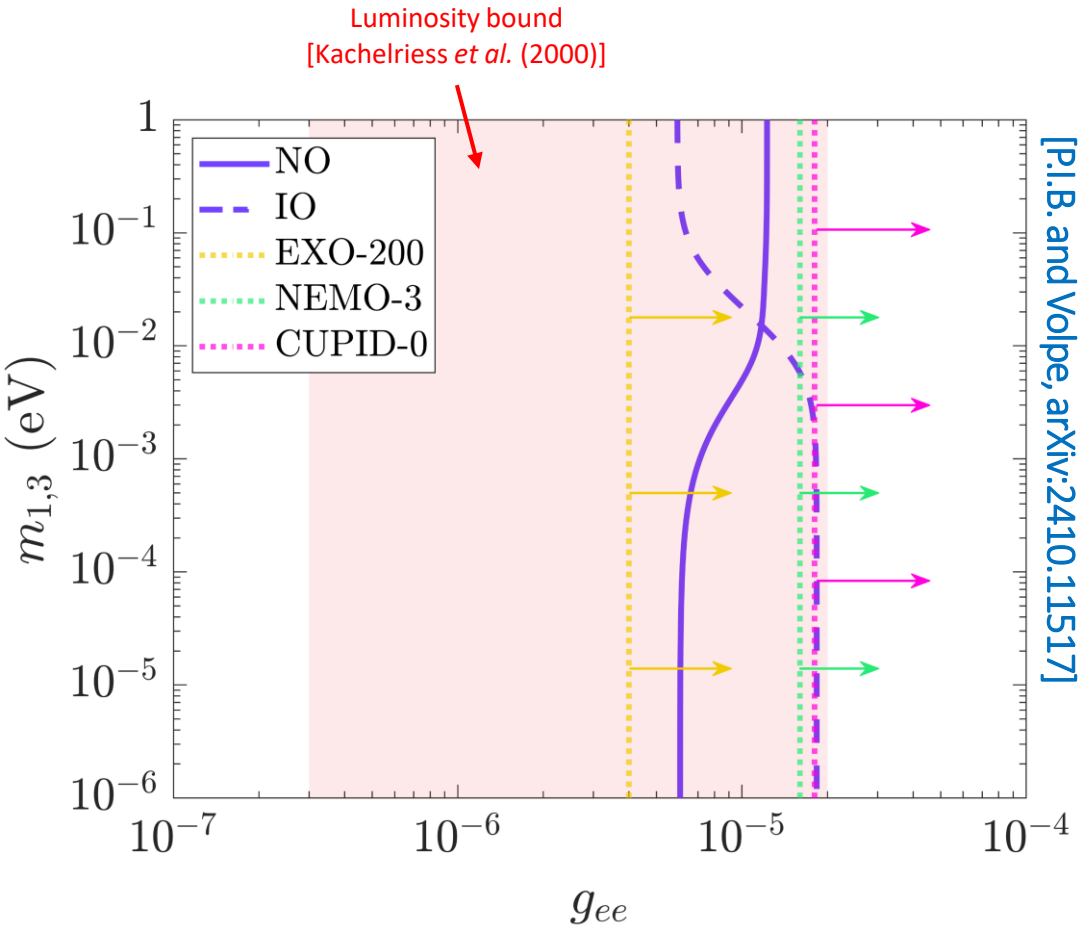
$$3 \times 10^{-7} \lesssim g_{\alpha\alpha} \lesssim 2 \times 10^{-5} \text{ (exclusion)}$$

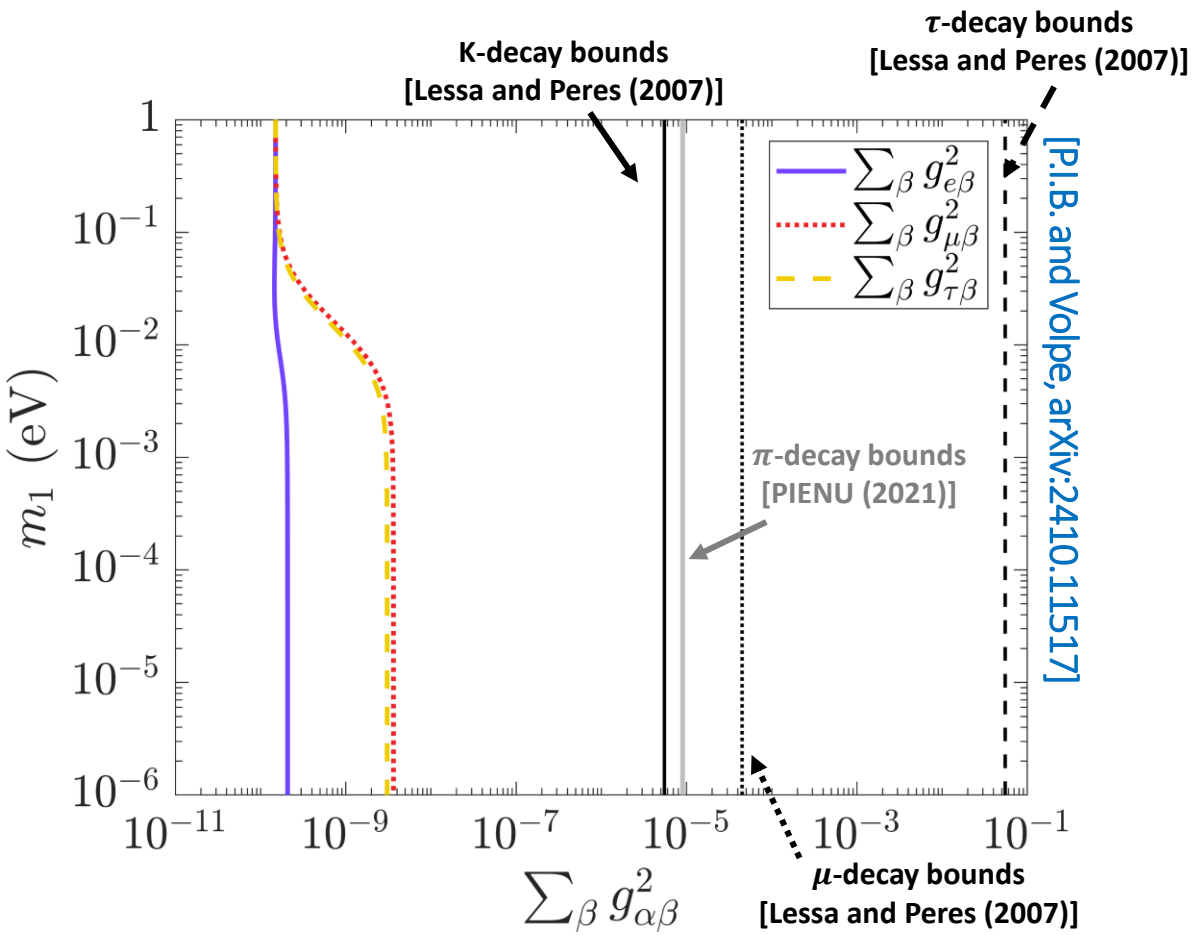
- $0\nu\beta\beta$ bounds only on g_{ee}:

EXO-200: $g_{ee} < (0.4 - 0.9) \times 10^{-5}$



Limits to ν-Majoron coupling: flavour basis





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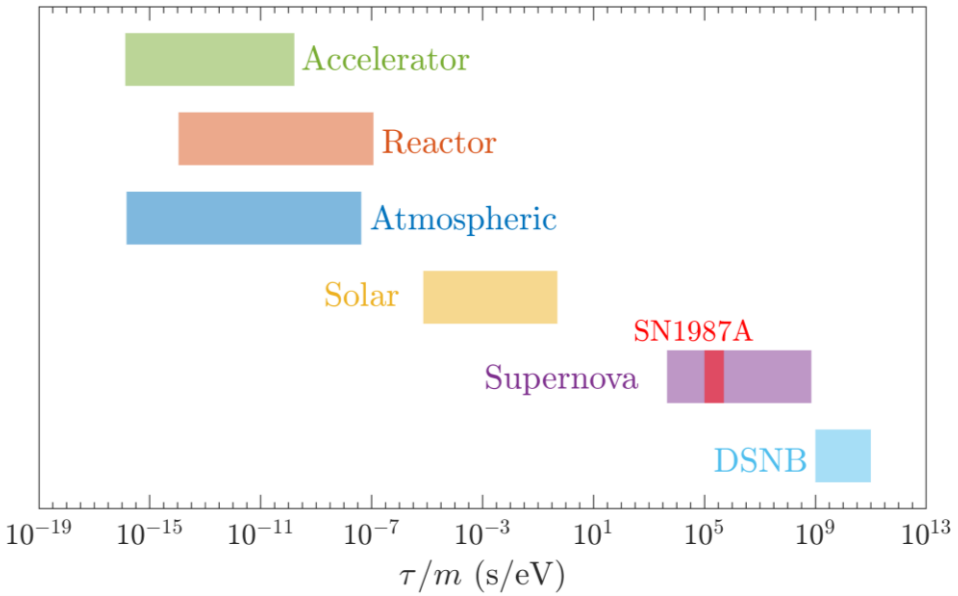
Neutrino nonradiative decay in vacuum

$$\nu_j \longrightarrow \nu_i \, (\overline{\nu}_i) + X$$

where $m_j > m_i$ and X is a very light (pseudo)scalar particle (e.g. Majoron).

Neutrino fluxes deplete over a distance L due to decay by a factor: $\mathbf{exp}\left(-\frac{m_i L}{\tau_i E}\right)$



Sensitivities to the lifetime-to-mass ratio, τ/m, for different experiments. Figure taken from P.I.B. and Volpe, PLB 2023.

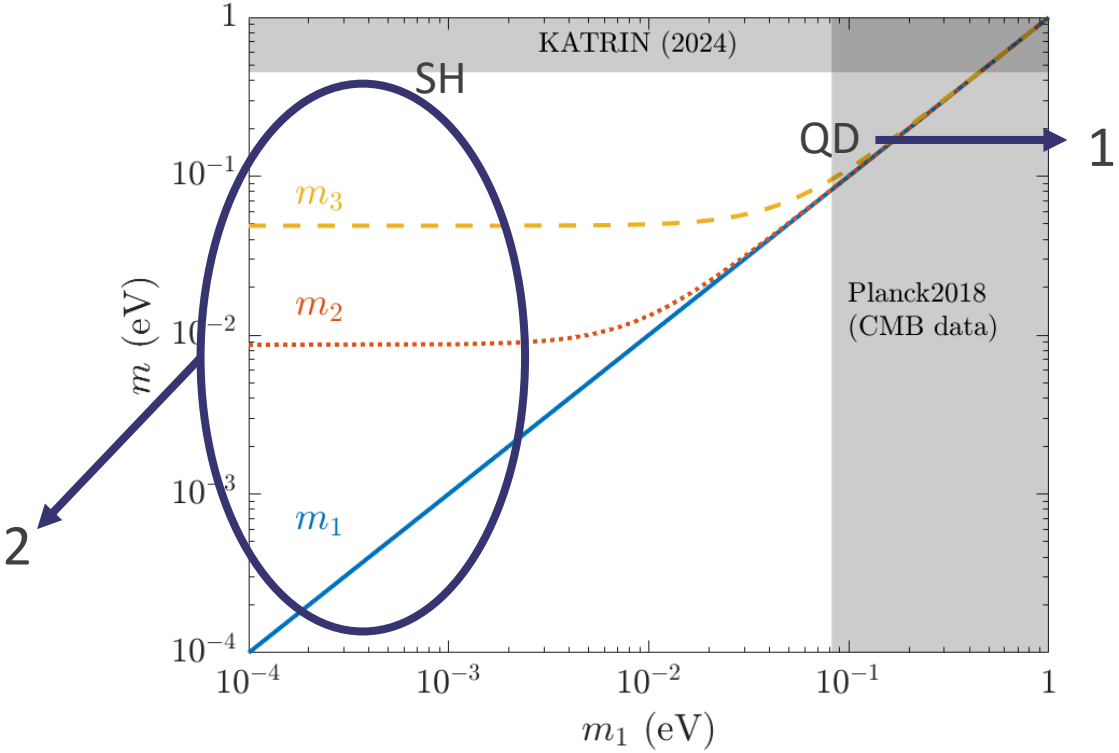
DSNB has unique sensitivity to this decay in the range:

$$\frac{\tau}{m} \in \left[10^9 - 10^{11}\right] \text{s/eV}$$

[Ando, 2003], [Fogli *et al.*, 2004], [de Gouvêa *et al.*, 2020], [Tabrizi and Horiuchi, 2021]

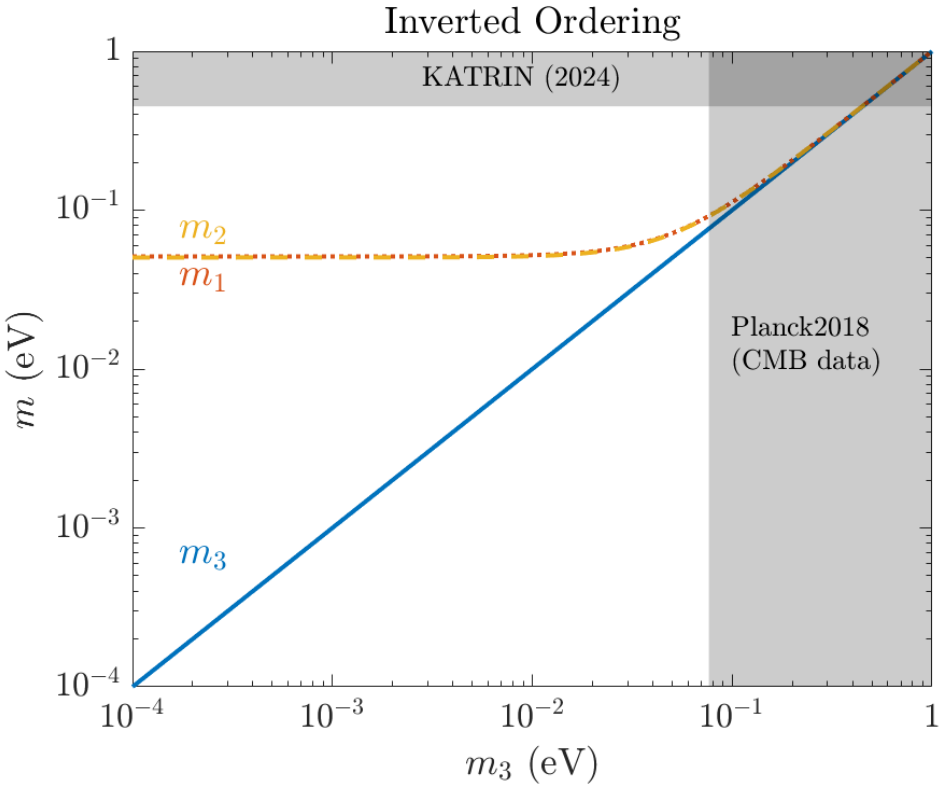
Mass ordering cases

Absolute neutrino masses as a function of the lightest neutrino. The shaded regions are excluded by KATRIN and Planck2018 (CMB data).



NORMAL ORDERING:

1. **QD** $\Longrightarrow m_1 \simeq m_2 \simeq m_3 \gg \Delta m_{ij}$
2. **SH** $\Longrightarrow m_3 \gg m_2 \gg m_1 \simeq 0$



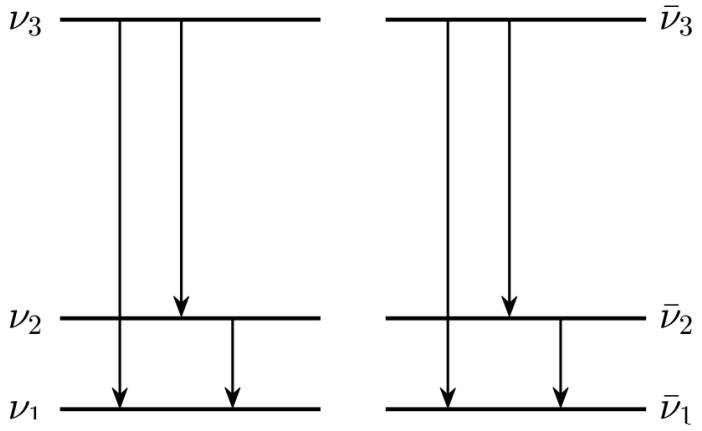
INVERTED ORDERING:

- QD $\Longrightarrow m_1 \simeq m_2 \gg \Delta m_{21}$
- SH $\Longrightarrow m_{1,2} \gg m_3 \simeq 0$

Decay patterns

NO and QD masses.

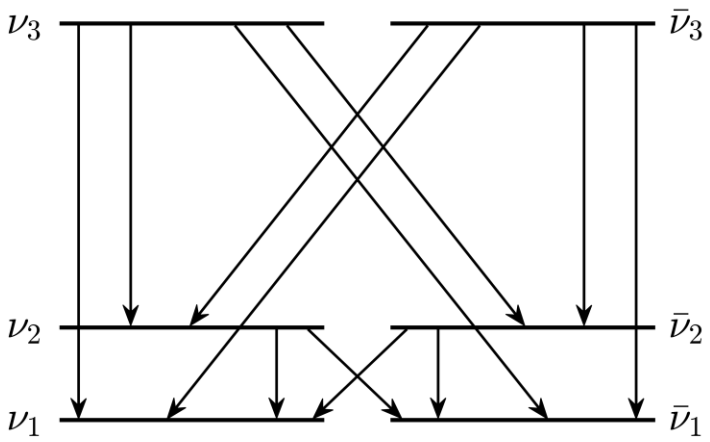
$$m_1 \simeq m_2 \simeq m_3 \gg \Delta m_{ij}$$



- $\tau_3/m_3 = \tau_2/m_2 = \tau/m$
- $B(\nu_3 \to \nu_2) = B(\nu_3 \to \nu_1) = \frac{1}{2}$
- $B(\nu_2 \to \nu_1) = 1$

NO and SH masses.

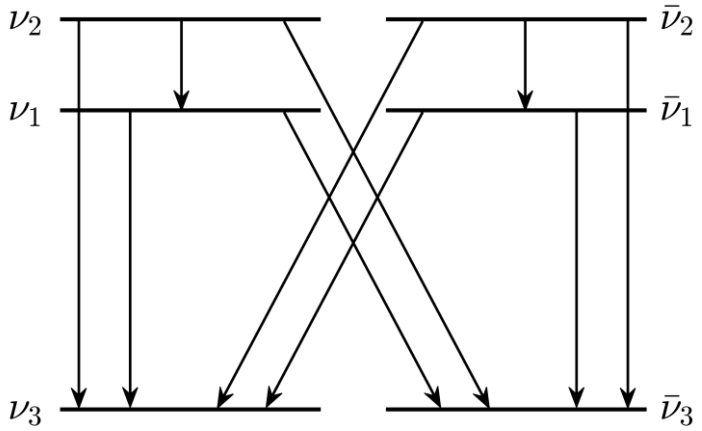
$$m_3 \gg m_2 \gg m_1 \simeq 0$$



- $\tau_3/m_3 = \tau_2/m_2 = \tau/m$
- $B(\nu_3 \to \nu_i) = B(\nu_3 \to \bar{\nu}_i) = \frac{1}{4}$
- $B(\nu_2 \to \nu_1) = B(\nu_2 \to \bar{\nu}_1) = \frac{1}{2}$

IO

$$m_1 \simeq m_2 \gg m_3 \simeq 0$$



- $\tau_1/m_1 = \tau_2/m_2 = \tau/m$
- $B(\nu_2 \to \nu_1) = \frac{1}{2}$
- $B(\nu_2 \to \nu_3) = B(\nu_2 \to \bar{\nu}_3) = \frac{1}{4}$
- $B(\nu_1 \to \nu_3) = B(\nu_1 \to \bar{\nu}_3) = \frac{1}{2}$

Limits on τ/m from SN1987A data

[P.I.B. and Volpe, PLB847 (2023) 138252]

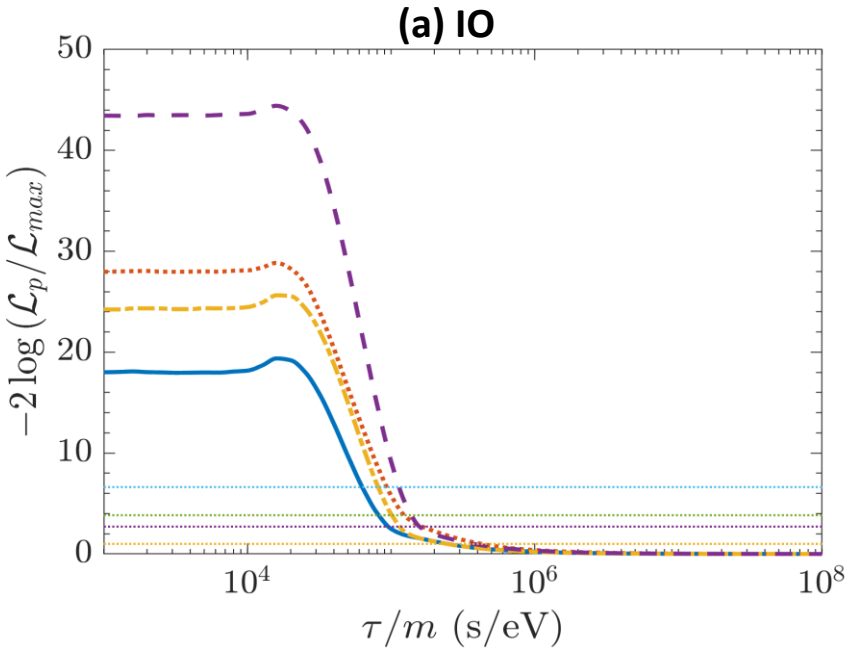
7D likelihood analysis of SN1987A data to obtain τ/m

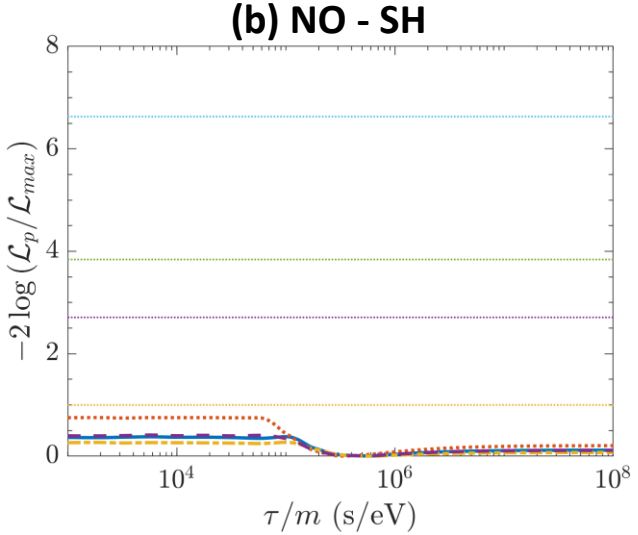
↳ Parameters considered: $L_{\nu_\alpha}, \langle E_{\nu_\alpha} \rangle$ with $\nu_\alpha = \nu_e, \bar{\nu}_e, \nu_x$ and τ/m (fixed $\alpha = 2.3$)

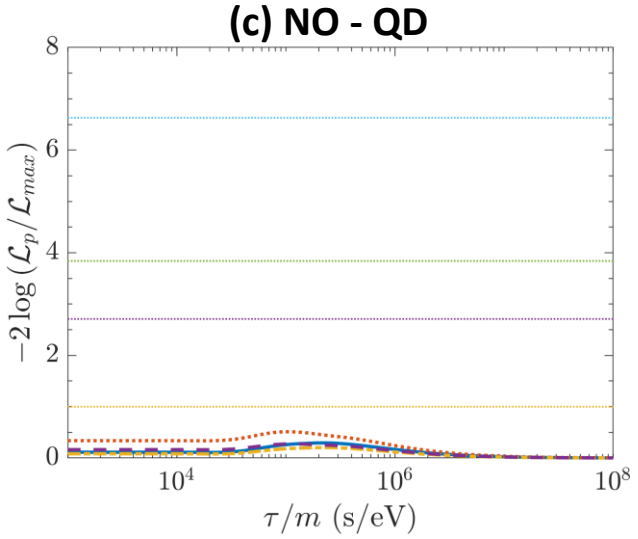
- Normal ordering: no sensitivity
- Inverted ordering: $\frac{\tau}{m} \geq 1.2 \times 10^5$ s/eV at 90% CL.

Profile likelihood ratios from the 7D likelihood analysis of SN1987A events: **(a)** inverted ordering, **(b)** normal ordering and strongly hierarchical masses, **(c)** normal ordering and quasidegenerate masses.
The curves correspond to the analysis:

- including Baksan data and background data (dot-dashed line);
- without Baksan data and with background (solid line);
- with Baksan data and without background data (dotted line); and,
- without Baksan data and background data (dashed line).







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   - **DSNB** [P.I.B. and Volpe, PRD107 (2023) 023017]

DSNB flux

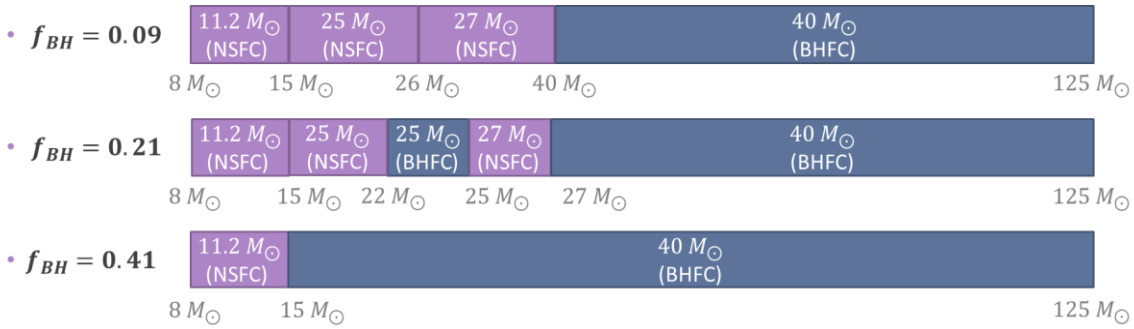
see e.g. [Beacom, 2010], [Priya and Lunardini, 2017], [Møller *et al.*, 2018], [de Gouvêa *et al.*, 2020], …

$$\phi_\nu(E) = \int_0^{z_{max}} \frac{dz}{H(z)} \int_{8\,M_\odot}^{125\,M_\odot} dM\, \dot{R}_{SN}(z, M) F_\nu(E', M) \qquad E' = E(1+z)$$

Hubble parameter:
accounts for Universe expansion. We consider a ΛCDM model.

Supernova rate:
proportional to the star formation rate. The normalization of SNR is one of the largest uncertainties of the DSNB

Neutrino emission from a single collapse:
The emission depends on the outcome of the collapse (NS or BH)



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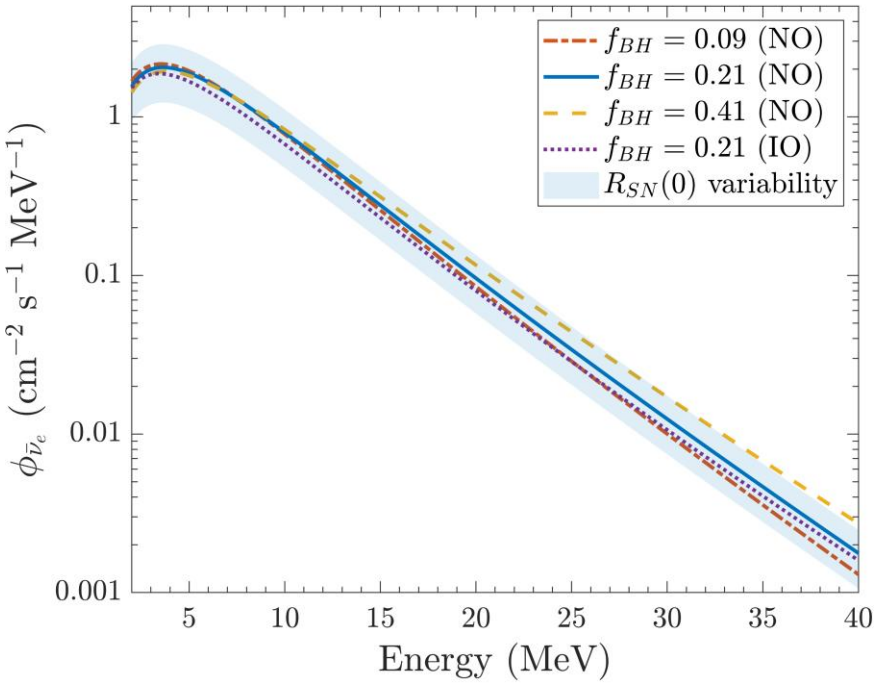
Results for the integrated flux in $\mathrm{cm}^{-2}\mathrm{s}^{-1}$ for the fiducial case ($f_{BH} = 0.21$) and the most optimistic case ($f_{BH} = 0.41$) in brackets:

	NO	IO	UPPER LIMITS
$\bar{\nu}_e$ ($E_\nu > 17.3$ MeV)	0.77 ± 0.30 $[1.02 \pm 0.41]$	0.63 ± 0.25 $[0.75 \pm 0.3]$	2.6 (SK)
ν_e ($22.9 < E < 36.9$ MeV)	0.20 ± 0.08 $[0.24 \pm 0.09]$	0.18 ± 0.08 $[0.23 \pm 0.09]$	19 (SNO)



[P.I.B. and Volpe, PRD107 (2023) 023017]

Flux of $\bar{\nu}_e$ on Earth for different f_{BH} in absence of decay. The band shows the uncertainty of the SNR normalisation. Results obtained using 1D SN simulations from Garching group.

How can we detect the DSNB?

- Detection of $\bar{\nu}_e$ flux → **Inverse Beta Decay** (IBD)

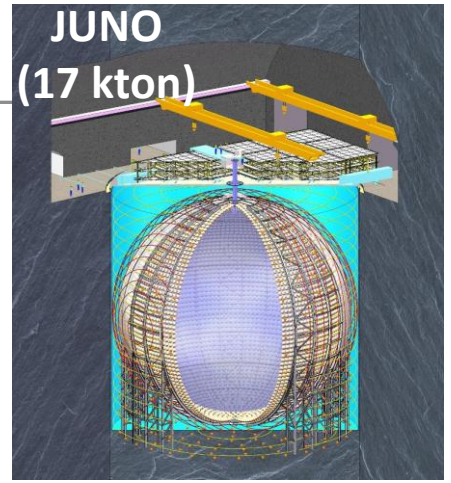
$$\bar{\nu}_e + p \rightarrow n + e^+$$

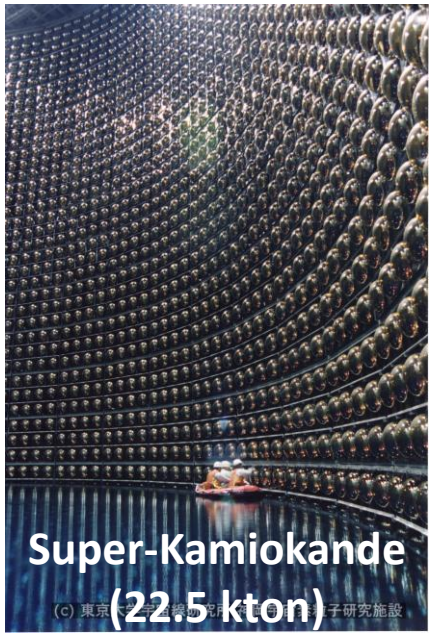
  - **Super-Kamiokande + Gd, Hyper-Kamiokande, JUNO**
  - Backgrounds: reactor $\bar{\nu}_e$ (low energies) and atmospheric ν (high energies)

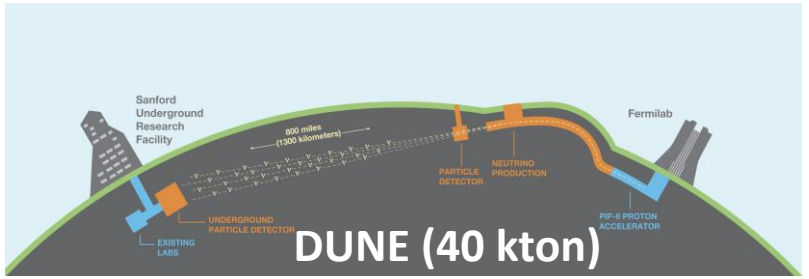
- Detection of ν_e flux → **neutrino absorption in ^{40}Ar**

$$\nu_e + {}^{40}Ar \rightarrow {}^{40}K^* + e^-$$

  - **Deep Underground Neutrino Experiment (DUNE)**
  - Backgrounds: solar neutrinos (low energies) and atmospheric ν_e (high energies)



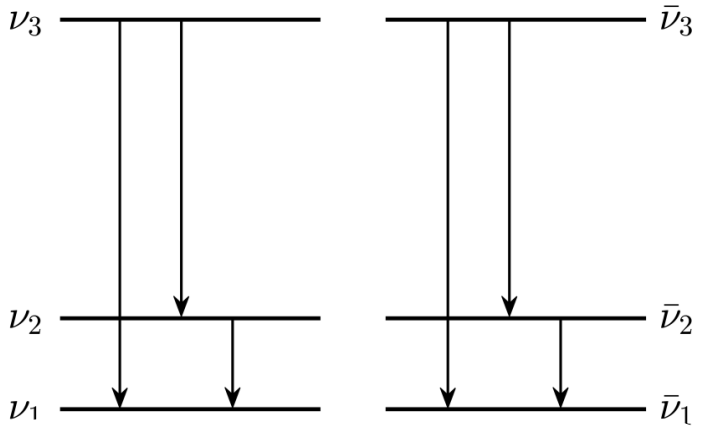




Decay patterns

NO and QD masses.

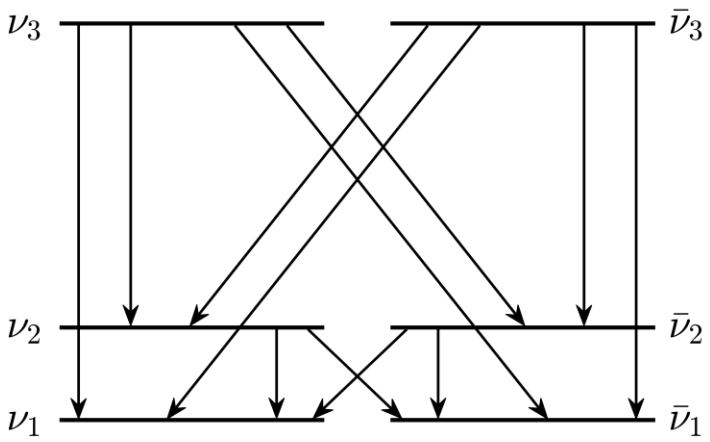
$$m_1 \simeq m_2 \simeq m_3 \gg \Delta m_{ij}$$



- $\tau_3/m_3 = \tau_2/m_2 = \tau/m$
- $B(\nu_3 \to \nu_2) = B(\nu_3 \to \nu_1) = \frac{1}{2}$
- $B(\nu_2 \to \nu_1) = 1$

NO and SH masses.

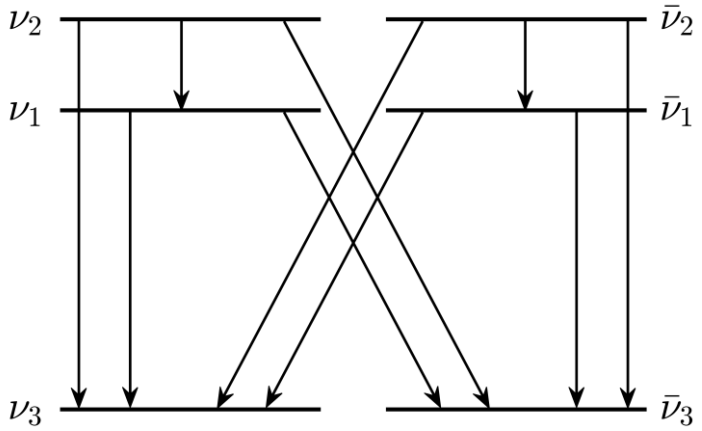
$$m_3 \gg m_2 \gg m_1 \simeq 0$$



- $\tau_3/m_3 = \tau_2/m_2 = \tau/m$
- $B(\nu_3 \to \nu_i) = B(\nu_3 \to \bar{\nu}_i) = \frac{1}{4}$
- $B(\nu_2 \to \nu_1) = B(\nu_2 \to \bar{\nu}_1) = \frac{1}{2}$

IO

$$m_1 \simeq m_2 \gg m_3 \simeq 0$$



- $\tau_1/m_1 = \tau_2/m_2 = \tau/m$
- $B(\nu_2 \to \nu_1) = \frac{1}{2}$
- $B(\nu_2 \to \nu_3) = B(\nu_2 \to \bar{\nu}_3) = \frac{1}{4}$
- $B(\nu_1 \to \nu_3) = B(\nu_1 \to \bar{\nu}_3) = \frac{1}{2}$

Predictions for the DSNB: Normal Ordering

* Results obtained for our fiducial case, $f_{BH} = 0.21$. The bands show the uncertainty of the SNR normalisation.

[P.I.B. and Volpe, PRD107 (2023) 023017]

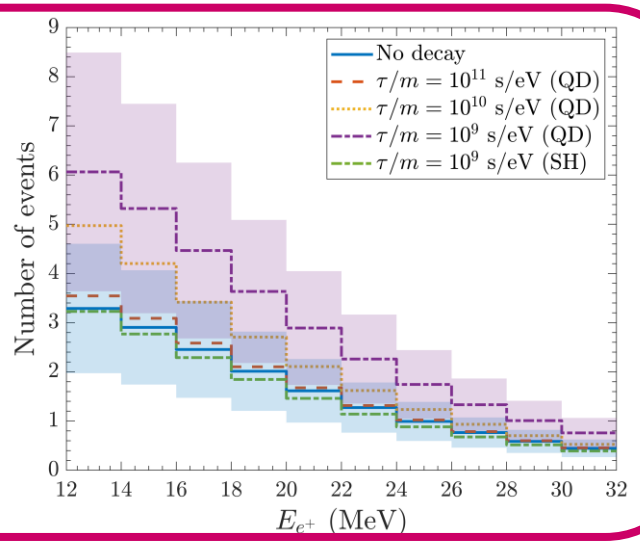
SK-Gd:

$N_{tot} = 14$ (no decay)

Exposure time: 10 years

Energy window:

$12.8 \leq E_\nu \leq 30.8$ MeV



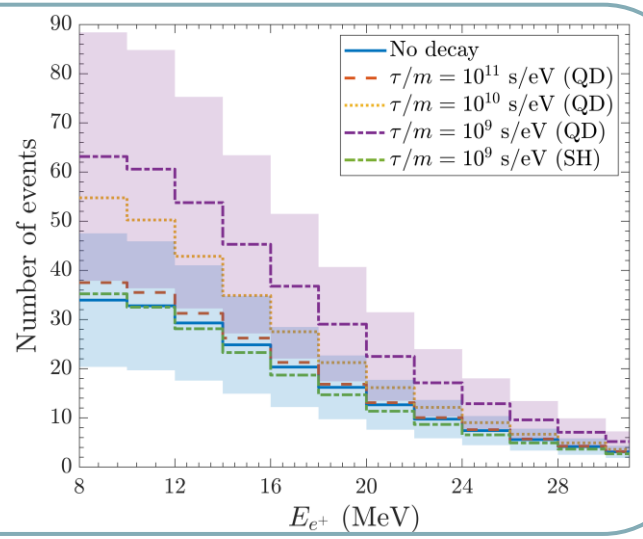
HK-Gd:

$N_{tot} = 76$ (no decay)

Exposure time: 20 years

Energy window:

$17.3 \leq E_\nu \leq 31.3$ MeV



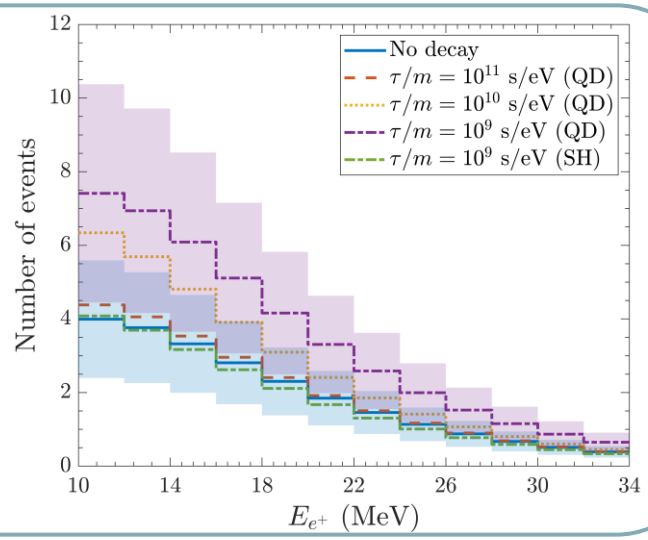
JUNO:

$N_{tot} = 20$ (no decay)

Exposure time: 20 years

Energy window:

$11.3 \leq E_\nu \leq 33.3$ MeV



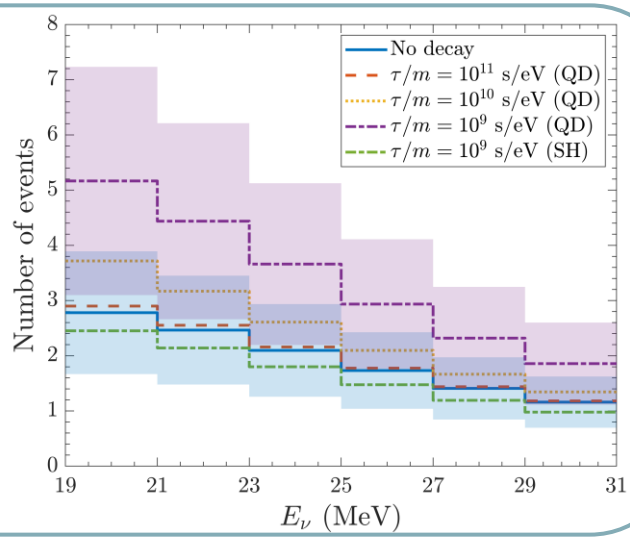
DUNE:

$N_{tot} = 12$ (no decay)

Exposure time: 20 years

Energy window:

$19 \leq E_\nu \leq 31$ MeV



Predictions for the DSNB: Inverted Ordering

* Results obtained for our fiducial case, $f_{BH} = 0.21$. The bands show the uncertainty of the SNR normalisation.

[P.I.B. and Volpe, PRD107 (2023) 023017]

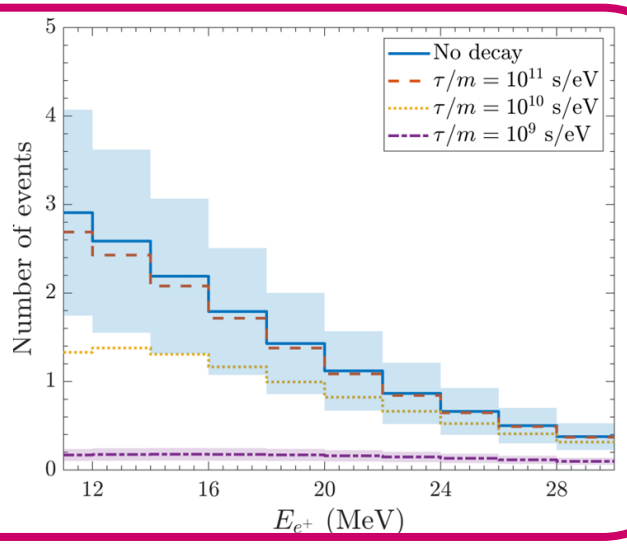
SK-Gd:

$N_{tot} = 12$ (no decay)

Exposure time: 10 years

Energy window:

$12.8 \leq E_\nu \leq 30.8$ MeV



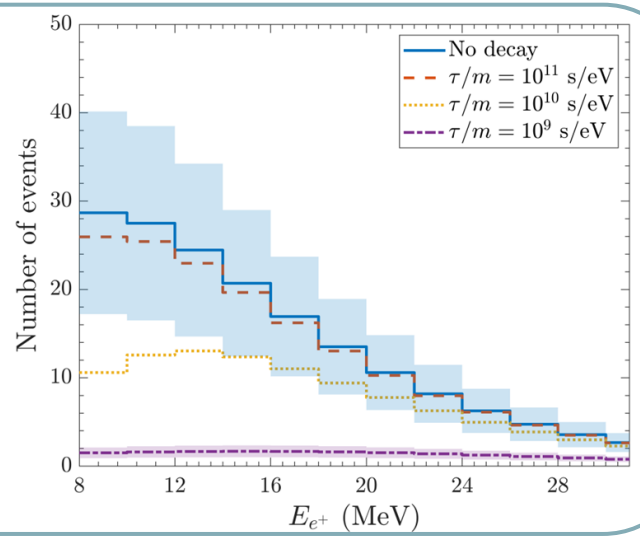
HK-Gd:

$N_{tot} = 64$ (no decay)

Exposure time: 20 years

Energy window:

$17.3 \leq E_\nu \leq 31.3$ MeV



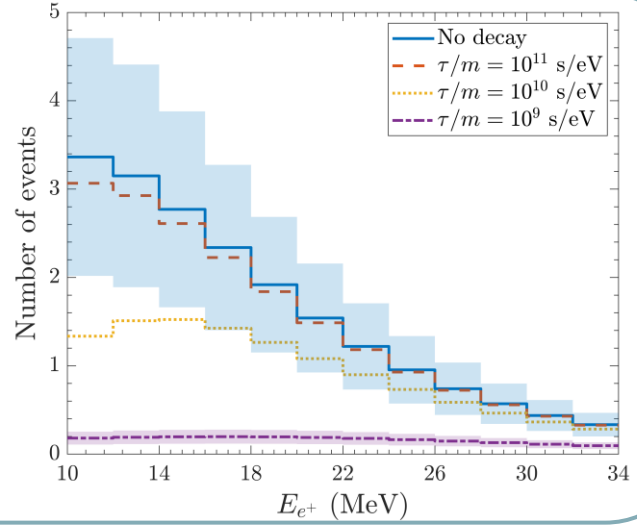
JUNO:

$N_{tot} = 17$ (no decay)

Exposure time: 20 years

Energy window:

$11.3 \leq E_\nu \leq 33.3$ MeV



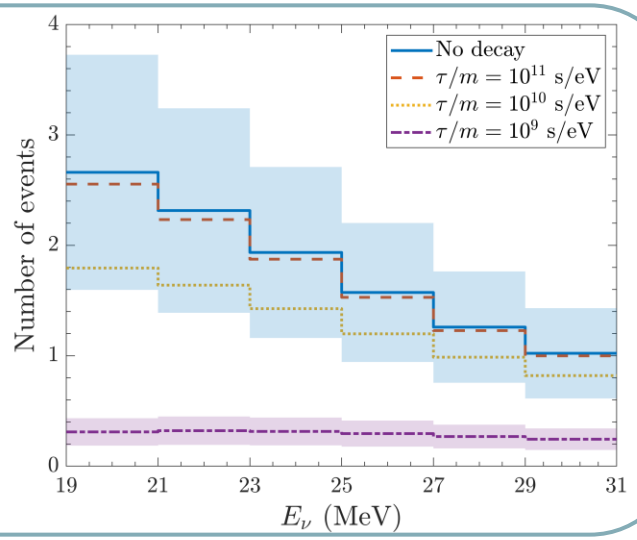
DUNE:

$N_{tot} = 11$ (no decay)

Exposure time: 20 years

Energy window:

$19 \leq E_\nu \leq 31$ MeV



Main results and conclusions

Investigation of neutrino decay and its effects on supernova neutrinos.

IN MATTER

- **Neutrino decay to Majorons** enhanced by **matter effects**
- First likelihood analysis of SN1987A data to obtain limits on couplings between neutrino- and massless Majorons
  - Competitive with limits from $0\nu\beta\beta$ decay experiments
  - Improving 4-7 orders of magnitude the limits from meson and lepton decays

IN VACUUM

- **Neutrino nonradiative decay** considering a **3ν framework** and considering both NO and IO
- Analysis of SN1987A data:
  - Normal Ordering: no sensitivity
  - Inverted ordering: $\frac{\tau}{m} \geq \mathbf{1.2 \times 10^5\ s/eV}$ at 90% CL
- Prospects for DSNB: including **dependence on the SN progenitors** and **uncertainty from the SN rate**
  - Enhancement on the ν_e and $\bar{\nu}_e$ events for the case of Normal Ordering and QD masses
  - Suppression on the ν_e and $\bar{\nu}_e$ events for the case of Inverted Ordering

P. Iváñez-Ballesteros and M.C. Volpe, PRD107 (2023) 023017, arXiv:2209.12465
P. Iváñez-Ballesteros and M.C. Volpe, PLB847 (2023) 138252, arXiv:2307.03549
P. Iváñez-Ballesteros and M.C. Volpe, arXiv:2410.11517

BACK UP SLIDES

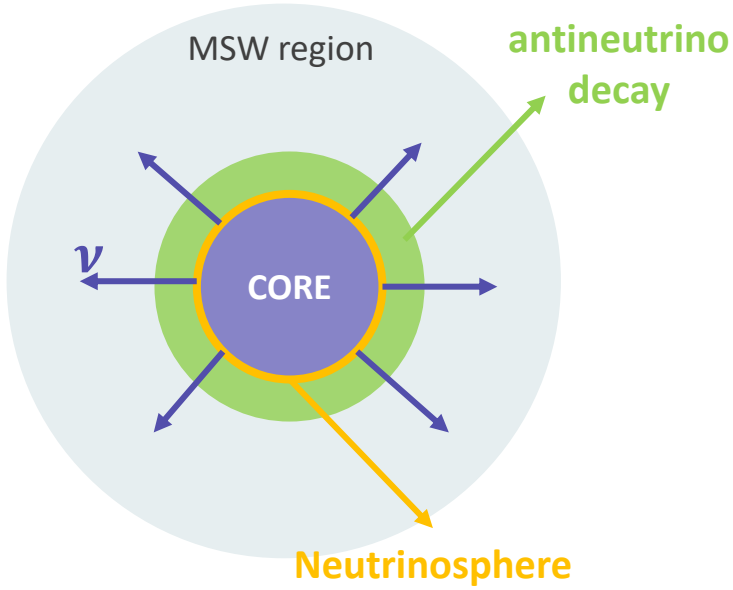
Antineutrino decay in matter: implementation

1. **Flux at the neutrinosphere:** $\phi^0_{\bar{\nu}_\alpha}(E,t)$
2. **Antineutrino decay**:
   - Decay only allowed for $\bar{\nu} \to \nu + J$ *
   - Survival probability: $N_{\bar{\nu}_\alpha}(E,t)$
3. **Flux after decay:** $\phi^d_{\bar{\nu}_\alpha}(E,t)$
   1. Supernova evolution split into 6 intervals
   2. Choose representative time-point for each interval: $\tilde{t}_i \in [t_{i-1}, t_i]$
   3. Calculate survival probability at those times: $\boldsymbol{N^i_{\bar{\nu}_\alpha}(E) = N_{\bar{\nu}_\alpha}(E, \tilde{t}_i)}$
   4. Decayed antineutrino flux at time $t \in [t_{i-1}, t_i]$ with $i = 1, \dots, 6$

$$\boldsymbol{\phi^d_{\bar{\nu}_\alpha}(E,t) = N^i_{\bar{\nu}_\alpha}(E)\phi^0_{\bar{\nu}_\alpha}(E,t)}$$

4. **Flux at the surface of the SN**:

$$\phi_{\bar{\nu}_1} = \phi^d_{\bar{\nu}_e}, \quad \phi_{\bar{\nu}_2} = \phi^d_{\bar{\nu}_{\mu'}}, \quad \phi_{\bar{\nu}_3} = \phi^d_{\bar{\nu}_{\tau'}} \ \text{(NO)}$$
$$\phi_{\bar{\nu}_1} = \phi^d_{\bar{\nu}_{\tau'}}, \quad \phi_{\bar{\nu}_2} = \phi^d_{\bar{\nu}_{\mu'}}, \quad \phi_{\bar{\nu}_3} = \phi^d_{\bar{\nu}_e} \ \text{(IO)}$$



*We used SN profiles and fluxes from the 1D simulations by the Garching group. https://wwwmpa.mpa-garching.mpg.de/ccsnarchive/archive.html These models agree well with SN1987A data. [Fiorillo *et al.* (2023)]

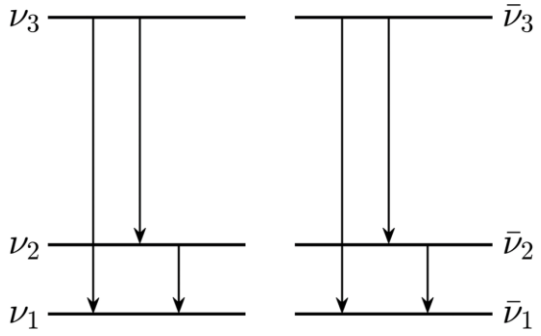
Neutrino nonradiative decay in vacuum

- Two body nonradiative decay: $\nu_j \longrightarrow \nu_i\ (\bar{\nu}_i) + X$
- Flux on Earth is obtained by solving:

$$\frac{dF_{\nu_i}}{dr}(E,r) = -\Gamma_i \frac{m}{E} F_{\nu_i}(E,r) + \sum_{m_j > m_i} \int_E^\infty dE' F_{\nu_j}(E',r) \Gamma_{\nu_j \to \nu_i} \frac{m}{E'} \psi_{\nu_j \to \nu_i}(E',E)$$

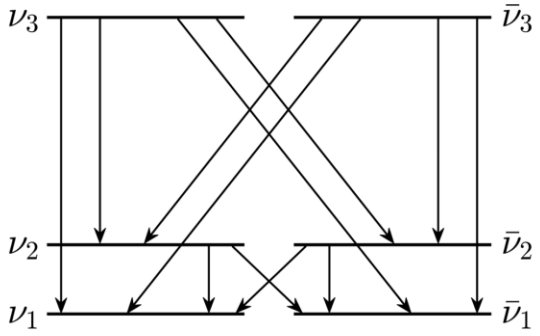
[Ando, 2004]

Normal Ordering, Quasi-Degenerate



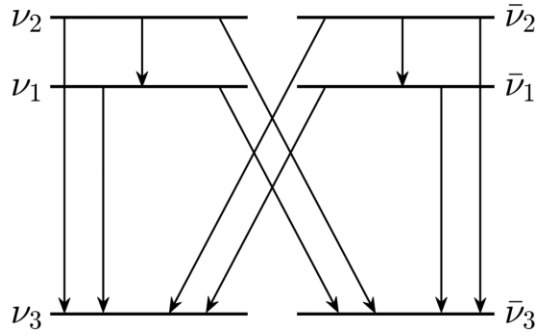
$m_1 \approx m_2 \approx m_3$

Normal Ordering, Strongly-Hierarchical



$m_1 \ll m_2 \ll m_3$

Inverted Ordering



$m_1 \approx m_2 \gg m_3$

Neutrino nonradiative decay in vacuum: QD case

[Beacom and Bell, 2002]

Neutrino nonradiative decay:

$$\boldsymbol{\nu_i \longrightarrow \nu_j\,(\bar{\nu}_j) + X}$$

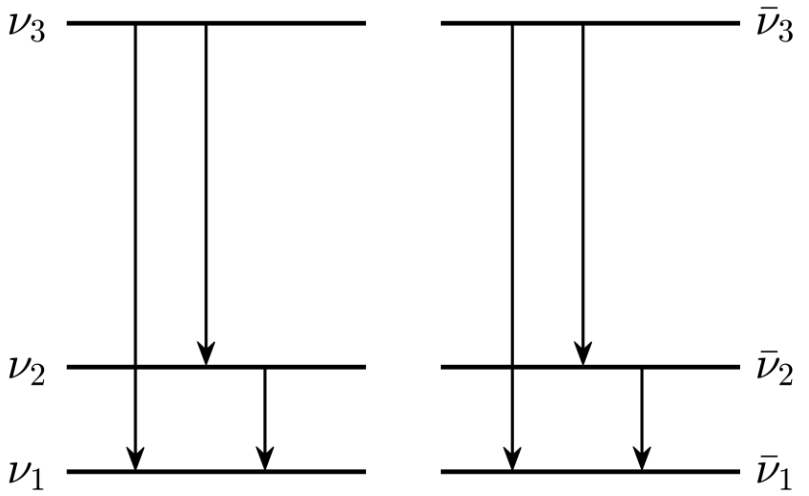
Typical lagrangian:

$$\mathcal{L} = g_{ij}\bar{\nu}_i\nu_j X + h_{ij}\bar{\nu}_i\gamma_5\nu_j X + h.c.$$

In the limit of **QD masses**, i.e. $\Delta m^2 = m_i^2 - m_j^2 \ll m_j^2 \approx m_i^2$

$$\Gamma_{\nu_i\to\nu_j} = \frac{g^2}{16\pi}\frac{\Delta m^2}{4E_i} + h^2 \times \mathcal{O}\left(\frac{\Delta m^2}{m_i^2}\right)^3$$

$$\boldsymbol{\Gamma_{\nu_i\to\bar{\nu}_j} = \frac{(g^2+h^2)}{16\pi}\frac{\Delta m^2}{E_i} \times \mathcal{O}\left(\frac{\Delta m^2}{m_i^2}\right)^3}$$



$\Longrightarrow$ helicity flipping decays are suppressed

DSNB flux in the presence of decay in vacuum

Solution to the neutrino kinetic equations in the presence of decay:

[Fogli *et al.*, 2004]

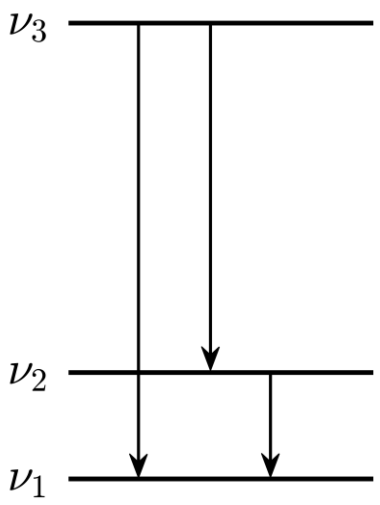
ν_i flux from core-collapses

decay of ν_j into ν_i

$$\phi_{\nu_i}(E,z) = \frac{1}{1+z}\int_z^{z_{max}} \frac{dz'}{H(z')}\left[R_{SN}(z')F_{\nu_i}\left(E\frac{1+z'}{1+z}\right) + \sum_{m_j>m_i} q_{ji}\left(E\frac{1+z'}{1+z}, z'\right)\right]$$

$$\times\, e^{-m_i\Gamma_i[\xi(z')+\xi(z)](1+z)/E}$$

ν_i decay into lighter neutrinos



$$_{ji}(E,z) = \int_E^\infty dE'\phi_{\nu_j}(E',z)\Gamma_{\nu_j\to\nu_i}\frac{m_j}{E'}\psi_{\nu_j\to\nu_i}(E',E)$$

(z) auxiliary function

$$\psi_{\nu_j\to\nu_i}(E',E) = \text{Prob}\left[\nu_j(E') \to \nu_i(E)\right]$$

Statistical analysis of SN1987A data (I)

[Vissani, 2015]
[P.I.B. and Volpe, PLB 2023]

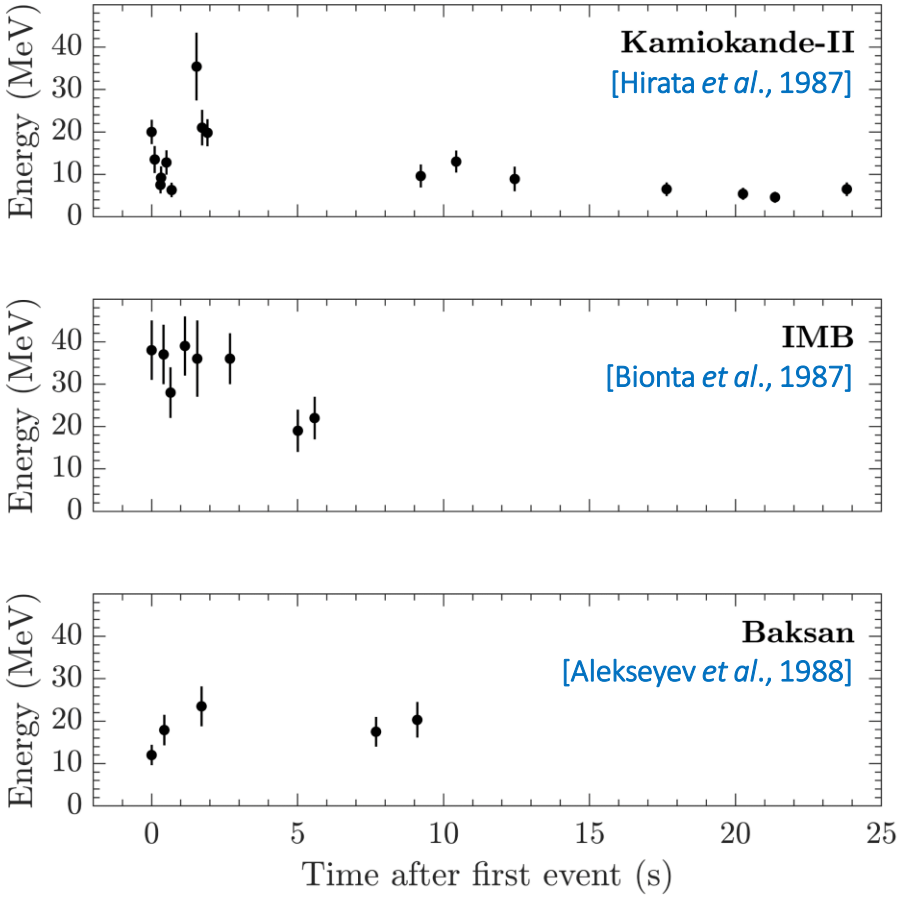
Since data available is limited, we use unbinned likelihood:

$$\mathcal{L}(x) = e^{-N_{tot}(x)} \times \prod_{i=1}^{N_{obs}} dN_i(x)$$

- N_{obs}: number of observed events
- dN_i: expected number of events around the observed energy E_i

$$dN_i = dE \left[\frac{dS}{dE_i} + \frac{dB}{dE_i} \right]$$

- N_{tot}: total number of expected events
- x: model parameters:
  - Decay in matter ⟶ g_{ii}, m_i ($i = 1$ in NO, $i = 3$ in IO)
  - Decay in vacuum ⟶ τ/m, $\overrightarrow{L_\nu}$, $\overrightarrow{\langle E_\nu \rangle}$



Statistical analysis of SN1987A data (II)

[Vissani, 2015]
[P.I.B. and Volpe, PLB 2023]

Main detection channel Inverse Beta Decay:

$$\bar{\nu}_e + p \rightarrow n + e^+$$

- True positron spectrum:

$$\frac{dS_e}{dE_e} \approx N_p F_{\bar{\nu}_e}(E_\nu)\sigma_{IBD}(E_\nu)J(E_\nu)$$

$$J(E_\nu) = \frac{\left(1 + {E_\nu}/{m_p}\right)^2}{1 + {\Delta_{np}}/{m_p}}, \left(\Delta_{np} = m_n - m_p = 1.293\ \text{MeV}\right)$$

- Observed positron spectrum:

$$\frac{dS}{dE_i} = \int_0^\infty \eta(E_e) G\left(E_e - E_i, \sigma(E_e)\right) \frac{dS_e}{dE_e}\, dE_e$$

  - $\eta(E_e)$: intrinsic efficiency function (depends on the detector)
  - $G\left(E_e - E_i, \sigma(E_e)\right)$: smearing function (assumed to be Gaussian)
  - $\sigma(E_e) = \sigma_{stat} \times \left(\frac{E_e}{10\ \text{MeV}}\right)^{1/2} + \sigma_{syst} \times \left(\frac{E_e}{10\ \text{MeV}}\right)$

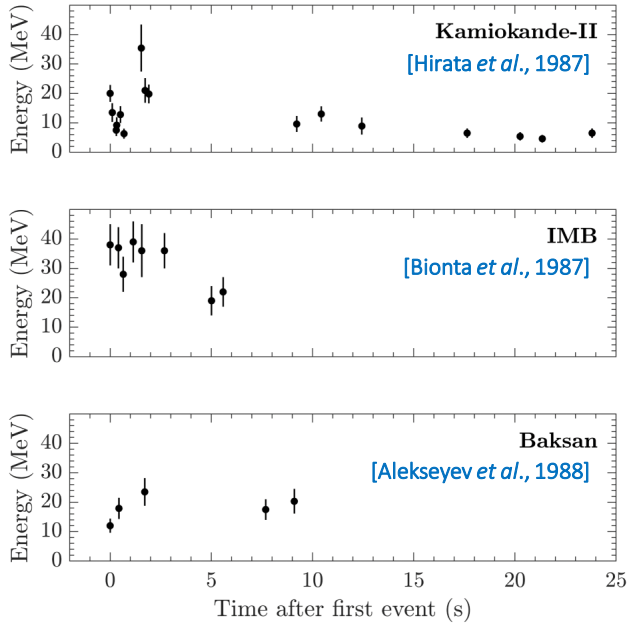


Table 1
Properties of the experiments (first column) that detected the neutrinos from SN1987A. The table shows the number of target protons (second column) and the two coefficients defining the uncertainty function $\sigma(E_e)$ (third and fourth columns). The last column gives the total background B_{tot} (see text). (From [52].)

	N_p	σ_{stat} [MeV]	σ_{syst} [MeV]	B_{tot}
Kamiokande-II	1.4×10^{32}	1.27	1.0	0.55
IMB	4.6×10^{32}	3.0	0.4	0.01
Baksan	0.2×10^{32}	0.0	2.0	1.0

DSNB number of events

$$N_\alpha = \epsilon\, N_t \int \mathrm{d}E_\nu \phi_{\nu_\alpha}(E_\nu)\sigma(E_\nu)$$

Properties of the experiments considered and total number of events in the absence of decay in NO (IO).

	N_t (10^{33})	ϵ (%)	Time (years)	DSNB window (MeV)	DSNB events
SK-Gd	1.5	57.5	2	(12.8, 30.8)	2 (2) $\bar{\nu}_e$
SK-Gd	1.5	73.75	8	(12.8, 30.8)	12 (10) $\bar{\nu}_e$
HK	12.5	25	20	(17.3, 31.3)	48 (40) $\bar{\nu}_e$
HK-Gd	12.5	40	20	(17.3, 31.3)	76 (64) $\bar{\nu}_e$
JUNO	1.21	50	20	(11.3, 33.3)	20 (17) $\bar{\nu}_e$
DUNE	0.602	86	20	(19,31)	12 (11) ν_e

Number of events associated with inverse-beta decay in SK-Gd, HK and JUNO as well as with ν_e $-^{40}$ Ar scattering in DUNE. The predicted number of events are given in the third to fifth columns for the different τ/m considered. The values are given for NO, QD; for NO, SH (in brackets) and for IO (in parenthesis).

	Number of events			
Experiment	No decay	$(\tau/m)_{\text{long}}$	$(\tau/m)_{\text{medium}}$	$(\tau/m)_{\text{short}}$
SK-Gd	2	2	3	4
(12.8–30.8)	(2)	[2]	[2]	[2]
2 + 8 years		(2)	(1)	(0)
	12	13	17	22
	(10)	[12]	[12]	[11]
		(10)	(7)	(1)
HK	48	49	61	84
(17.3–31.3)	(40)	[47]	[45]	[43]
20 years		(39)	(29)	(6)
HK-Gd	76	79	98	135
(17.3–31.3)	(64)	[73]	[73]	[69]
20 years		(62)	(46)	(9)
JUNO	20	21	28	37
(11.3–33.3)	(17)	[20]	[19]	[19]
20 years		(16)	(10)	(2)
DUNE	12	12	15	20
(19–31)	(11)	[11]	[11]	[10]
20 years		(10)	(8)	(2)