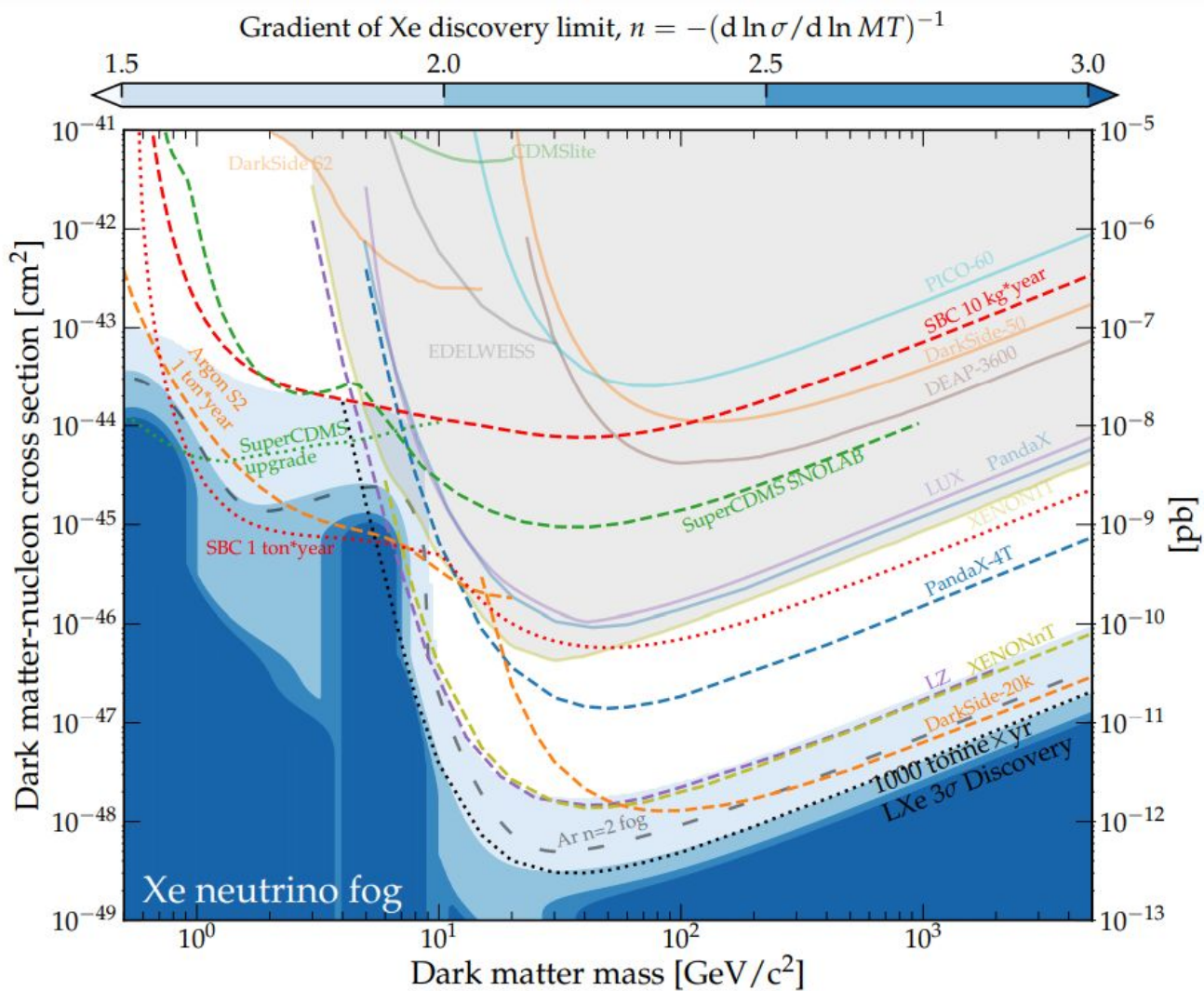


A BAYESIAN ANALYSIS WITH MACHINE LEARNING IN DM DIRECT DETECTION



Martín de los Ríos*, Andres Perez & David Cerdeño



OUTLINE

ML analysis
to obtain
posteriors

DM-nucleon
interaction
with NR-EFT

DM
differential
rate for a DD
experiment

Simulate the
expected
signal

Parameter space that
can be reconstructed

MACHINE LEARNING

BAYESIAN ANALYSIS

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$$P(\theta | x) = P(x | \theta) P(\theta) / P(x)$$

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Posterior
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$$P(\theta | x) = P(x | \theta) \frac{P(\theta)}{P(x)}$$

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Prior
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BAYESIAN ANALYSIS

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Posterior probability of the parameters θ of interest given the data x .

Probability of the data x given the parameters θ .

Prior probability of the parameters θ .

Probability of the data x also call evidence.

BAYESIAN ANALYSIS WITH SWYFT

MARGINAL NEURAL
RATIO ESTIMATION

<https://swyft.readthedocs.io/>
<https://arxiv.org/abs/2107.01214>

$$r(\theta, x) = P(\theta | x) / P(\theta) = P(x | \theta) / P(x) = P(x, \theta) / P(\theta)P(x)$$

BAYESIAN ANALYSIS WITH SWYFT

$$r(\theta, x) = P(\theta, x) / P(\theta)P(x)$$

CLASS = 1

(θ_2, x_2) (θ_4, x_4)
 (θ_3, x_3) (θ_1, x_1) (θ_5, x_5)
 (θ_7, x_7) (θ_6, x_6)

CLASS = 0

(θ_6, x_2) (θ_2, x_4)
 (θ_3, x_5) (θ_7, x_1) (θ_3, x_5)
 (θ_1, x_7) (θ_6, x_4)


BAYESIAN ANALYSIS WITH SWYFT

$$r(\theta, x) = P(\theta, x) / P(\theta)P(x)$$

CLASS = 1


(cat, )


(dog, )

(house, )

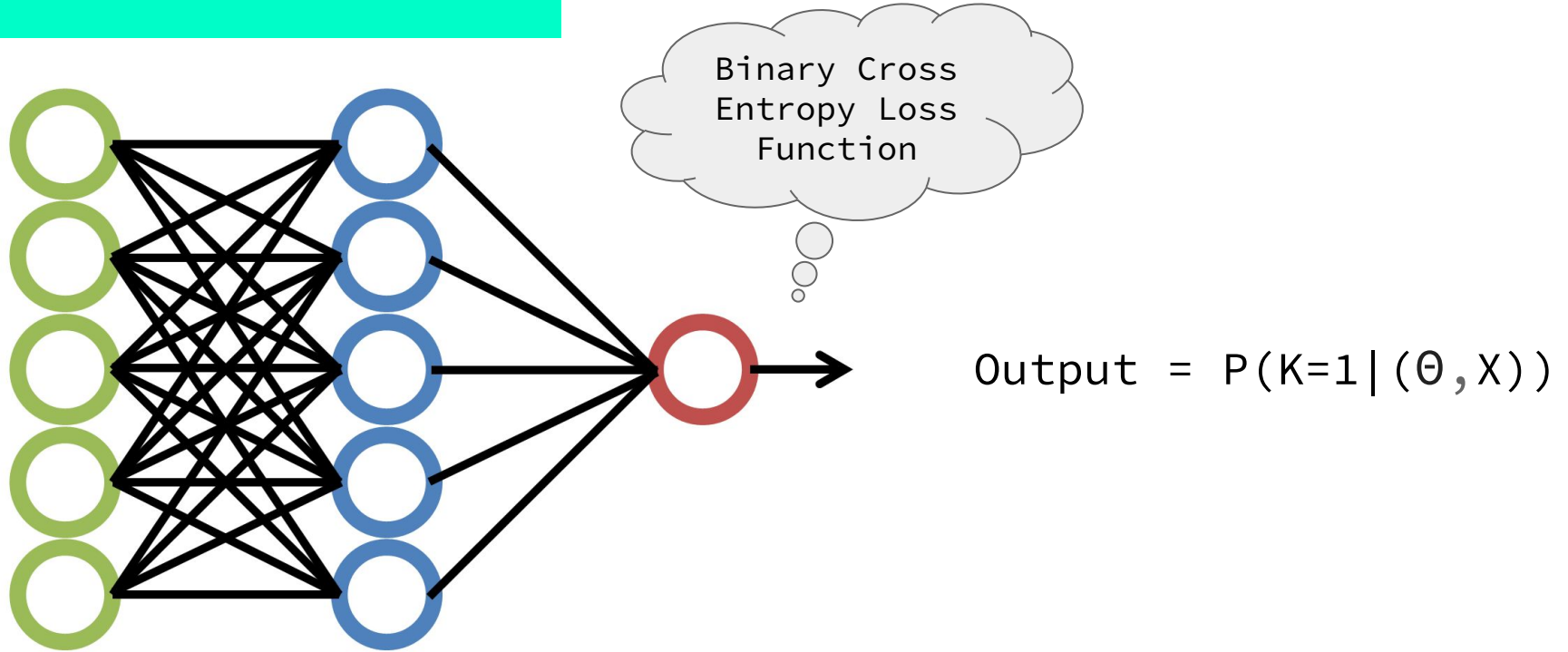
CLASS = 0

(dog, )

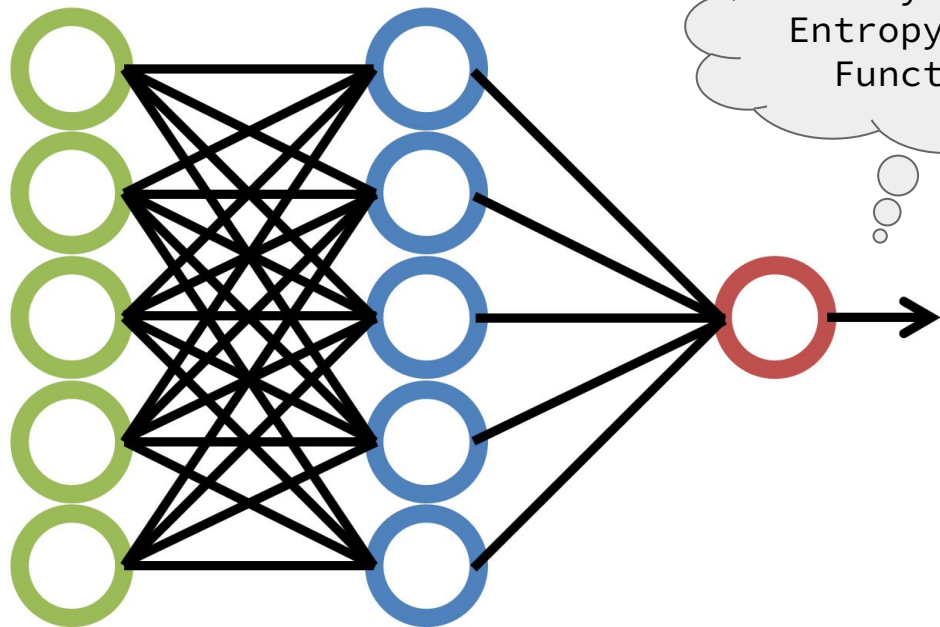
(dog, ) (cat, )

(house, )

BINARY CLASSIFICATION



BINARY CLASSIFICATION

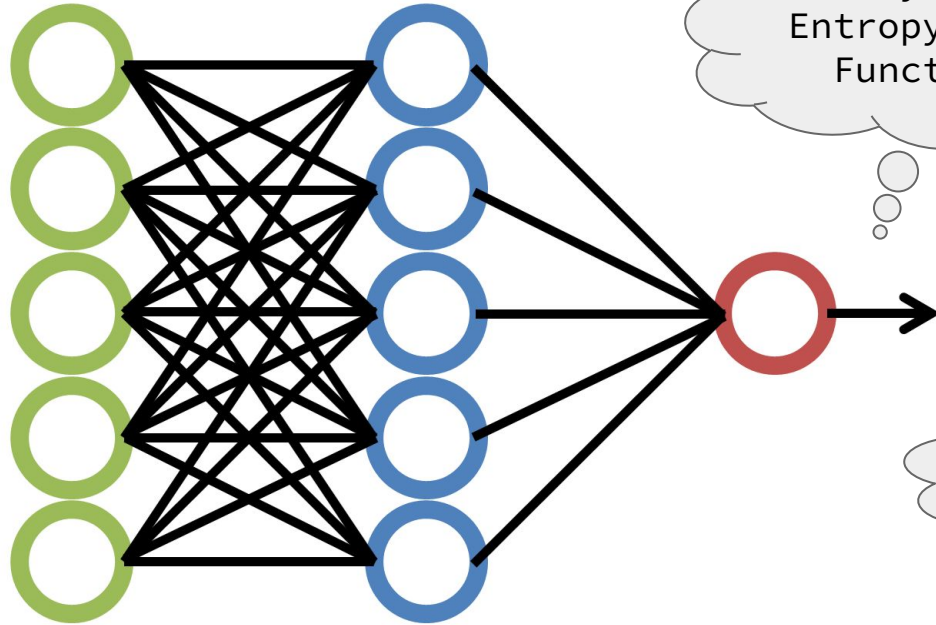


Binary Cross
Entropy Loss
Function

$$P(k=0 | (\theta, x)) = 1 - P(k=1 | (\theta, x))$$
$$\text{Class } 0 \Rightarrow P(x)P(\theta)$$

$$\text{Output} = P(k=1 | (\theta, x))$$

BINARY CLASSIFICATION



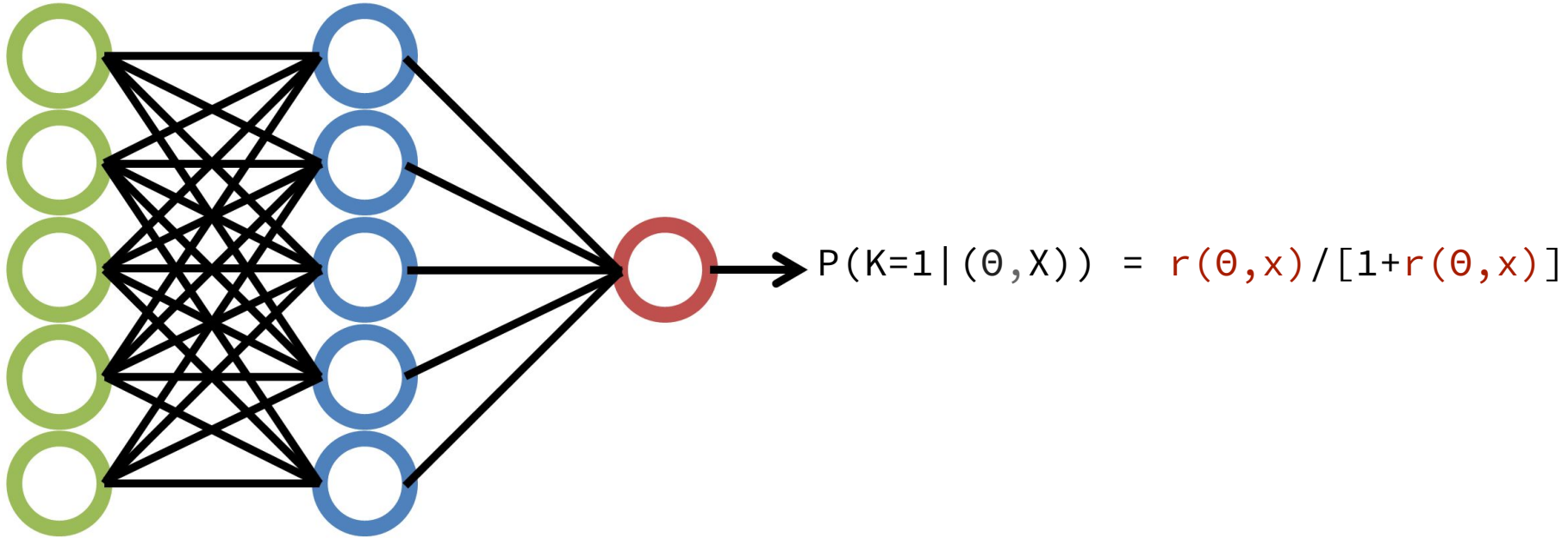
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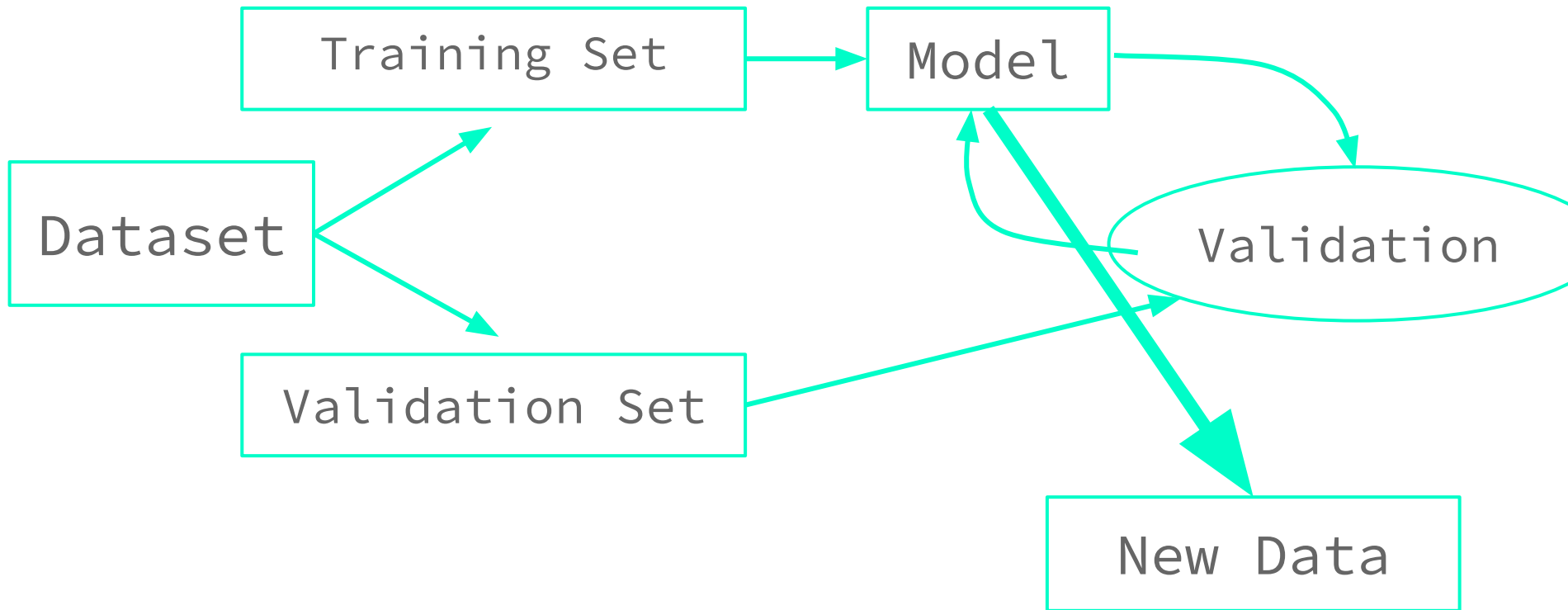
$$\text{Output} = P(k=1 | (\theta, x))$$

$$\text{Class } 1 \Rightarrow P(x, \theta)$$

BINARY CLASSIFICATION



Supervised Learning



So...

- 1) We measure some data x
- 2) We sample model parameters θ from prior $P(\theta)$
- 3) We feed the neural network with pairs (x, θ) , and the network gives back de $r(\theta, x)$
- 4) We multiply $r(\theta, x)$ by $P(\theta)$ and obtain $P(\theta | x)$

- In our case the parameters of interest will be the EFT parameters and the DM mass.
- In our case, the data x will be the signal measured by XENONnT, this can be:
 - The total number of events.
 - The differential rate.
 - The full s_1 - s_2 plane.
 - We also add all the relevant backgrounds, including $C_{\nu\nu}$ s

DATA SAMPLE GENERATION

DM-NUCLEON NON-RELATIVISTIC EFFECTIVE FIELD THEORY (NR-EFT)

For DM particles with spin up to $\frac{1}{2}$, the effective DM-nucleon scattering interaction Lagrangian

$$\mathcal{L}_{\text{EFT}} = \sum_{\tau} \sum_i c_i^{\tau} \mathcal{O}_i \bar{\chi} \chi \bar{\tau} \tau$$

nucleon basis:

$$c^p: \text{proton} \quad c_i^0 = \frac{1}{2} (c_i^p + c_i^n)$$

$$c^n: \text{neutron} \quad c_i^1 = \frac{1}{2} (c_i^p - c_i^n)$$

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$i=14$
possible
interactions

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$i=14$
possible
interactions

nucleon basis:

c^p : proton

c^n : neutron

$$c_i^0 = \frac{1}{2} (c_i^p + c_i^n)$$

$$c_i^1 = \frac{1}{2} (c_i^p - c_i^n)$$

01:
spin-independent
04:
spin-dependent

DM-NUCLEON NON-RELATIVISTIC EFFECTIVE FIELD THEORY (NR-EFT)

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$$\mathcal{L}_{\text{EFT}} = \sum_{\tau} \sum_i c_i^{\tau} \mathcal{O}_i \bar{\chi} \chi \bar{\tau} \tau$$

Change to polar coordinates:

$$c_i^0 = \frac{1}{2} (c_i^p + c_i^n) = A_i \sin(\theta_i)$$

$$c_i^1 = \frac{1}{2} (c_i^p - c_i^n) = A_i \cos(\theta_i)$$

Natural choice for the EFT parameter space because the interaction cross section:

$$\sigma_i \propto A_i^2$$

For SI (O1) $\sigma_{\chi\mathcal{N}}^{\text{SI}} = \frac{A_1^2 \mu_{\chi\mathcal{N}}^2}{\pi}$ → DM-nucleon reduced mass

DM-NUCLEON NON-RELATIVISTIC EFFECTIVE FIELD THEORY (NR-EFT)

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For each operator **2 parameters**:

- amplitude (cross-section)
- phase

+ DM mass

$(\sigma_i, \theta_i, m_{\text{DM}})$

DM DIFFERENTIAL RATE

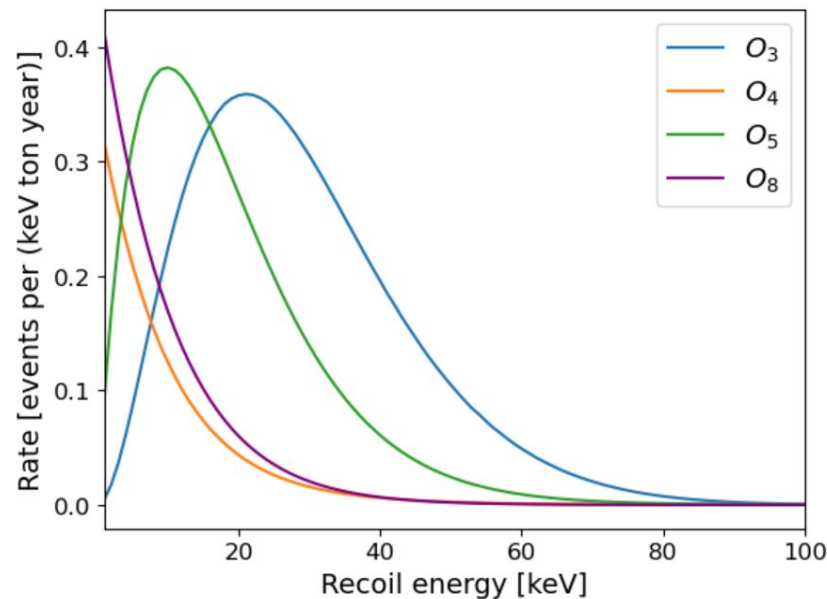
<https://wimpydd.hepforge.org/>
<https://arxiv.org/abs/2106.06207>

From NR-EFT operators to differential rate with WimPyDD

Inputs:

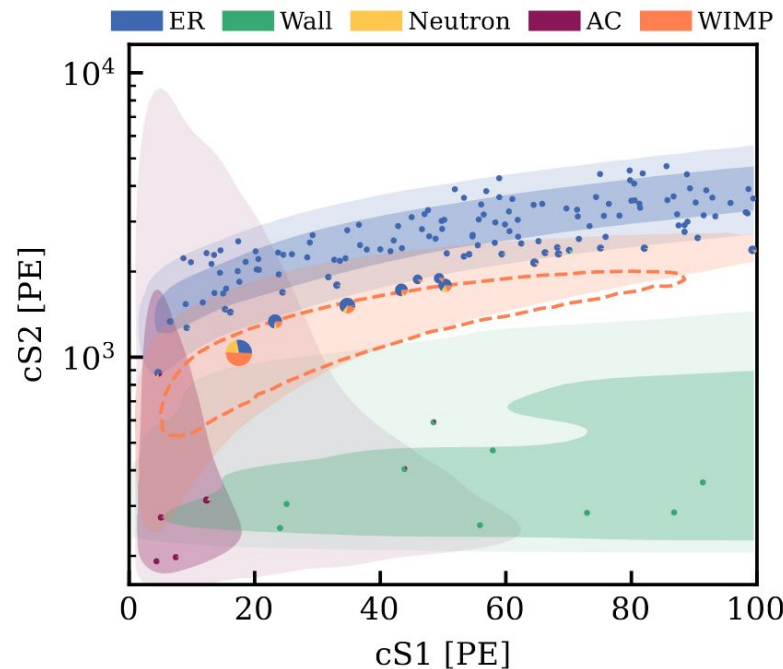
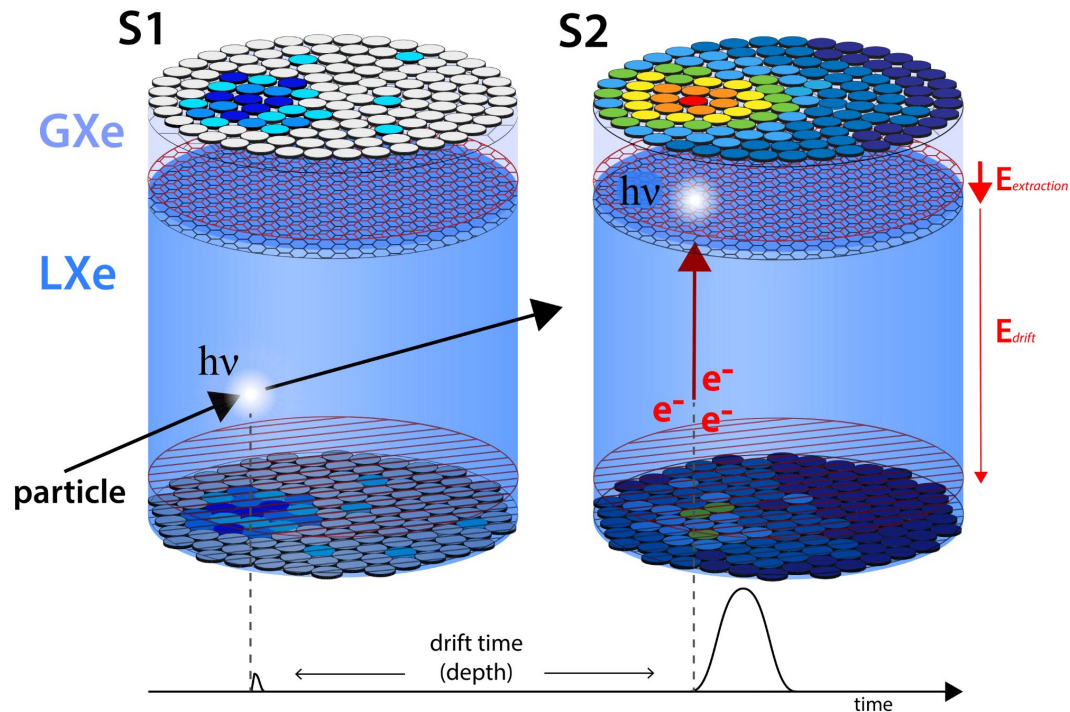
- Operator
- Parameters:
 - amplitude (cross-section)
 - phase
 - DM mass
- DM halo model
- DD experiment (XENONnT)

Output:



DM SIGNAL

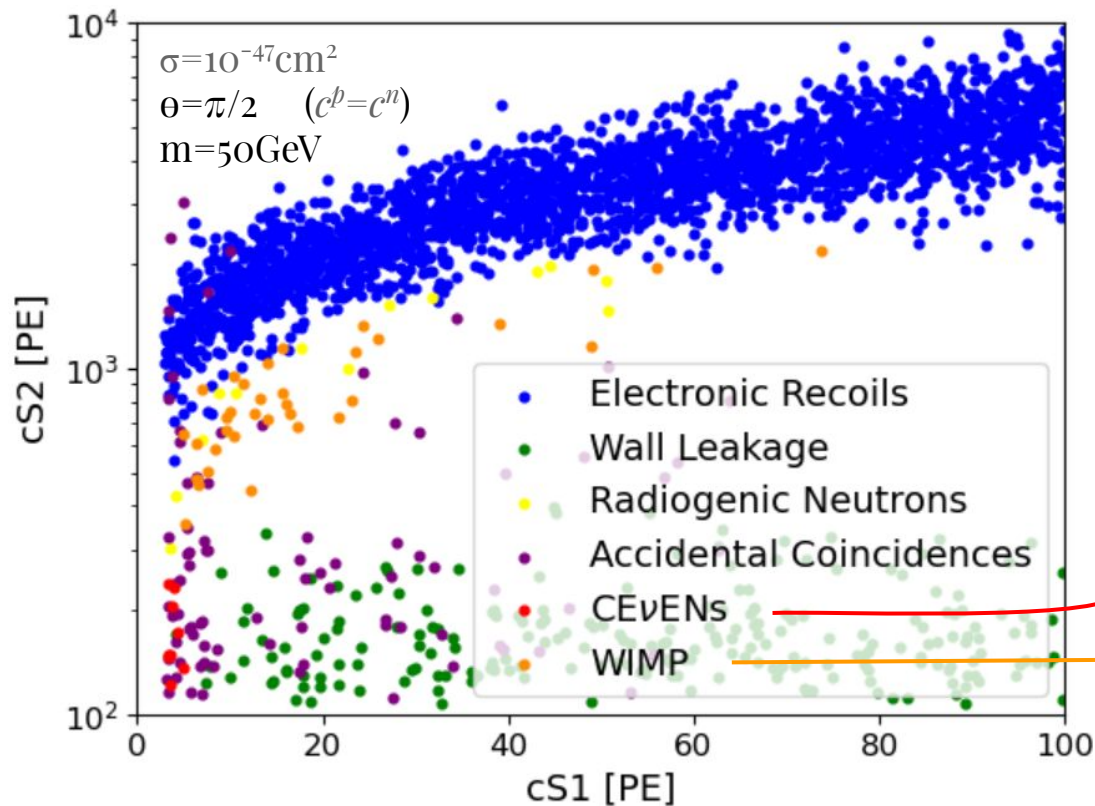
XENONnT



DM SIGNAL

XENONnT 20ty

NR-EFT: O₁



XENONnT simulator

We specify background and signal characteristics

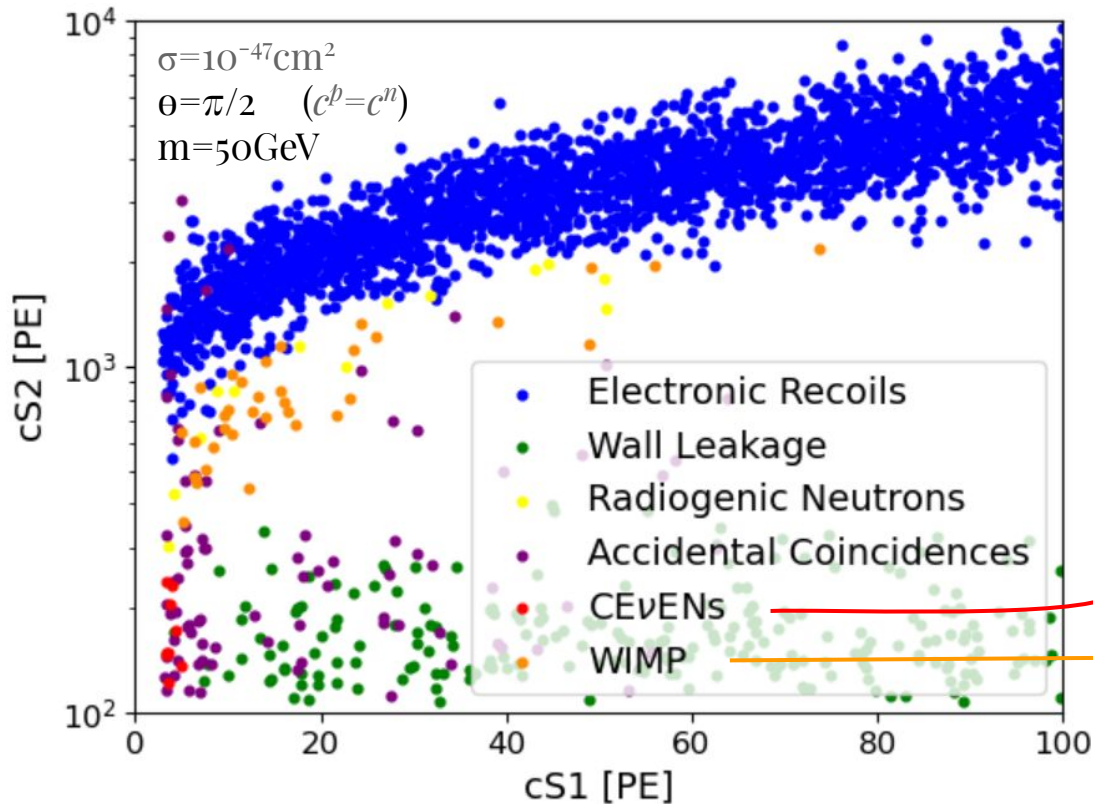
differential rate compute with Snudd

differential rate compute with WimPyDD for a particular operator, amplitude, phase and DM_{28} mass.

DM SIGNAL

XENONnT 20ty

NR-EFT: O₁



XENONnT simulator

We specify background and signal channels

<https://github.com/SNuDD/SNuDD>
<https://arxiv.org/abs/2302.12846>

differential rate compute with SNuDD

differential rate compute with WimPyDD for a particular operator, amplitude, phase and DM₂₉ mass.

DATA REPRESENTATION: S1 vs S2 plane

XENONnT 20ty

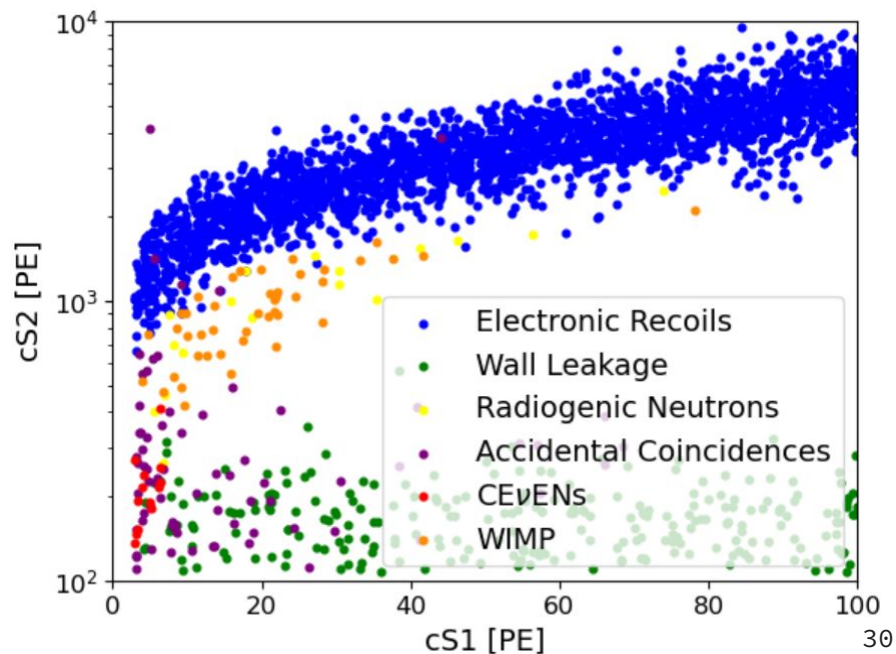
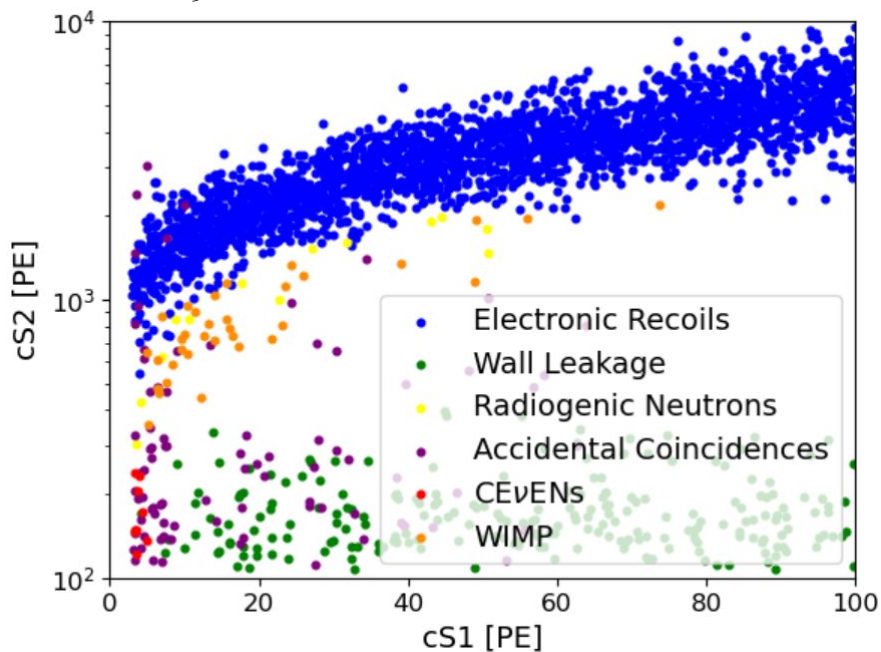
NR-EFT: O1

$$\sigma = 10^{-47} \text{cm}^2$$

$$\theta = \pi/2 \quad (c^b = c^n)$$

$$m = 50 \text{GeV}$$

We generate a 10k pseudo experiments per operator varying σ , θ , and m_{DM}



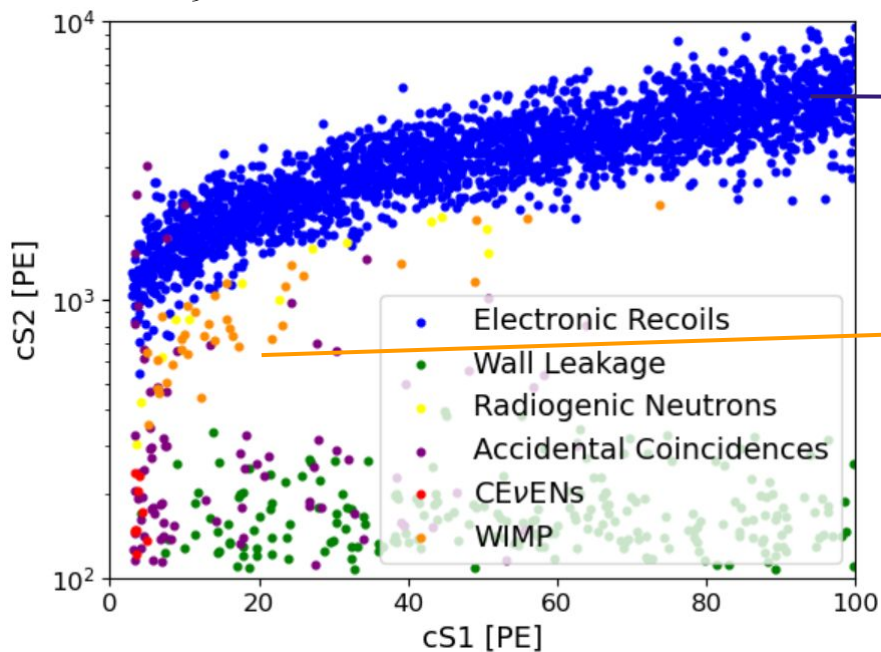
DATA REPRESENTATION: number of events

NR-EFT: O₁

$$\sigma = 10^{-47} \text{cm}^2$$

$$\theta = \pi/2 \quad (c^b = c^n)$$

$$m = 50 \text{GeV}$$



	name	pseudo_exp_events
0	er	2459
1	radiogenics	17
2	ac	71
3	wall	246
4	WIMP	43
5	CEVNS-SM	13

DATA REPRESENTATION:

differential rate

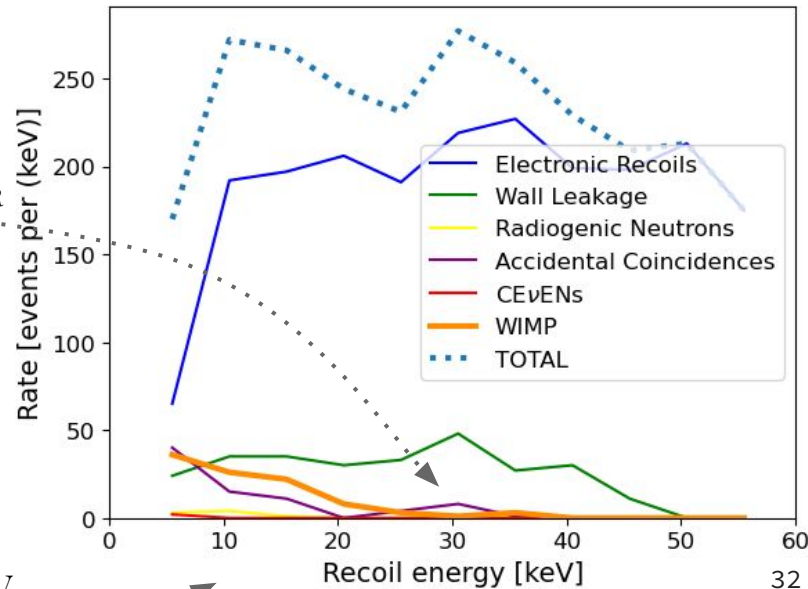
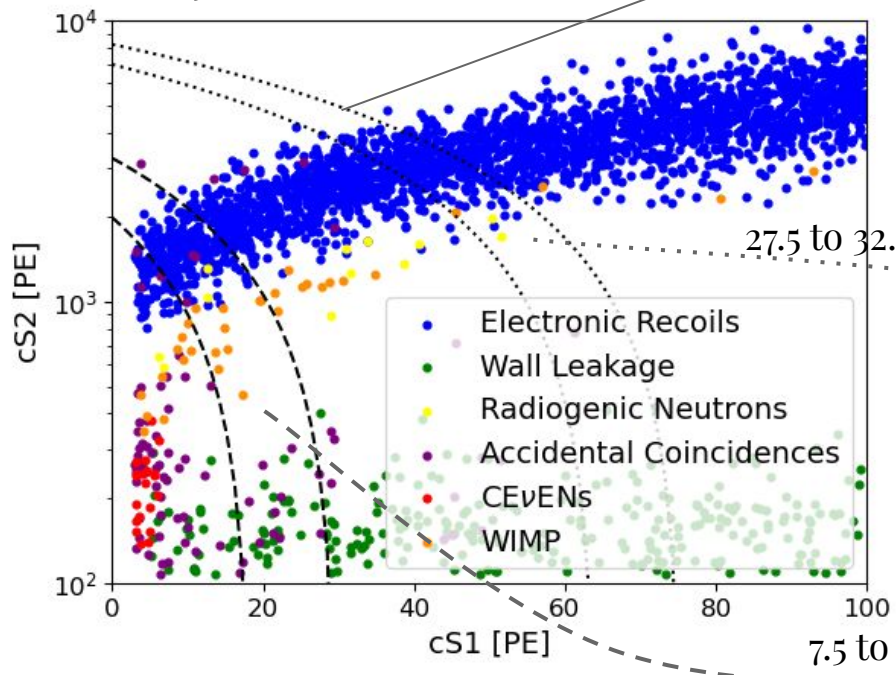
NR-EFT: O₁

$$\sigma = 10^{-47} \text{cm}^2$$

$$\theta = \pi/2 \quad (c^b = c^n)$$

$$m = 50 \text{GeV}$$

Nuclear Recoil
isoenergy
curves



RESULTS

RESULTS

Data:

S1 vs S2 plane

differential rate

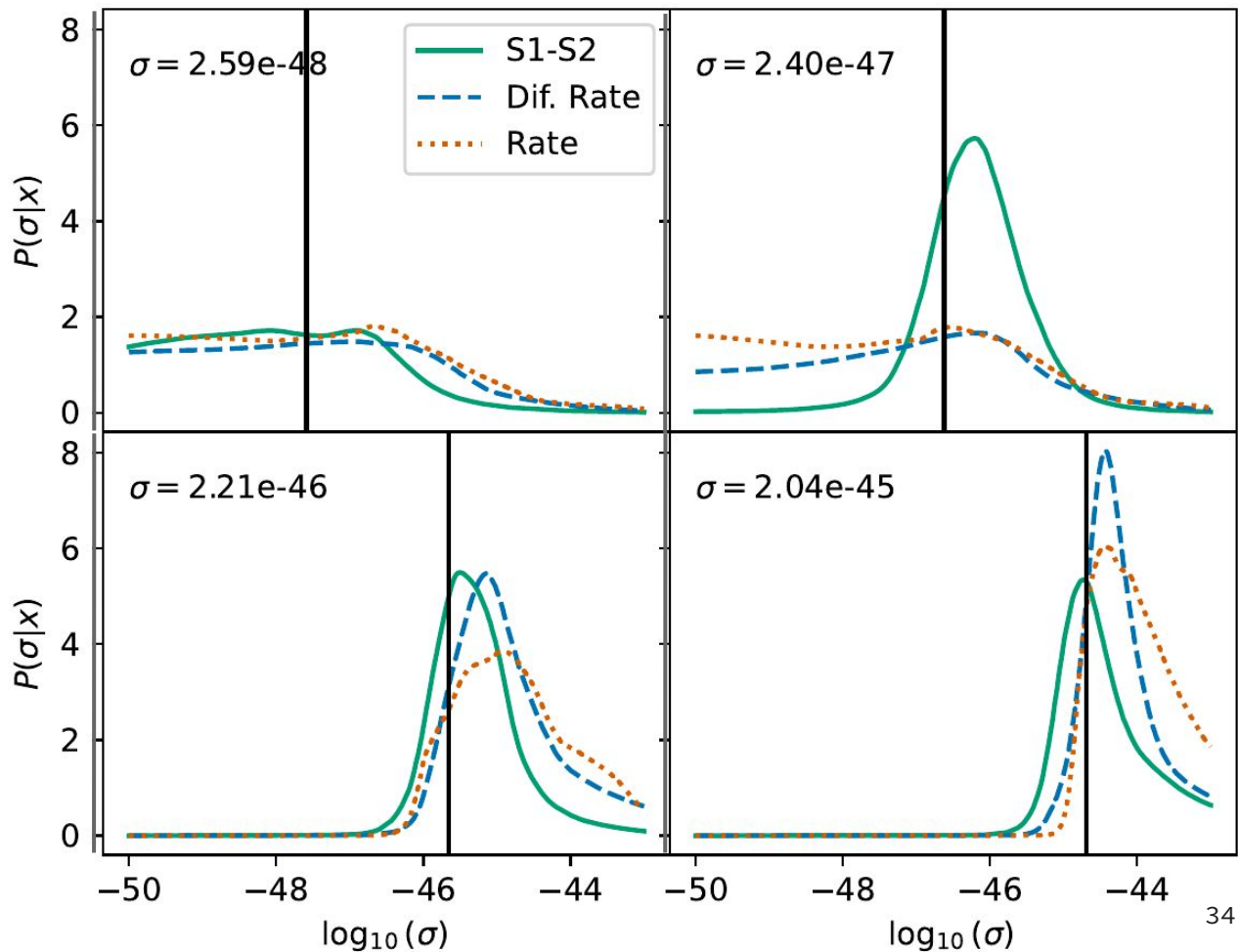
total number of events

examples with

O1 (SI)

$m_{\text{DM}} \approx 100\text{GeV} \rightarrow \text{fixed}$

$\theta = \pi/2 \rightarrow \text{fixed}$



RESULTS

Data:

S1 vs S2 plane

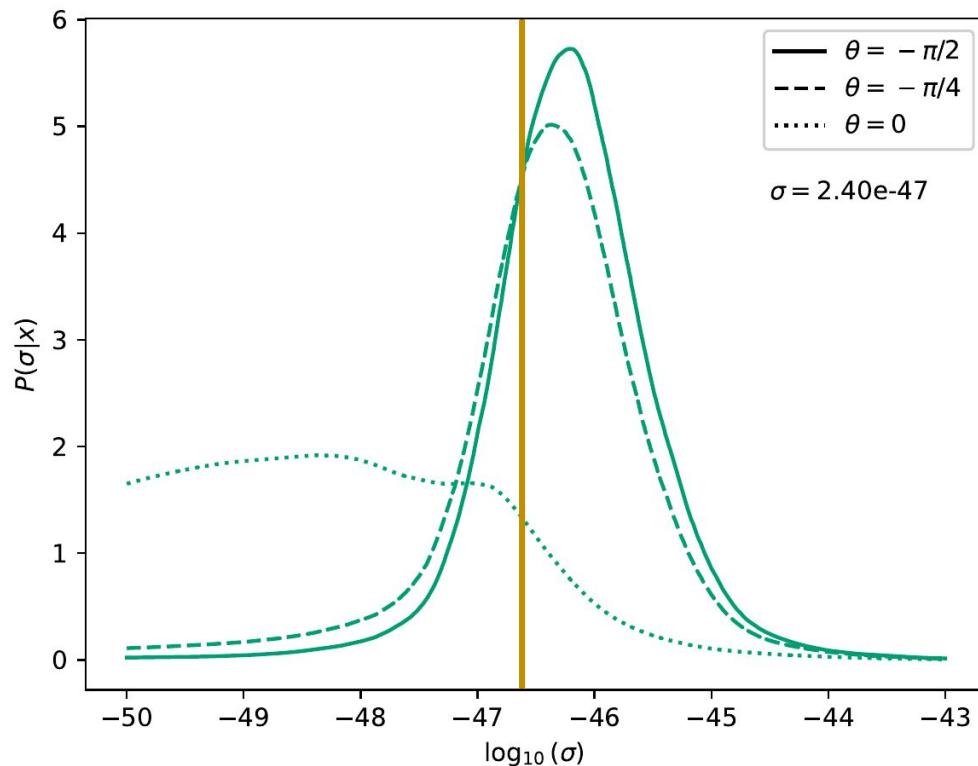
These are all the posteriors for

O_1 (SI)

$m_{\text{DM}} \simeq 100 \text{ GeV} \rightarrow \text{fixed}$

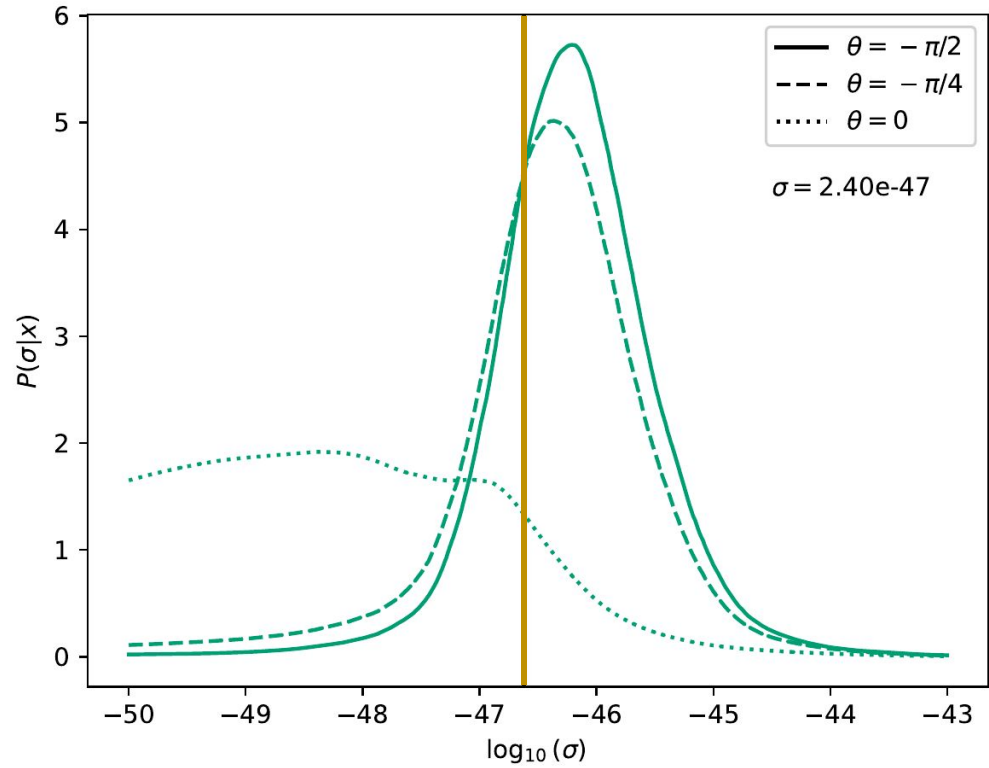
$\sigma = 2.4 \cdot 10^{-47} \text{ cm}^2 \rightarrow \text{fixed}$

S1 vs S2



RESULTS

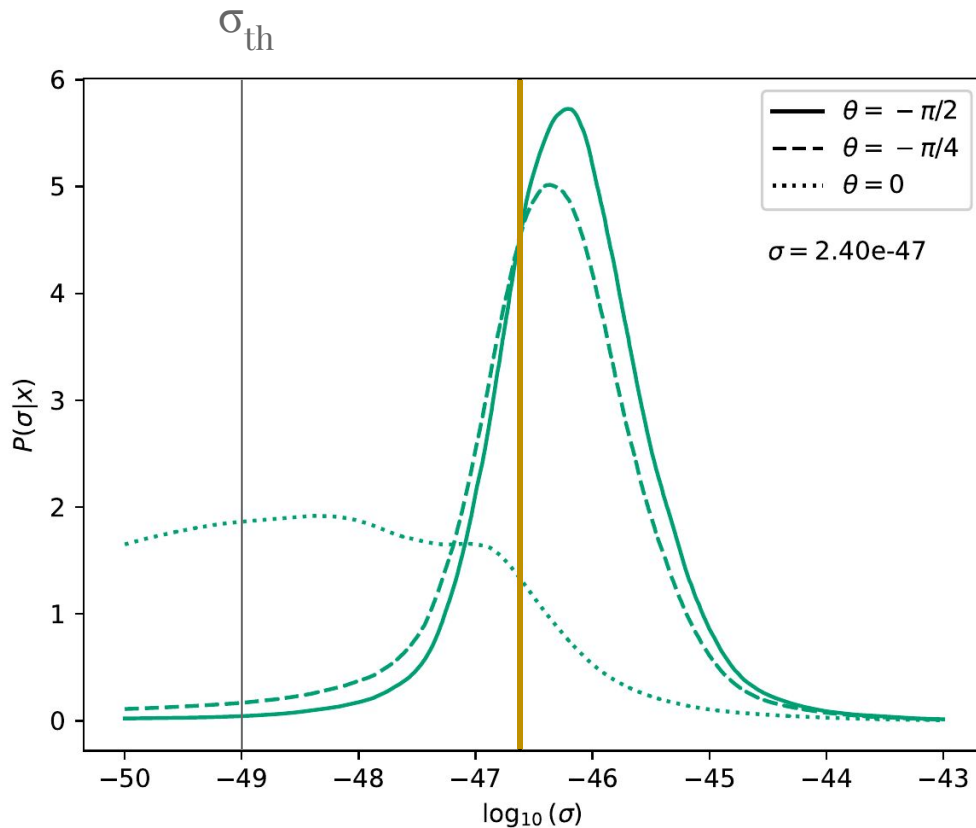
S1 vs S2



RESULTS

threshold:
 $\sigma_{\text{th}} = 10^{-49} \text{cm}^2$

S1 vs S2

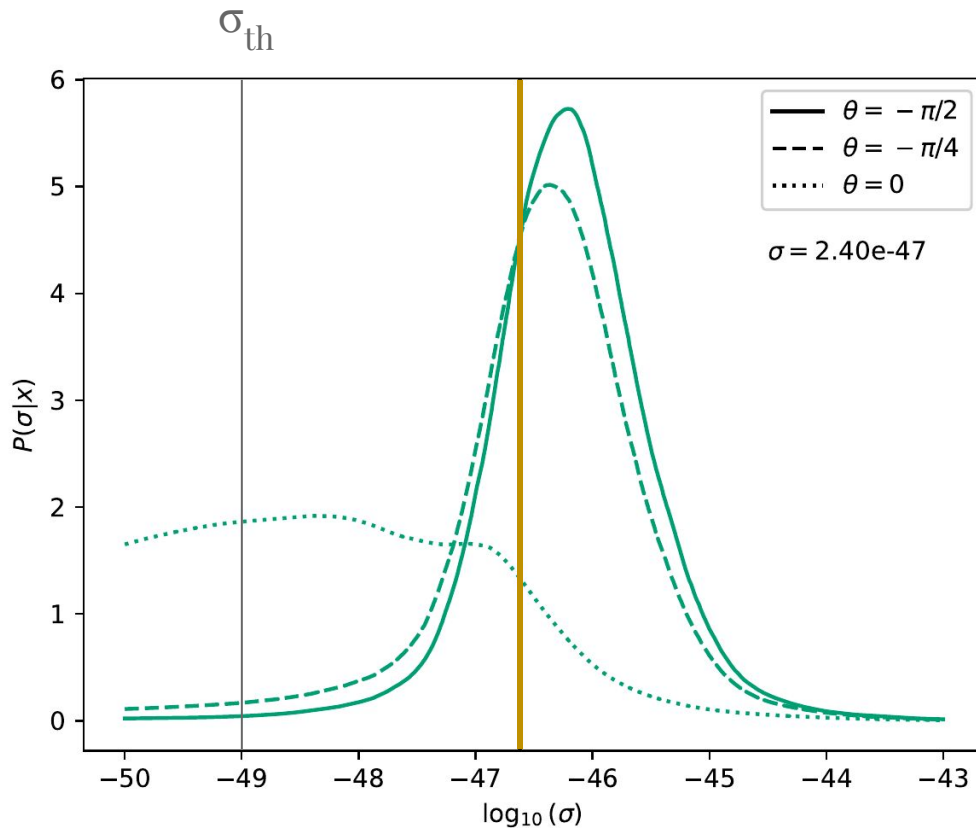


RESULTS

S1 vs S2

threshold:
 $\sigma_{th} = 10^{-49} \text{cm}^2$

$$\int_{\sigma_{th}}^{\infty} P(\sigma|x)$$

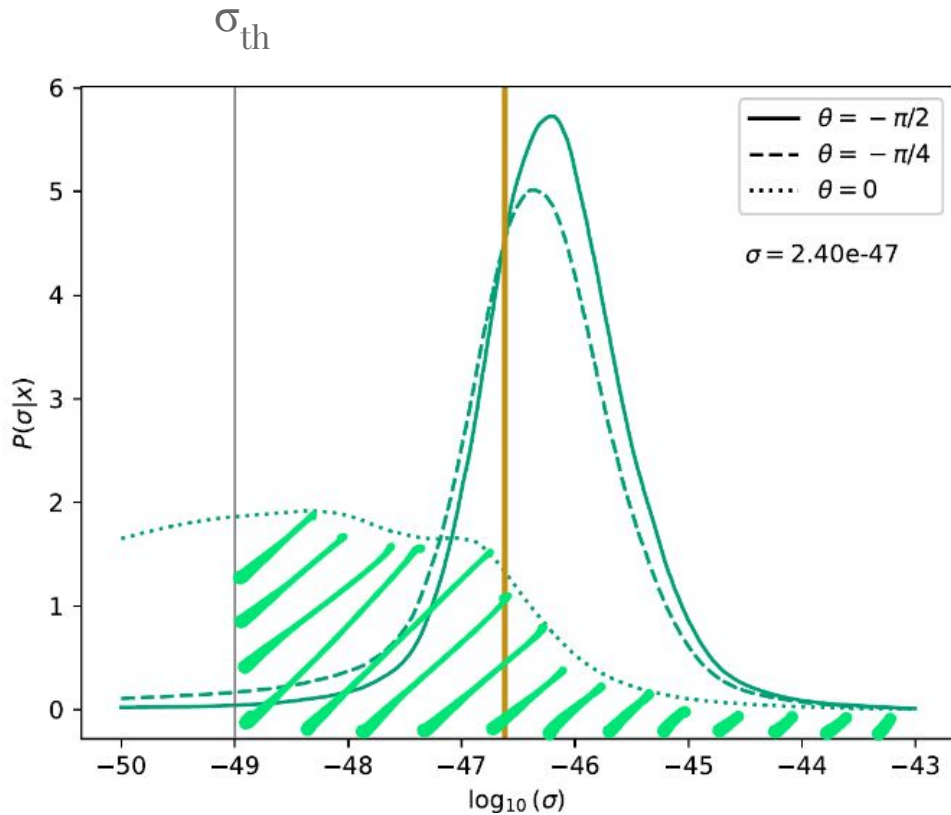


RESULTS

S1 vs S2

threshold:
 $\sigma_{th} = 10^{-49} \text{cm}^2$

$$\int_{\sigma_{th}}^{\text{inf}} P(\sigma|x) < 0.90$$

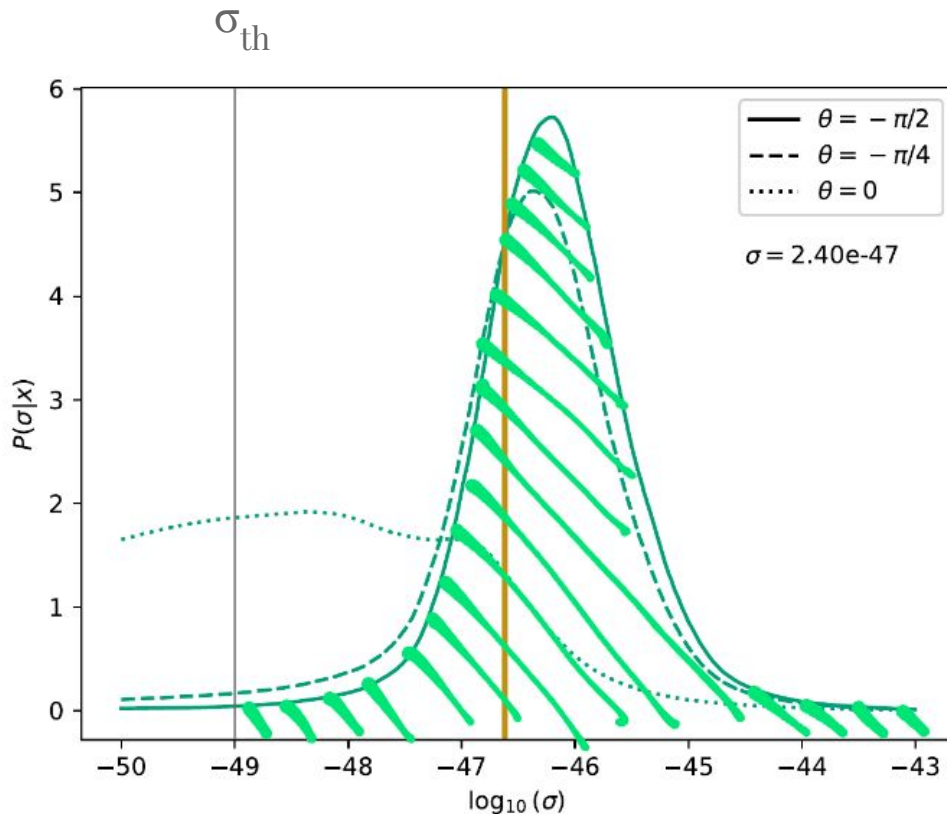


RESULTS

S1 vs S2

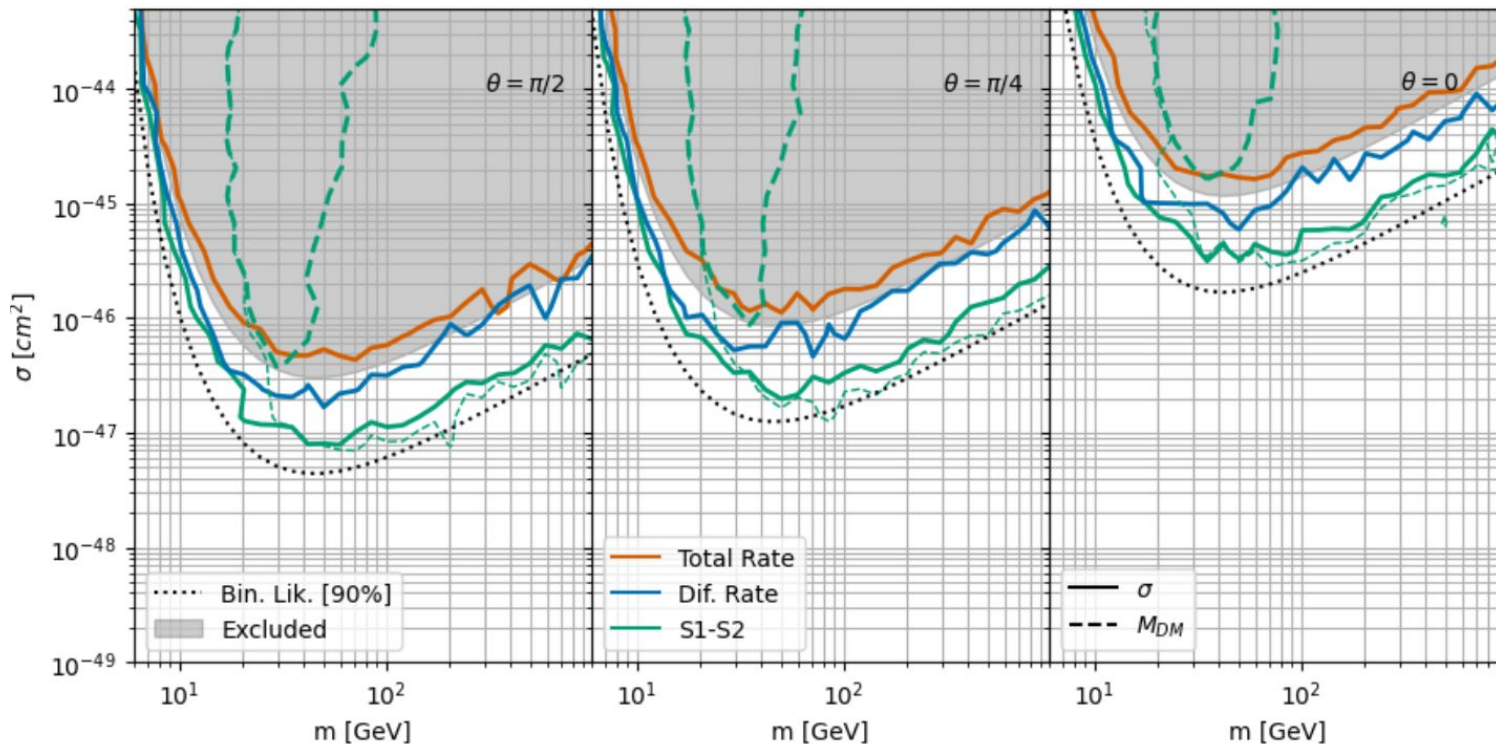
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 $\sigma_{th} = 10^{-49} \text{cm}^2$

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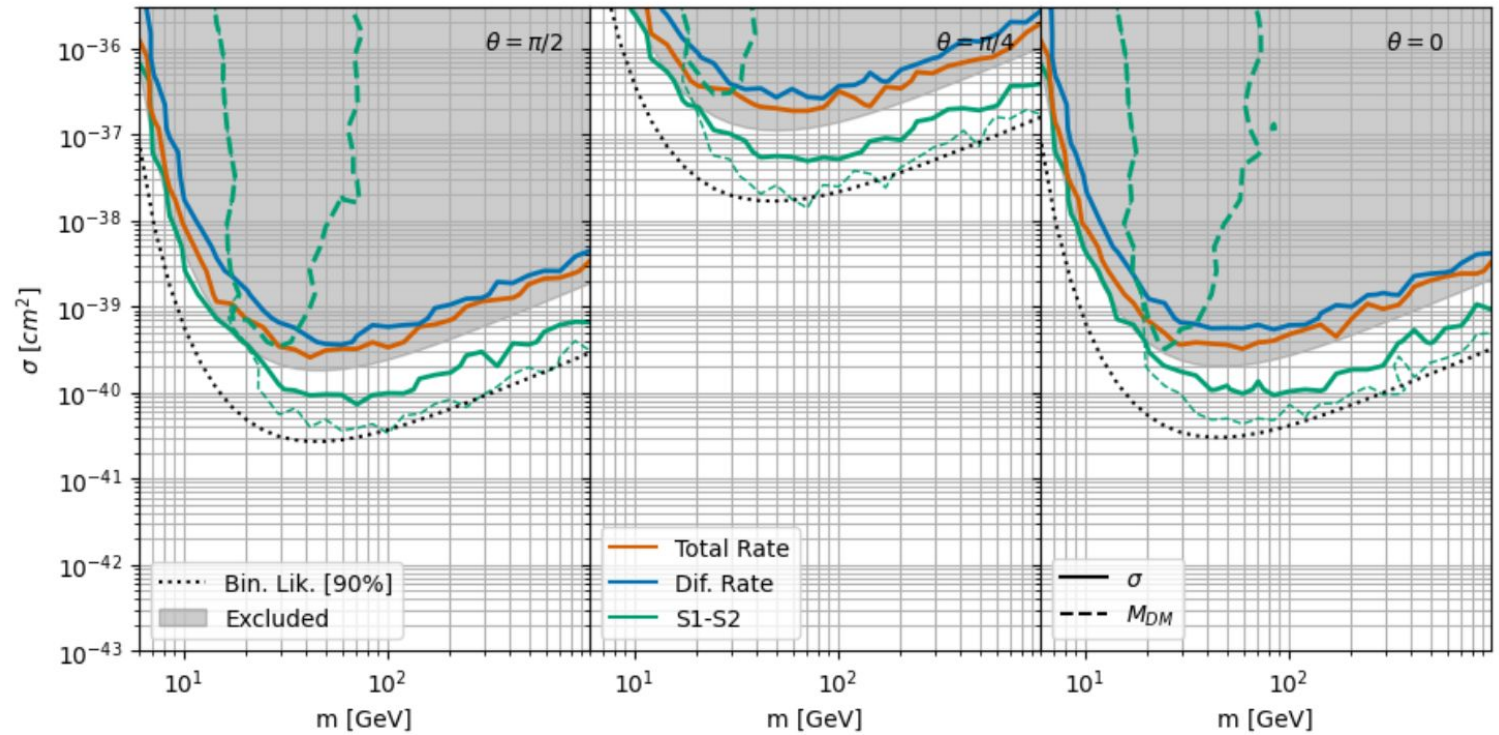
RESULTS: σ DETECTION PLOT

XENONnT 20ty
01 operator



Data: total number of events
differential rate
S1 vs S2 plane

RESULTS: σ DETECTION PLOT



total number of events
Data: differential rate
S1 vs S2 plane

CONCLUSIONS

CONCLUSIONS

- We developed a bayesian analysis to explore the reach of direct detection experiments.
- The ML implementation (SWYFT) is fundamental for estimating the posteriors in a fast way.
- We presented here 01 (SI) & 04 (SD) as first examples.
- We computed the parameter space where σ and m can be reconstructed.
- We compared: total number of events vs the differential rate vs the full S1-S2 space.

NEXT...

- Apply to other NR-EFT operators → combine operators
- Different DD experiments → combine experiments
- Compare with MCMC analysis.



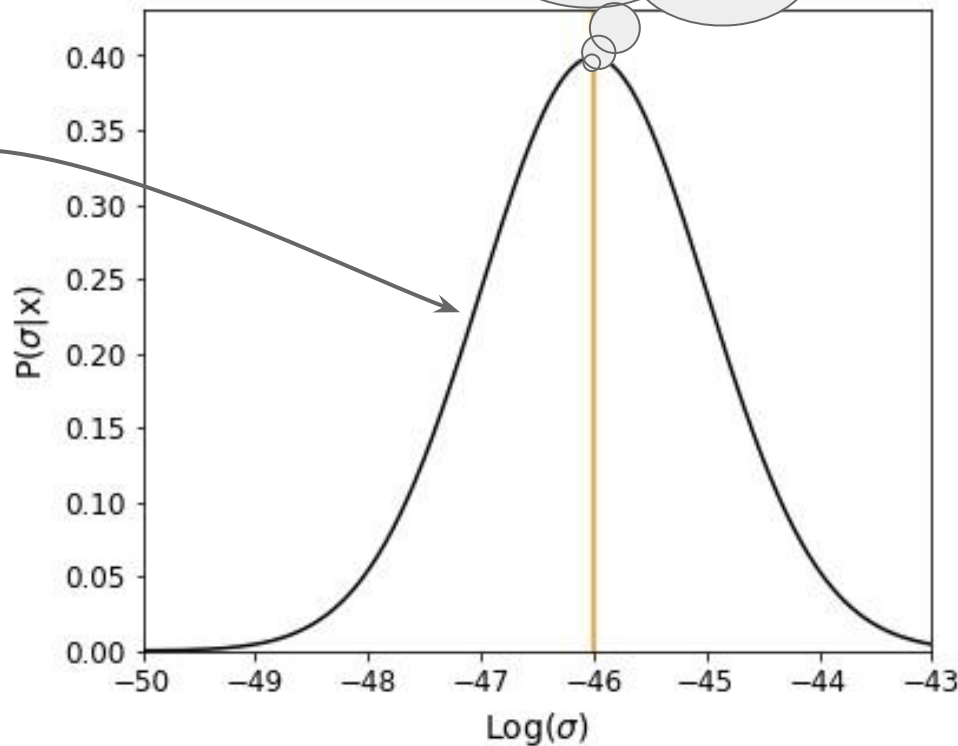
THANK YOU

BACK-UP

RECONSTRUCTION OF PARAMETERS

Once we trained SWYFT we can compute the posterior for any new pseudo experiment

For example $P(\sigma|x)$



RECONSTRUCTION OF PARAMETERS

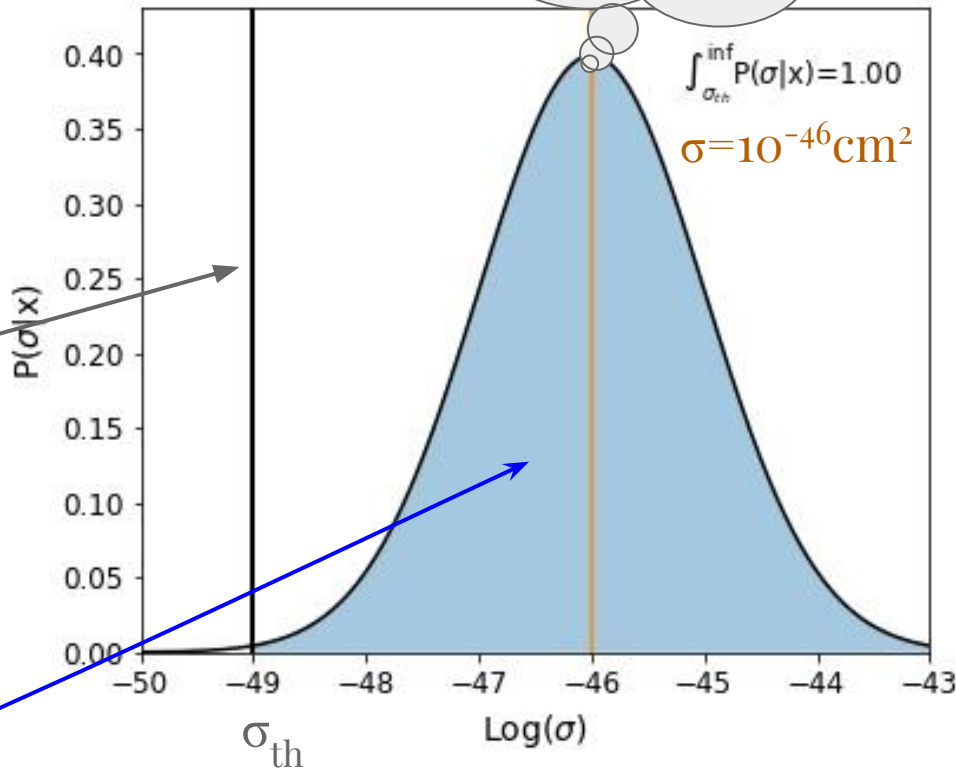
Once we trained SWYFT we can compute the posterior for any new pseudo experiment

We define a σ_{th} threshold:

$\sigma_{th} = 10^{-49} \text{cm}^2 \rightarrow$ **NO SIGNAL!**

Then, we can *reconstruct* σ if:

$$\int_{\sigma_{th}}^{\text{inf}} P(\sigma|x) > 0.90$$



RECONSTRUCTION OF PARAMETERS

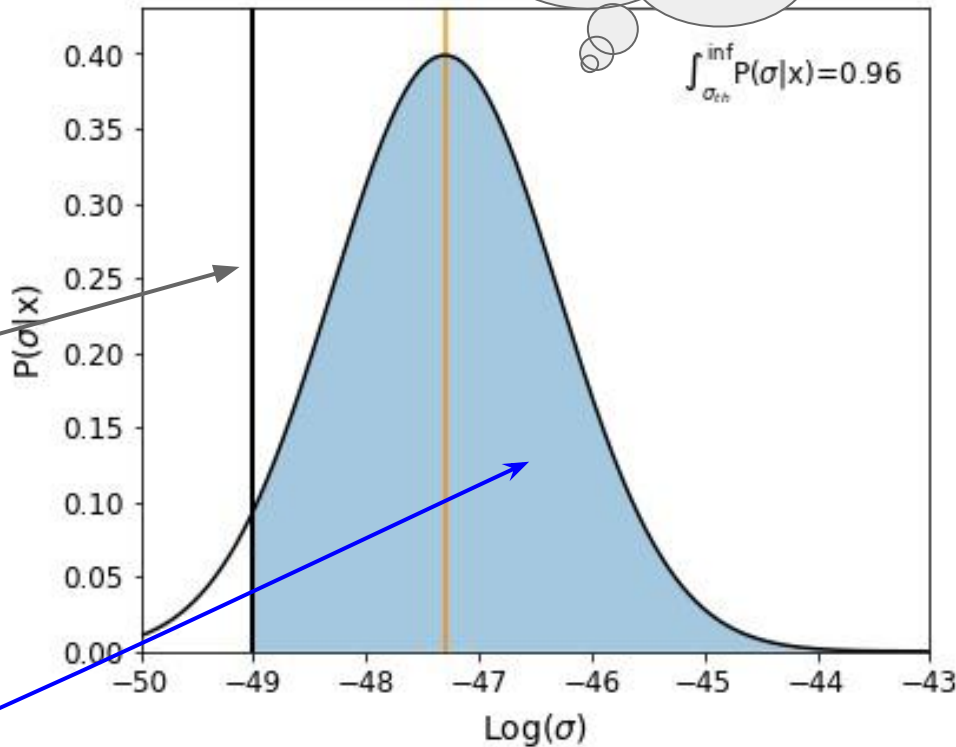
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RECONSTRUCTION OF PARAMETERS

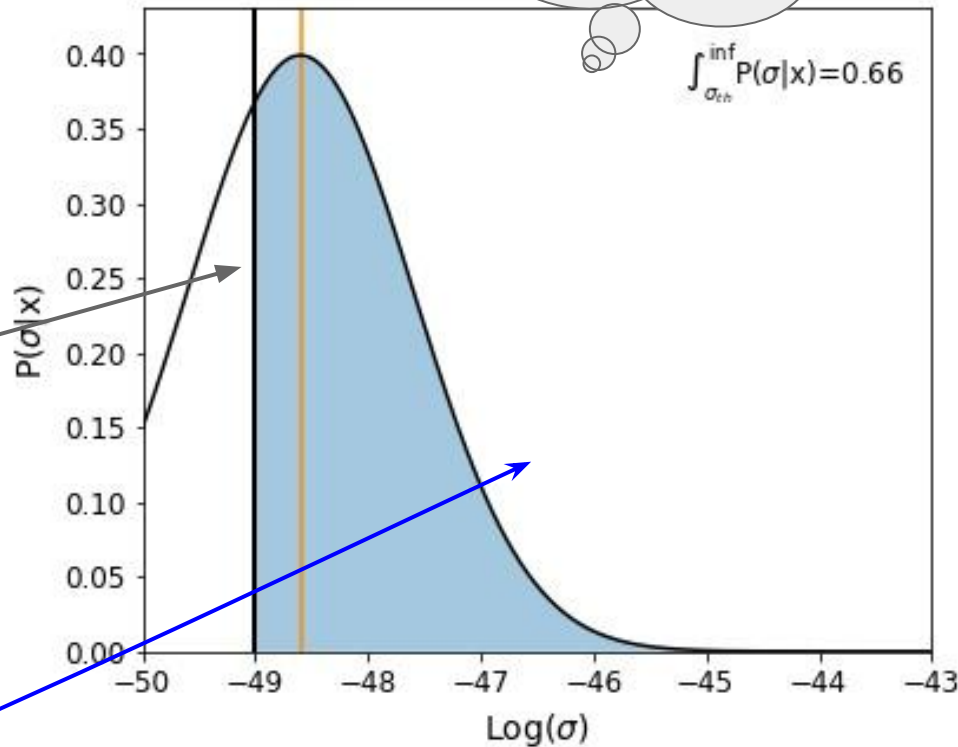
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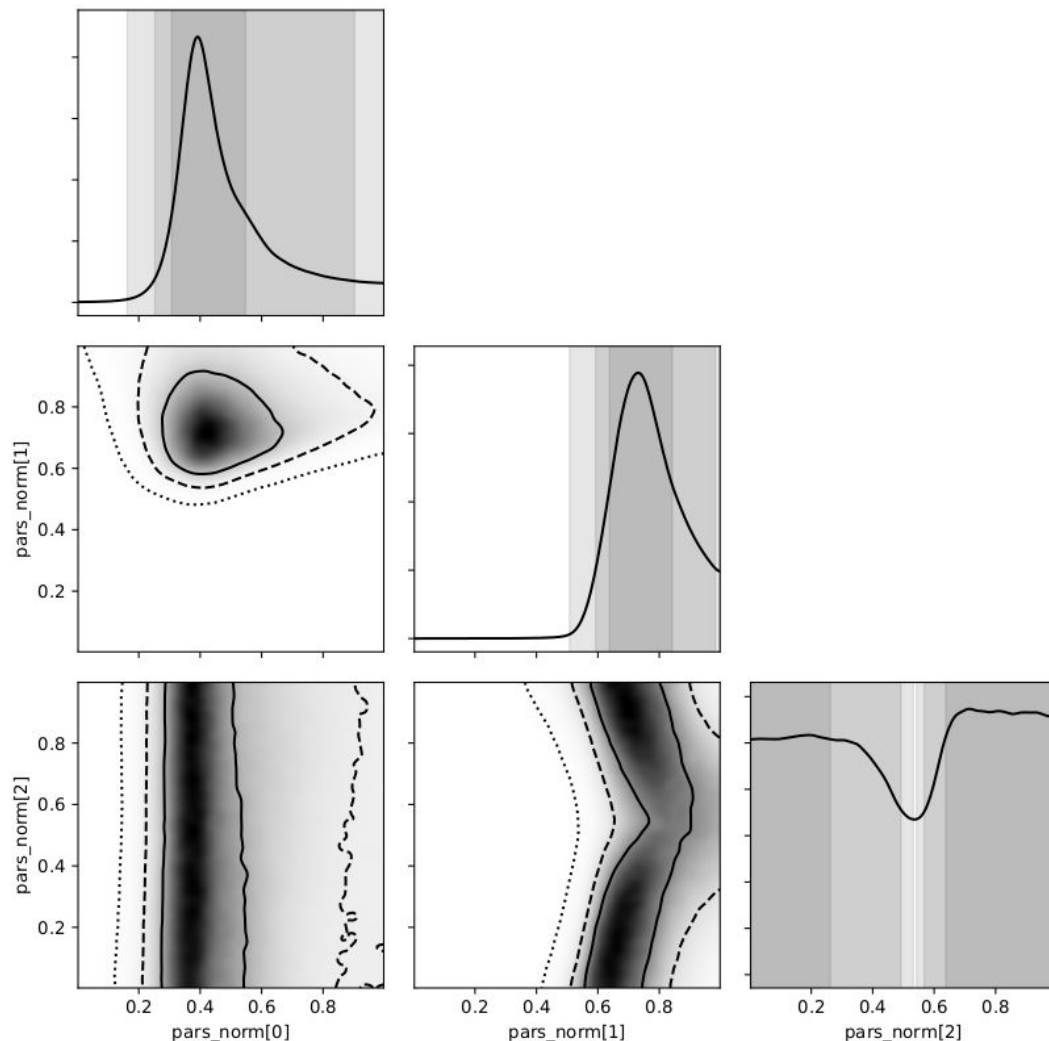
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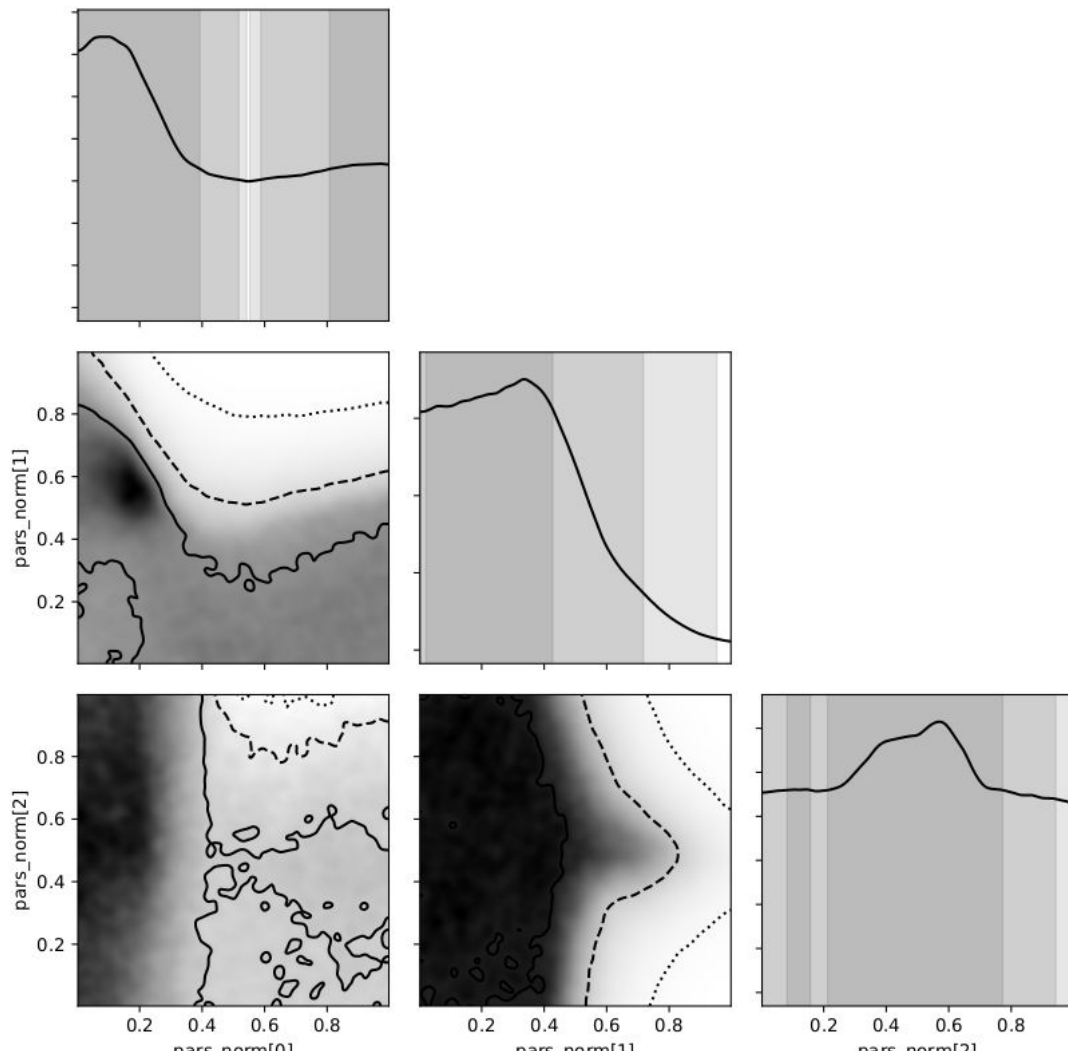
$$\int_{\sigma_{th}}^{\text{inf}} P(\sigma|x) > 0.90$$



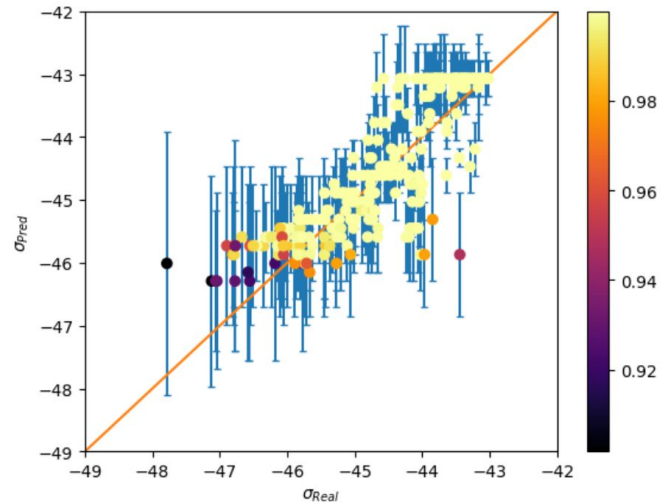
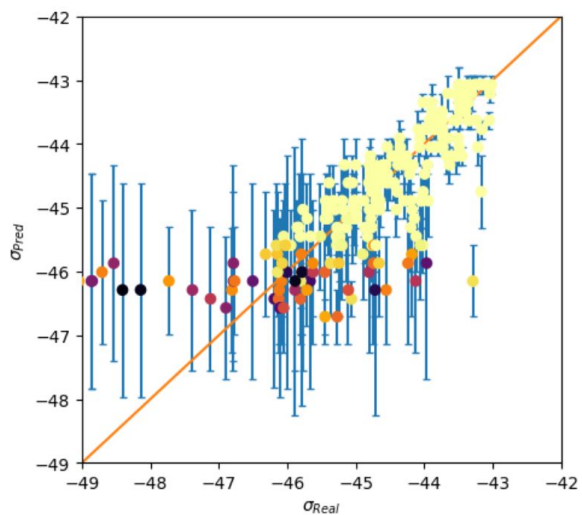
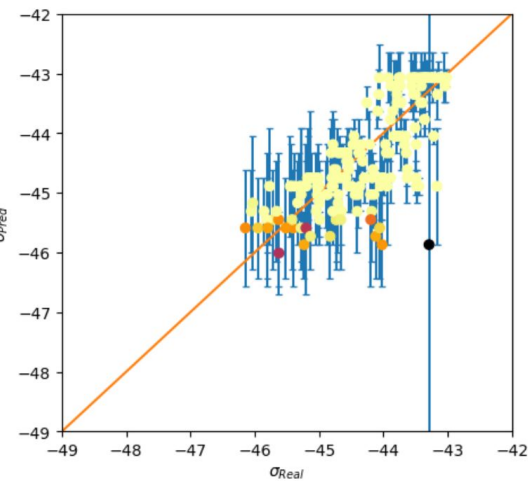
2D POSTERIOR. DISCOVERY S1-S2 (01)



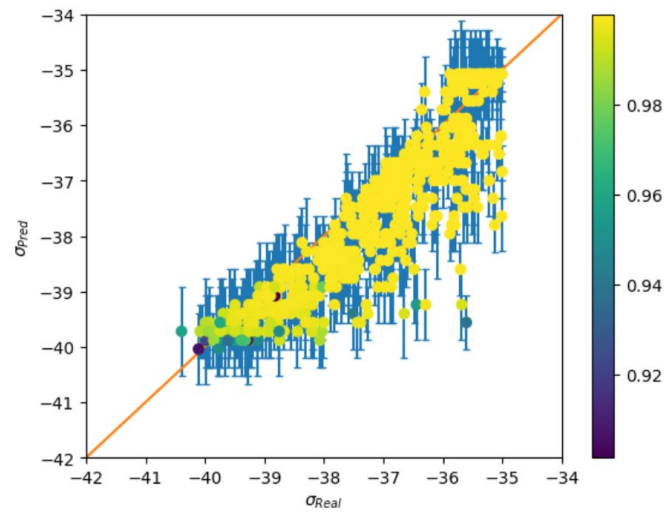
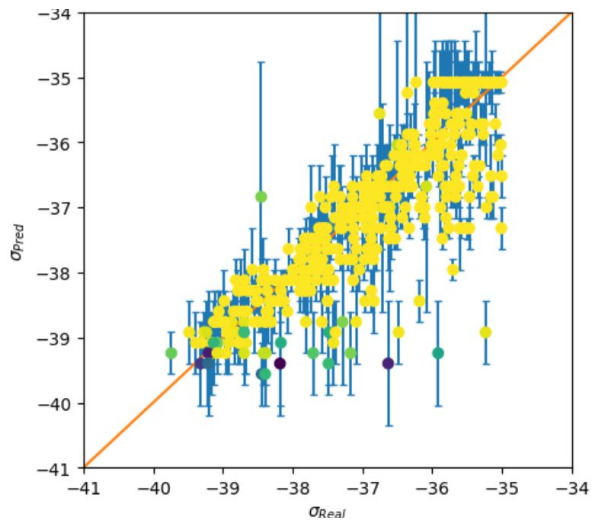
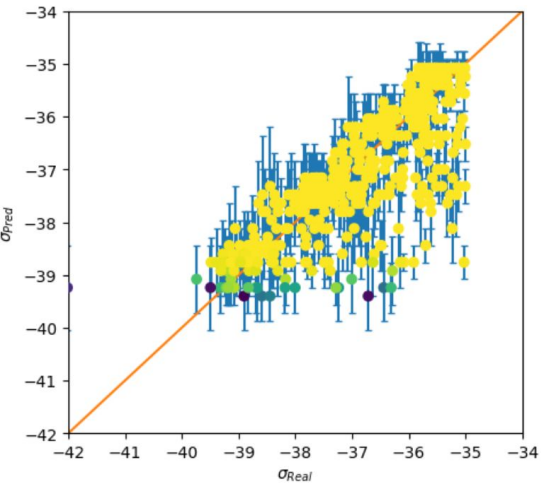
2D POSTERIOR. EXCLUSION S1-S2 (01)



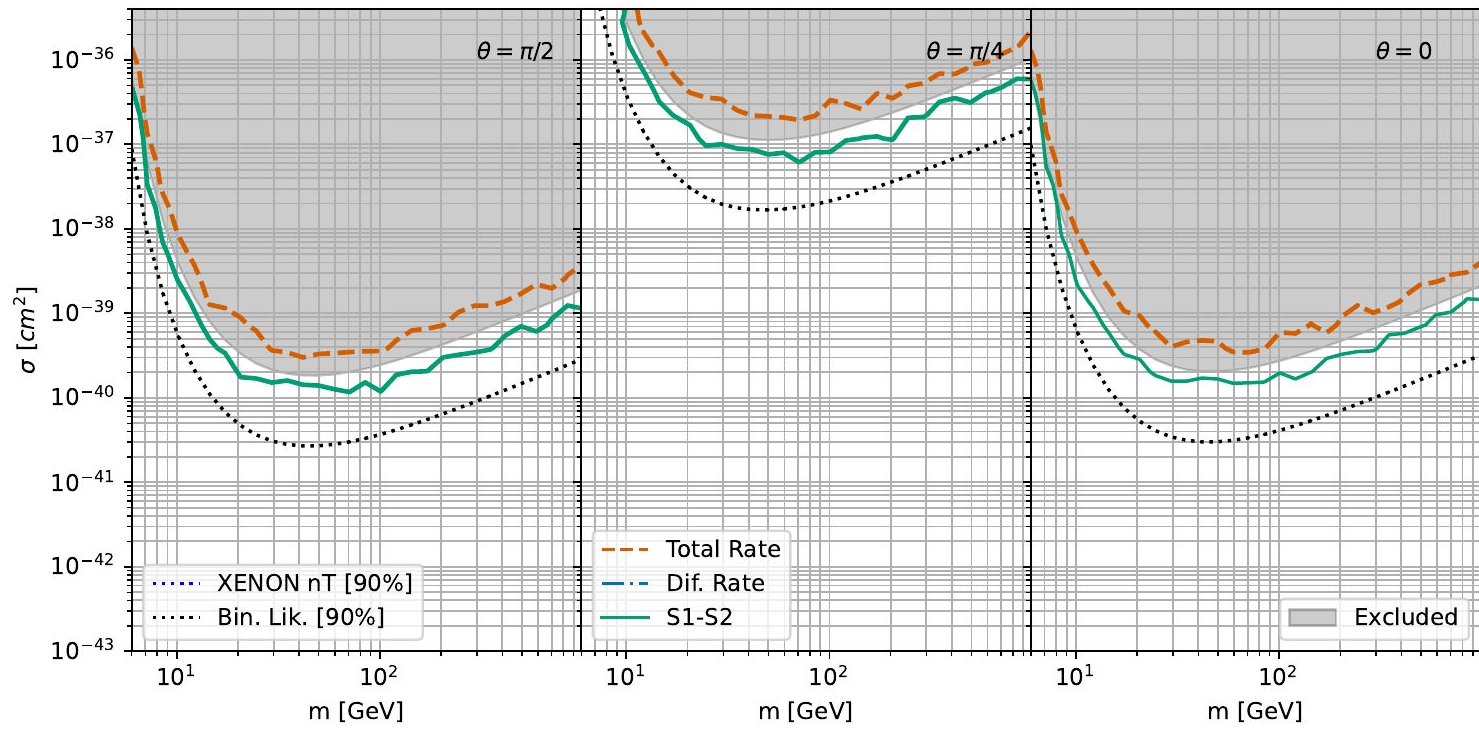
O1 UNCERTAINTIES



04 UNCERTAINTIES



RESULTS: σ RECONSTRUCTION PLOT



Data: total number of events
differential rate
S1 vs S2 plane