

# Galactic propagation of GCRs and EGCRs in the shin region with CRPropa

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**CR/Propa** Workshop on Astroparticle Propagation  
Instituto de Física Teórica UAM-CSIC, Madrid  
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# Outline of lecture

- 1) The transition region in data
  - Spectrum, composition and dipole anisotropy
  - Open questions → role of GMF
- 2) Computational challenges and requirements
  - Ballistic vs. diffusive propagation
  - Galactic magnetic field modelling
- 3) Combating the transition region: Propagation in the Galactic magnetic field
  - Propagation effects in the GMF
  - Effect on observables (flux, composition and arrival direction)
- 4) Summary

The transition region in data

# Cosmic ray energy spectrum

Broken power-law with three ‘main’ features:

- ‘**knee**’: softening at  $\sim 10^{15.4}$  eV
- ‘**ankle**’: hardening at  $\sim 10^{18.7}$  eV
- high-energy cut-off beyond  $\sim 10^{19.6}$  eV

Further more subtle features:

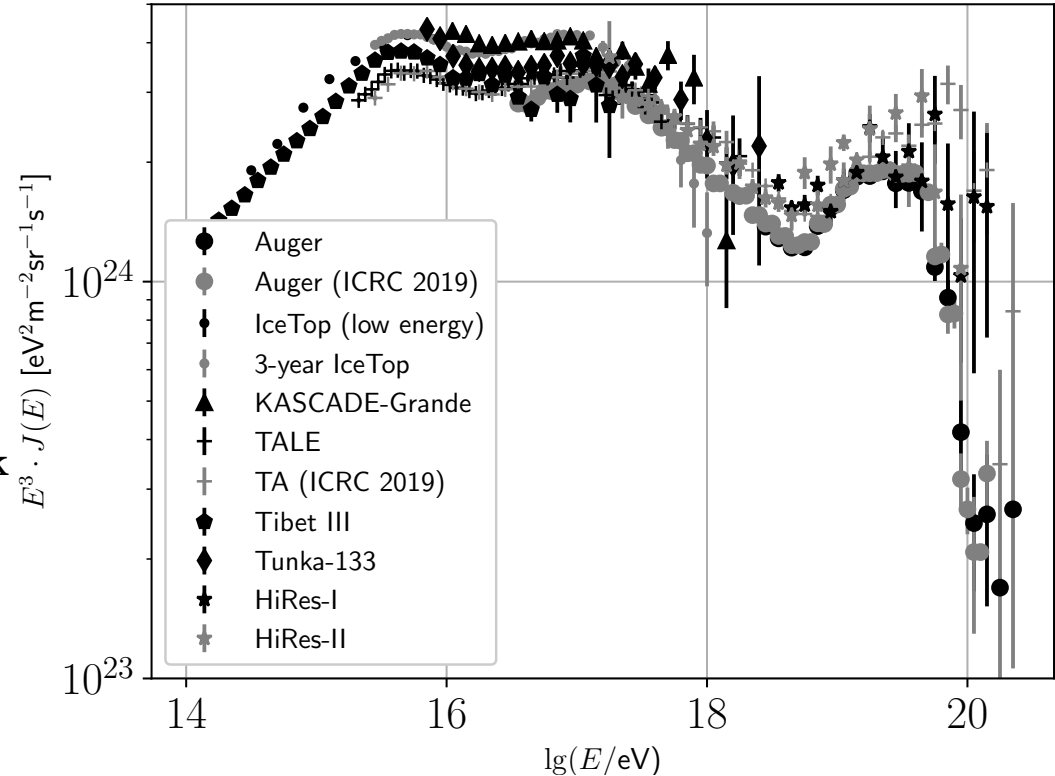
- hardening at  $\sim 10^{16.7}$  eV
- ‘**2<sup>nd</sup> knee**’: softening at  $\sim 10^{17.(0...4)}$  eV
- ‘**toe**’: softening at  $\sim 10^{19.1}$  eV

**Galactic** cosmic rays (**GCRs**) for diffusive shock acceleration (DSA) in supernova remnants (SNR) dominate **below** ‘**knee**’ energies.

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**Transition** region (= ‘**shin**’) **unexplained**:

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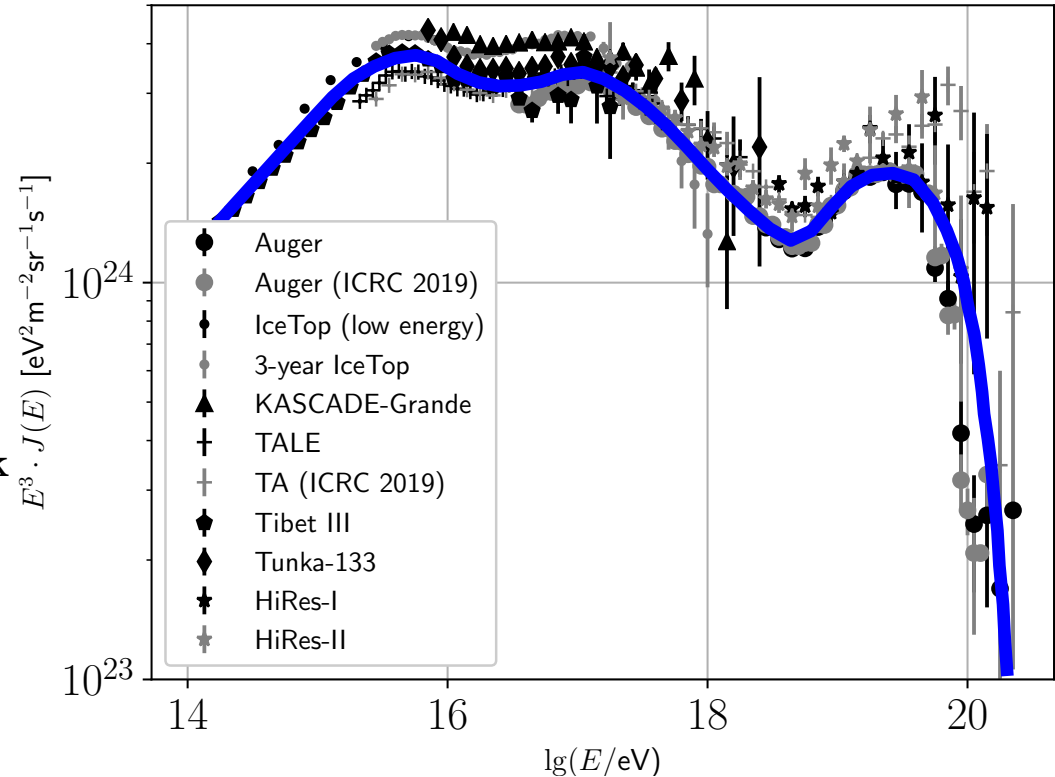
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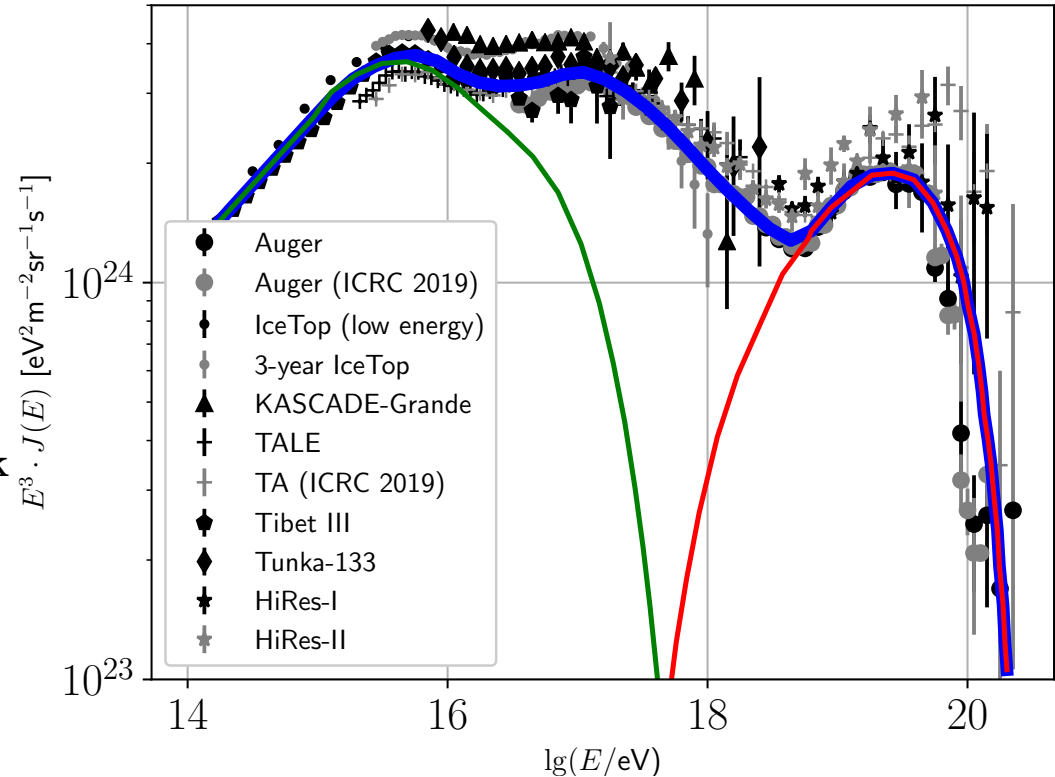
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see also: Thoudam, Astron.Astrophys. 595 (2016) A33



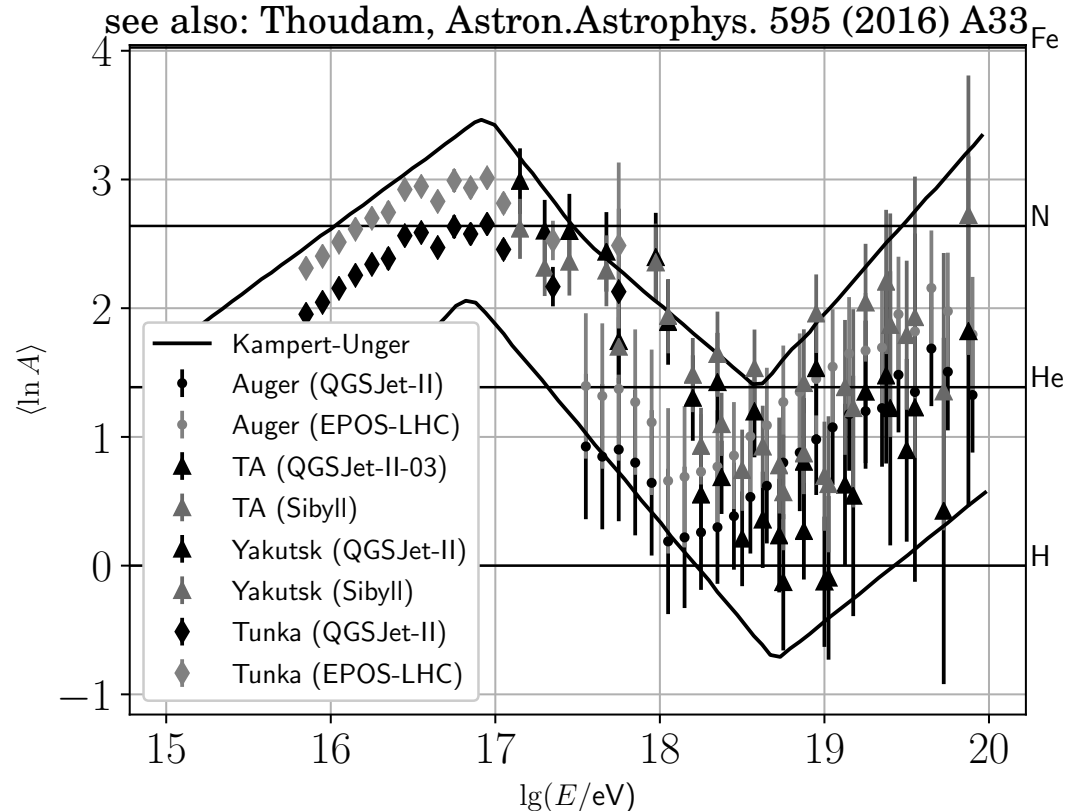
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Composition highly energy-dependent:

- heavier beyond the ‘knee’
- maximum **before** ‘2<sup>nd</sup> knee’
- minimum just before ‘ankle’
- **increasing mean mass at high-energy cut-off**

Increasing mean mass  
→ **rigidity-dependent** change in:

- source properties (**maximum acceleration energy**)
- **propagation regimes** in magnetic fields



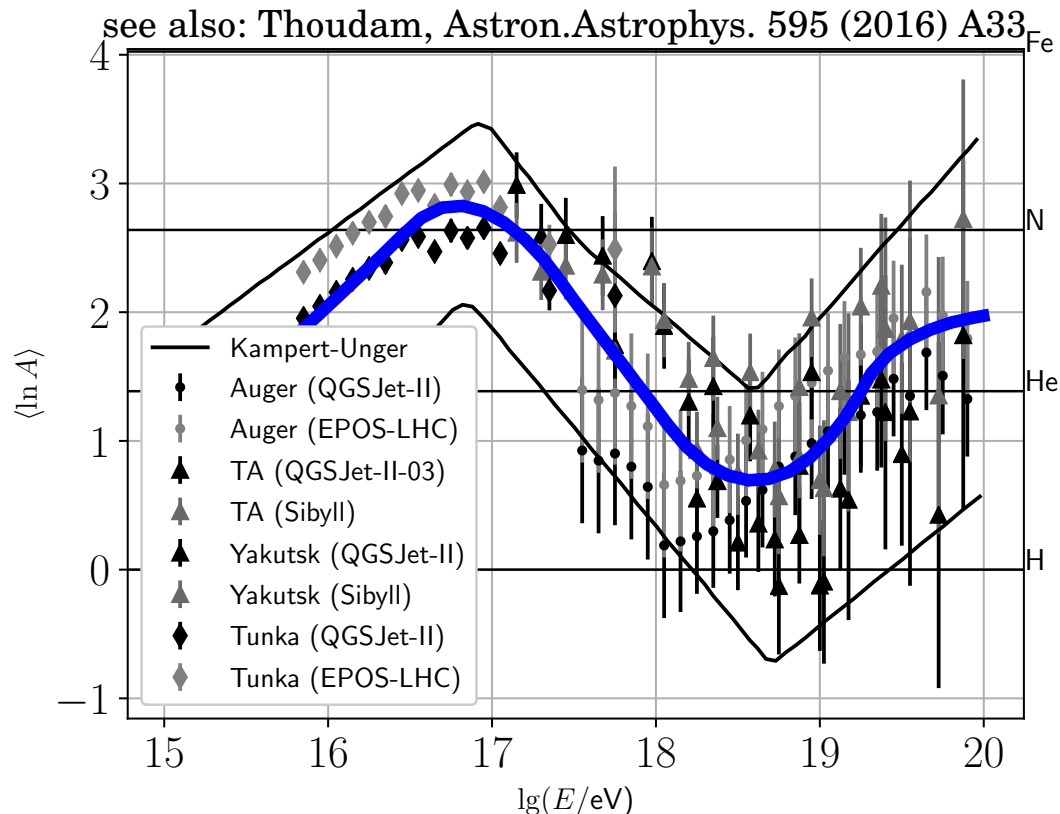
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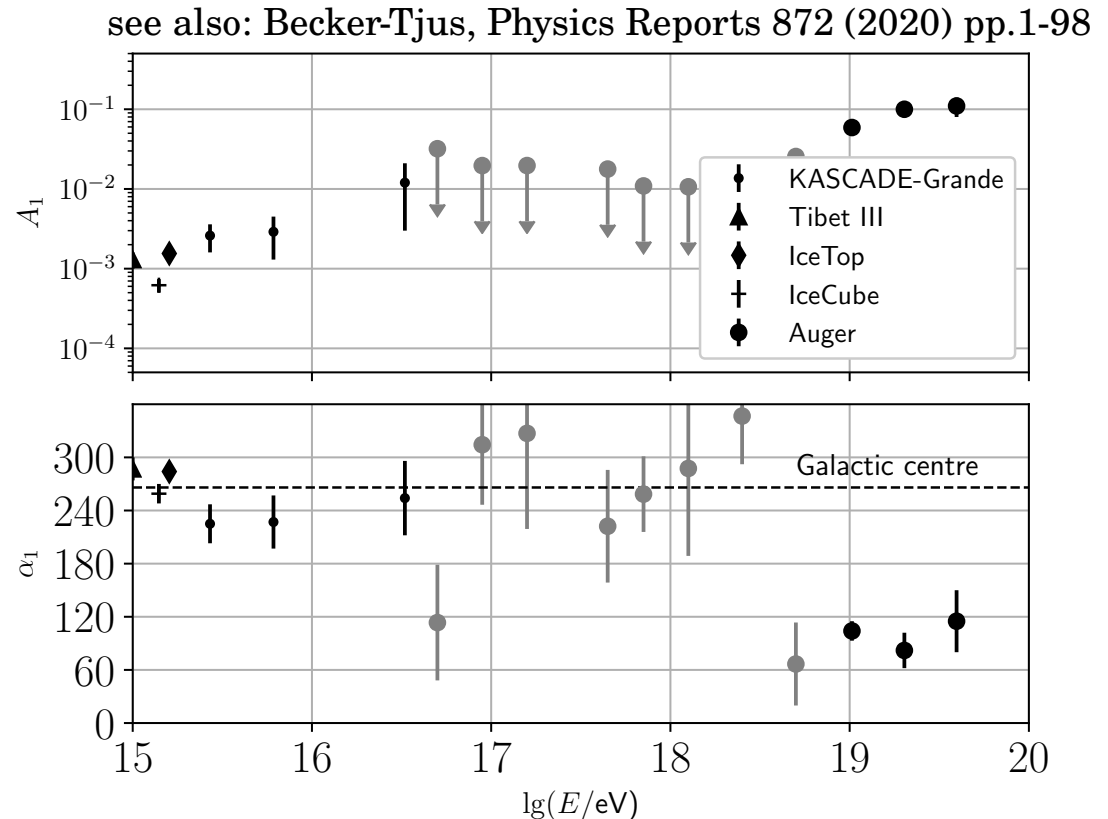
# Cosmic ray anisotropy (dipole)

## Dipole anisotropy:

- amplitude increases with energy
- **no significant dipole** between  $\sim 10^{16.5} \text{ eV} - 10^{19} \text{ eV}$
- **phase roughly constant** in both energy ranges but **shifts away from Galactic centre (GC)** for highest energies  
→ **extragalactic** origin likely

## Small-scale anisotropies:

- amplitude and direction indicate strength of **diffusion** vs. **advection**: correlation with **source direction**  
⇒ **strength of Galactic wind**



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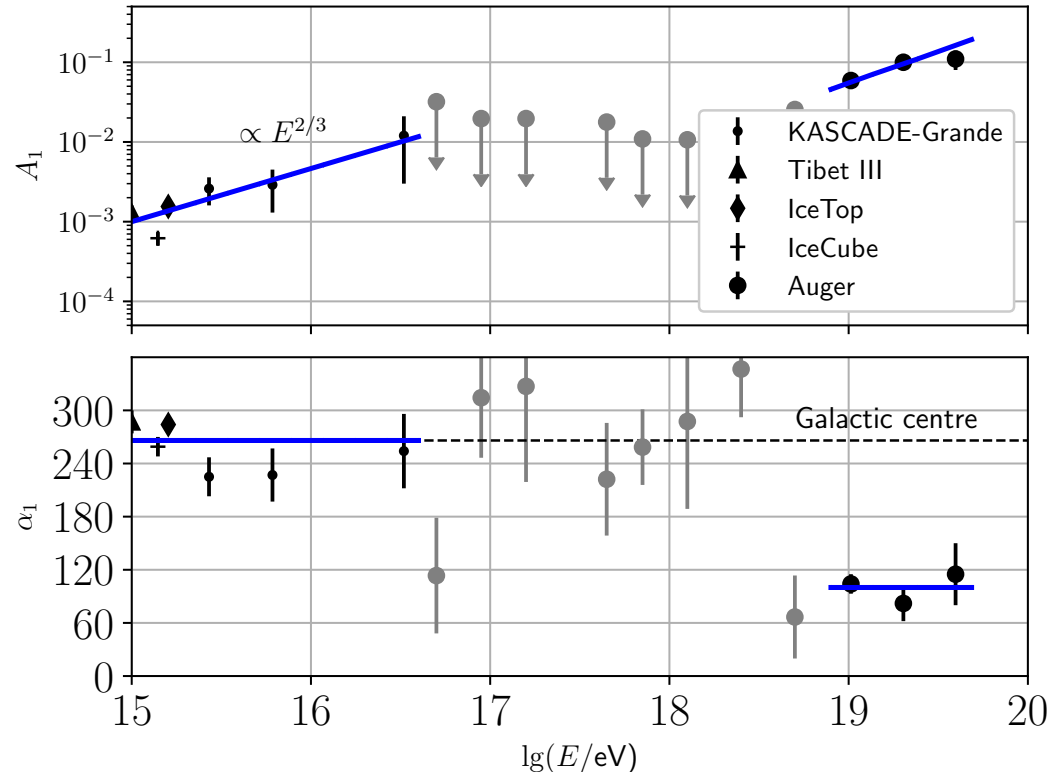
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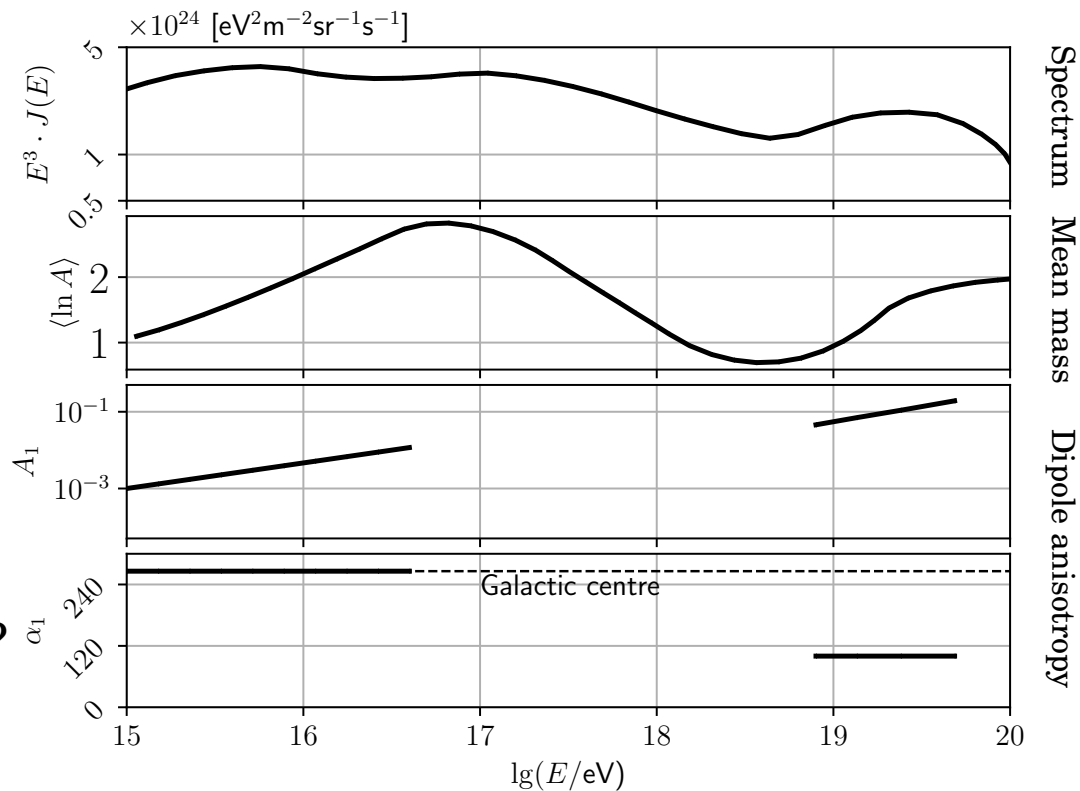
# “All” data in one look

## Composition:

- What **explains ‘2<sup>nd</sup> knee’** if maximum mean mass is reached well before?
- Why does the composition become **lighter up to the ‘ankle’**?

## Spectrum:

- How could **GCRs** be accelerated up to energies **beyond the ‘knee’**?
- What **constraints** are there on **low-energy** contribution of **EGCRs**?
- **How are observables affected by the propagation in the Galactic magnetic field (GMF)?**



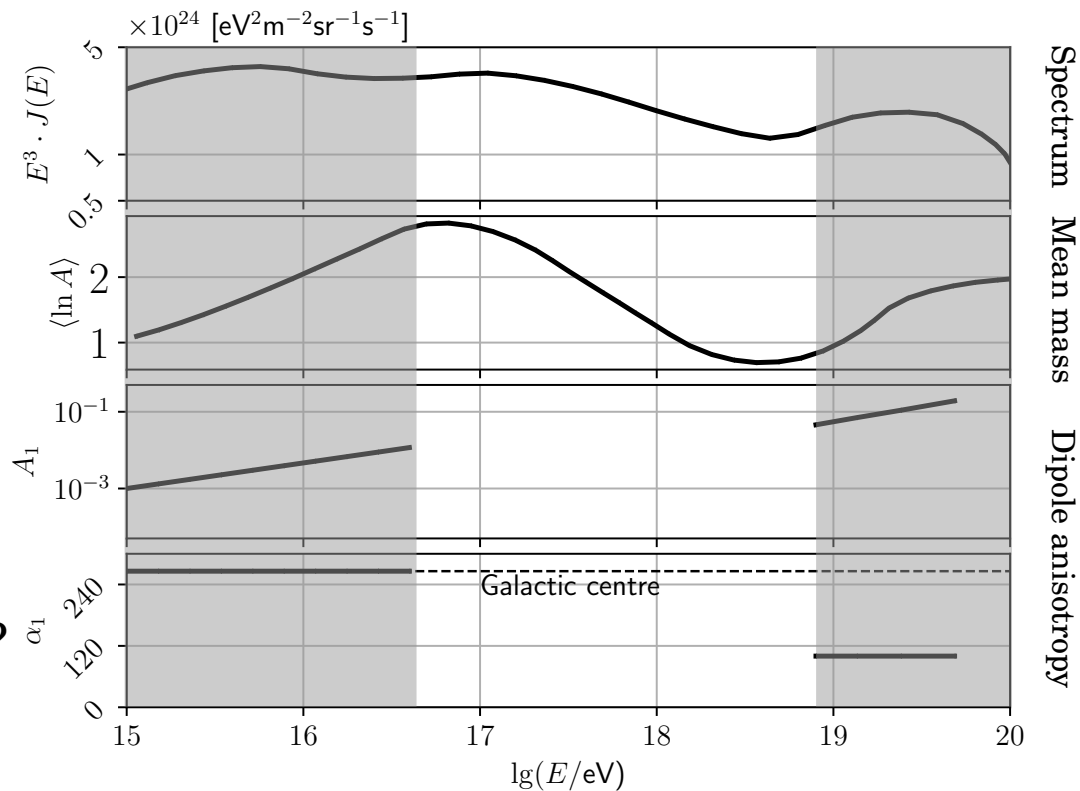
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# Galactic magnetic field (GMF)

x-z projection of JF12 field

**GMF model: JF12** (ApJ 757 14x) with three components:

- Large-scale regular
- Large-scale random (striated)
- (Small-scale) random

GMF has **three regions** of differing **field strength**:

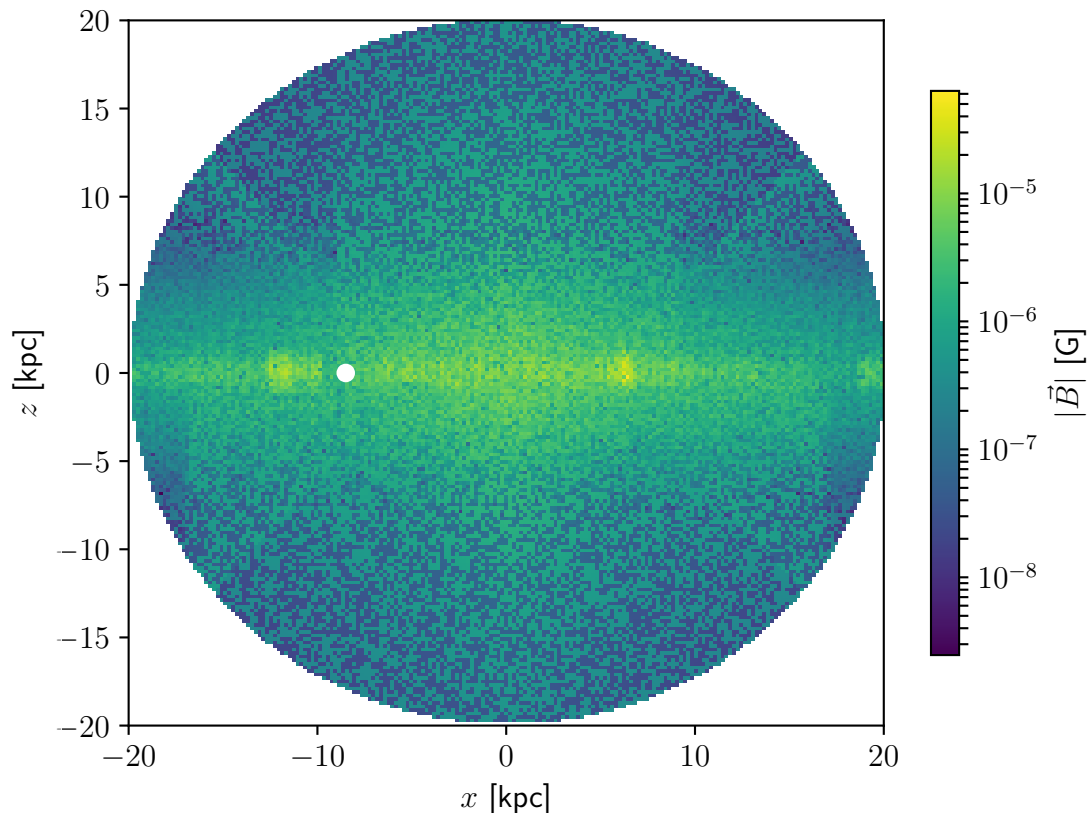
- **Galactic plane (GP):**  $\sim 1 - 10 \mu\text{G}$
- Halo:  $\sim 0.1 - 1 \mu\text{G}$
- Edge of Galaxy:  $10 - 100 \text{ nG}$

**Gyroradius  $r_g$ :**

$$r_g[\text{pc}] \approx 11 \cdot \frac{R[\text{PV}] \cdot v_{\perp}/c}{B[\mu\text{G}]}, \quad R = E/Ze$$

Transition region = **change in propagation regimes**

- **diffusive**  $\rightarrow$  **ballistic** propagation



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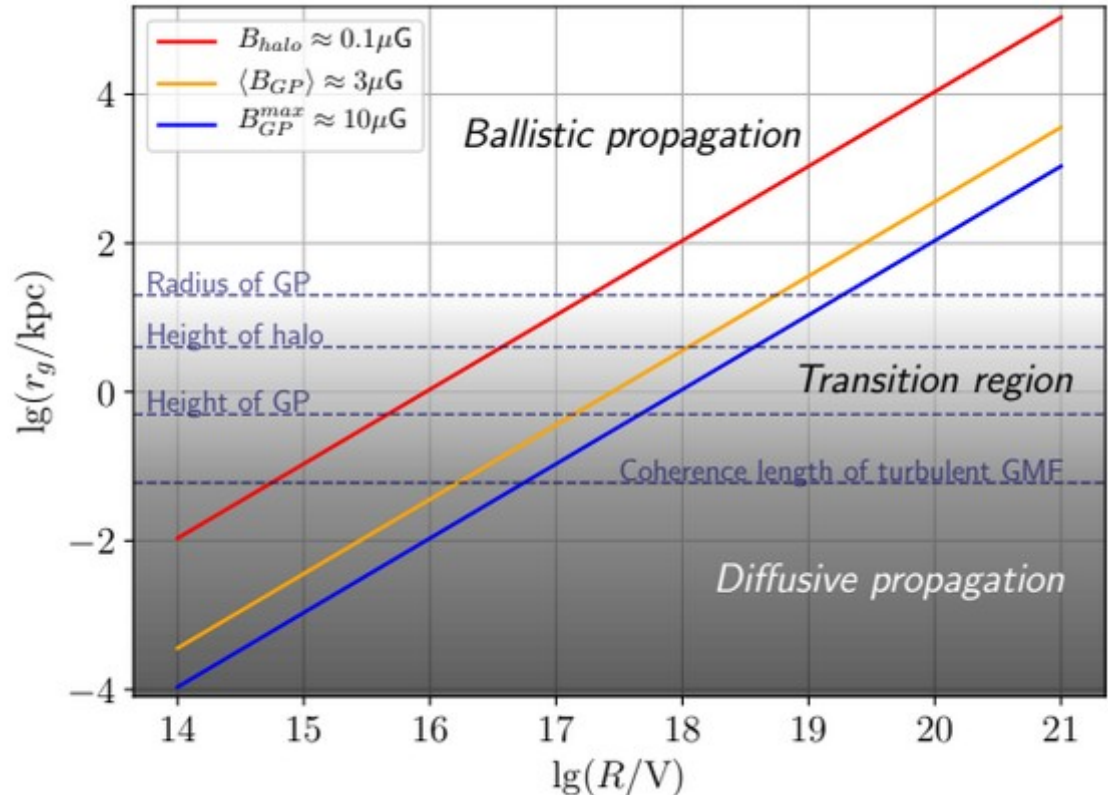
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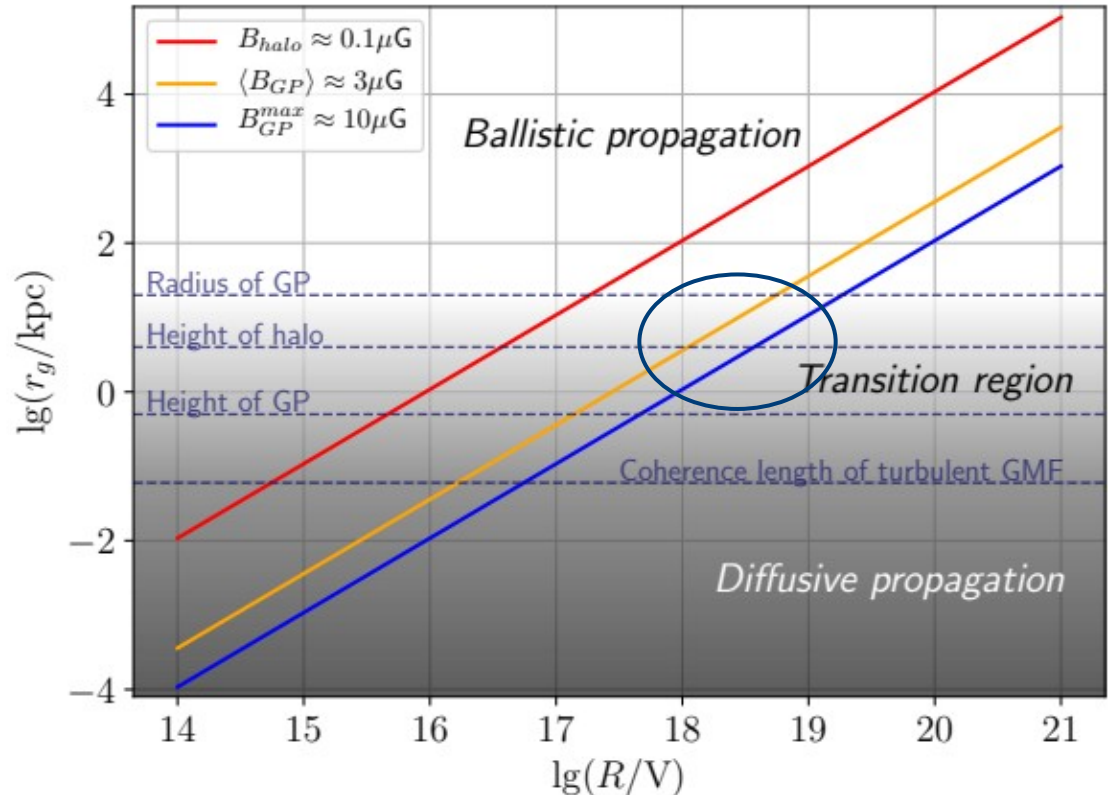
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# Computational challenges and requirements

# Ballistic propagation

Trajectories of ballistically propagating GCRs

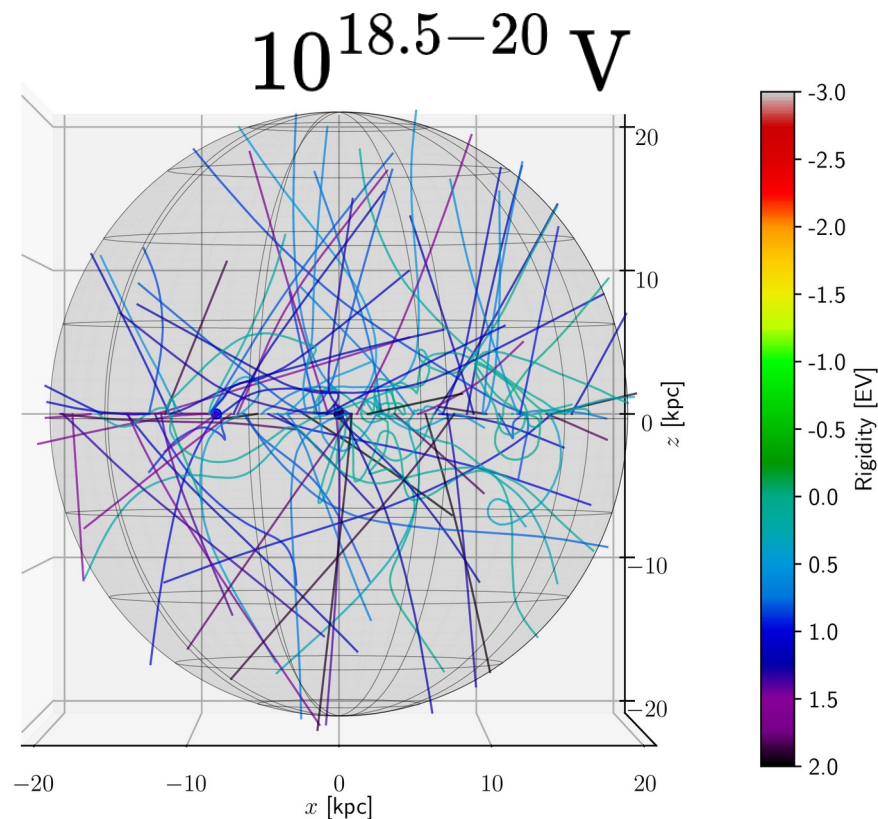
Solve **equation of motion (EoM)**:

$$\ddot{\vec{r}} = \frac{q}{E/c^2} \left( \vec{v} \times \vec{B} \right)$$

- tracking of **single particles** (microscopic view)
- best suited for **large**  $r_g$
- applicable for arbitrary fields  
→ **more fundamental and precise\***
- particle trajectories are tracked  
→ possibility of anisotropy studies

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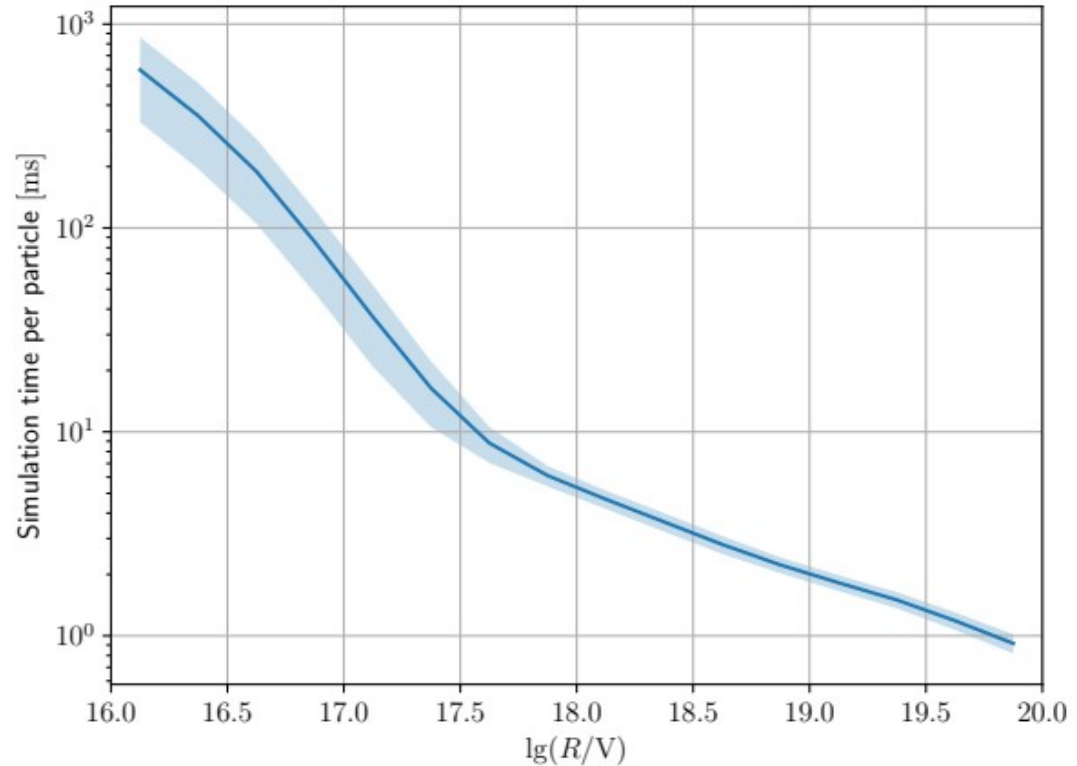
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Change of computation time per particle with rigidity for propagation in GMF



# Diffusive propagation

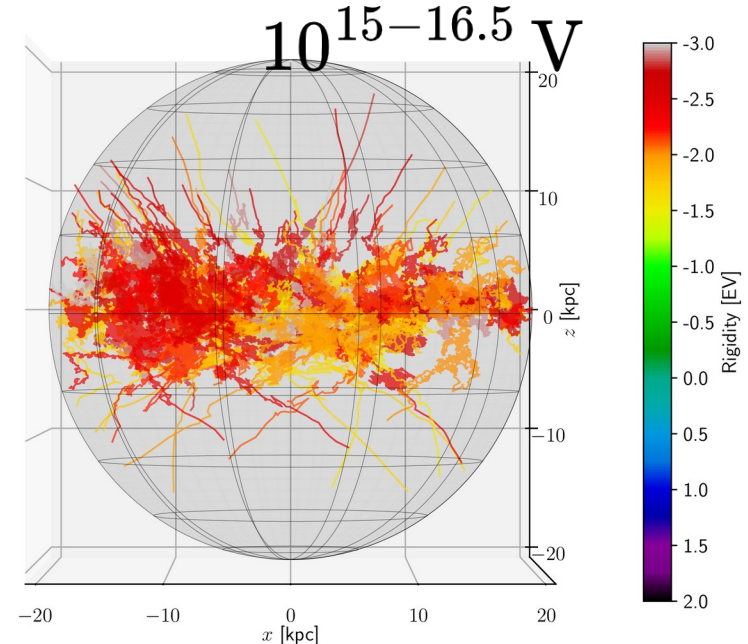
Solve **transport equation (TE)**: 
$$\frac{\partial n_l}{\partial t} = \sum_{j=1}^3 \frac{\partial}{\partial x_j} \left[ \left( D_{jk} \cdot \frac{\partial}{\partial x_k} \right) n_l \right] - \frac{\partial}{\partial x_j} [u_j \cdot n_l] + \frac{\partial}{\partial p} \left[ p^2 D_{pp} \frac{\partial}{\partial p} \left( \frac{n_l}{p^2} \right) \right] - \frac{\partial}{\partial p} \left[ \dot{p} n_l - \frac{p}{3} (\nabla \cdot \vec{u}) \cdot n_l \right] + \sum_{j>l} \frac{v_l}{c} n_0 \int dp' \sigma_{j \rightarrow l}(p, p') n_j(p') - \frac{n_l}{\tau} + Q_l(p)$$

- **multi-particle** approach:
  - change of momentum density (macroscopic view)
- best suited for **small**  $r_g$  & **dominant turbulent** B-field component
  - resonant scattering regime is reached for EoM approach
- generally **shorter** computation times
- For large  $r_g$  increasingly inaccurate

NOTE:

- diffusive propagation module via SDEs is **implemented in CRPropa 3** (JCAP 06 (2017) 046)
- For a **full description** of the transition region **both EoM & TE approaches** must be applied

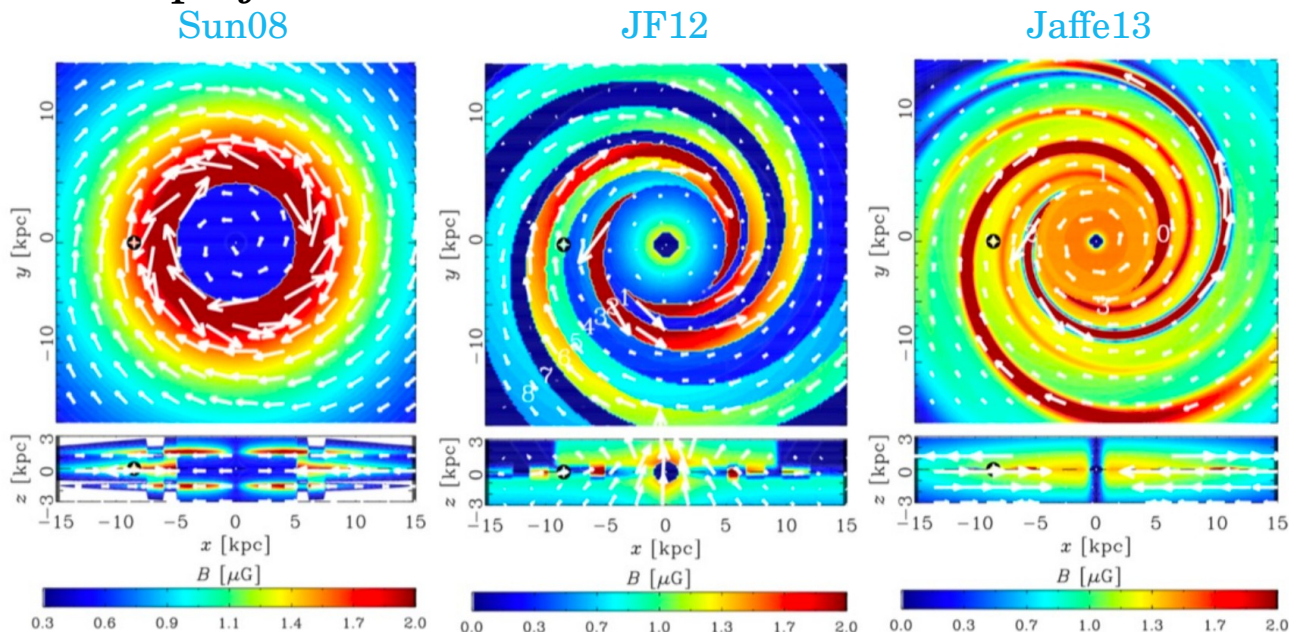
Trajectories of diffusively propagating GCRs





# Major challenge: GMF model

x-y and x-z projections of coherent field for various GMF models



GMF not well known:

- field strength **inferred indirectly via observables** with large uncertainties & contamination
- **ad hoc assumptions** necessary (simplifications): morphological features (spiral arms, halo field), field components (regular, turbulent etc.)

→ many GMF models exist



# Combating the transition region: Propagation in the GMF

# Procedure: Ballistic propagation with CRPropa3

## Forward tracking:

- Cash-Karp algorithm: minimal step size  $d_{min} < 0.1 r_g$ 
  - Boris-Push recommended!
- particle tracked **from source to observer**:
  - highly **inefficient** (1:10<sup>28</sup> for observer the size of Earth)
    - increase observer size, BUT: this introduces **artefacts!** → observer size  $\sim r_g$

## Only propagation effects (i.e. only deflections/no interactions):

- propagation of **one nuclear species: proton** → results can be scaled to all nuclei (important for composition)

## Galactic magnetic field model:

- **JF12** (including regular, random and striated components)
  - edge of Galaxy defined as volume within which GMF is defined (20 kpc sphere are Galactic centre)

## Source properties:

- $R^{-1}$  injection spectrum,  $\lg(R/V) = 16.0 - 20.0$

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# Sources and observers

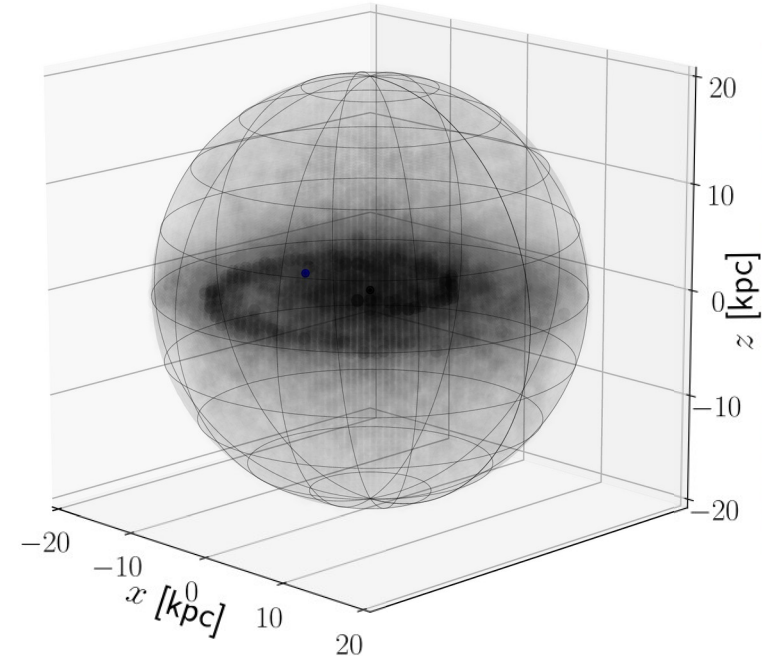
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- **‘Galactic plane’:** cylinder of 100 pc height around Galactic centre with variable radius
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## Galactic volume with GMF



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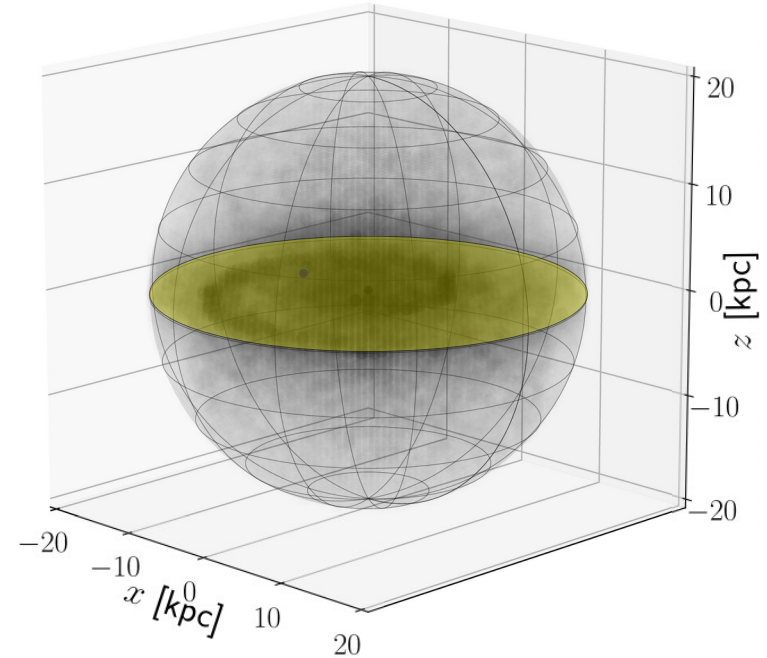
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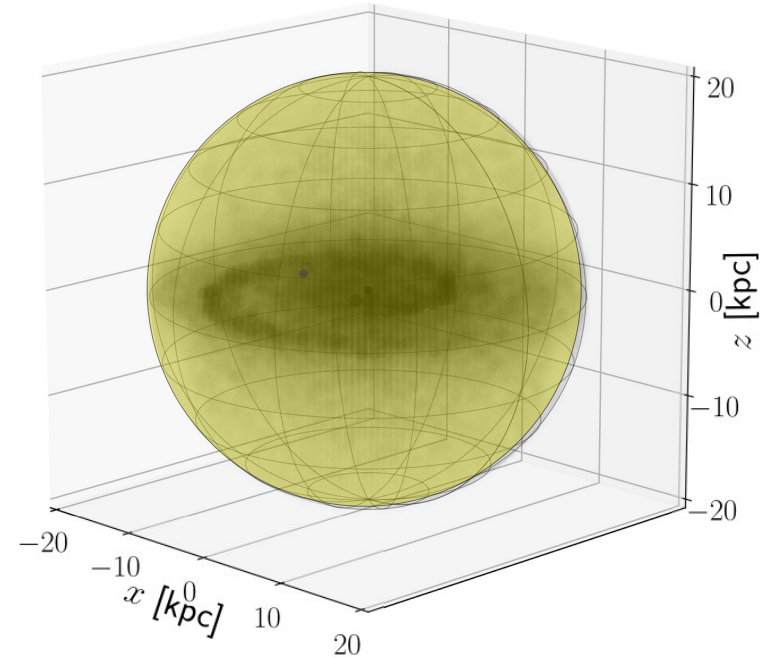
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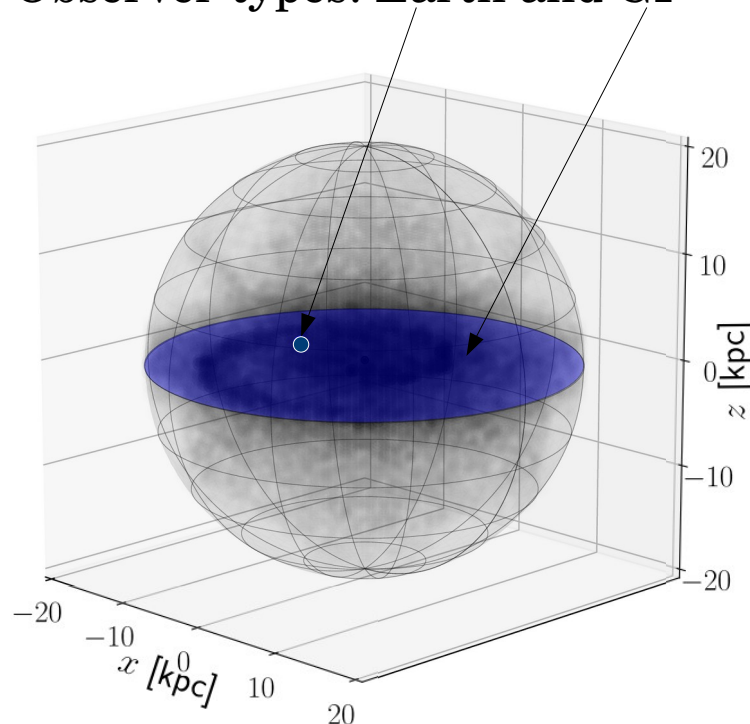
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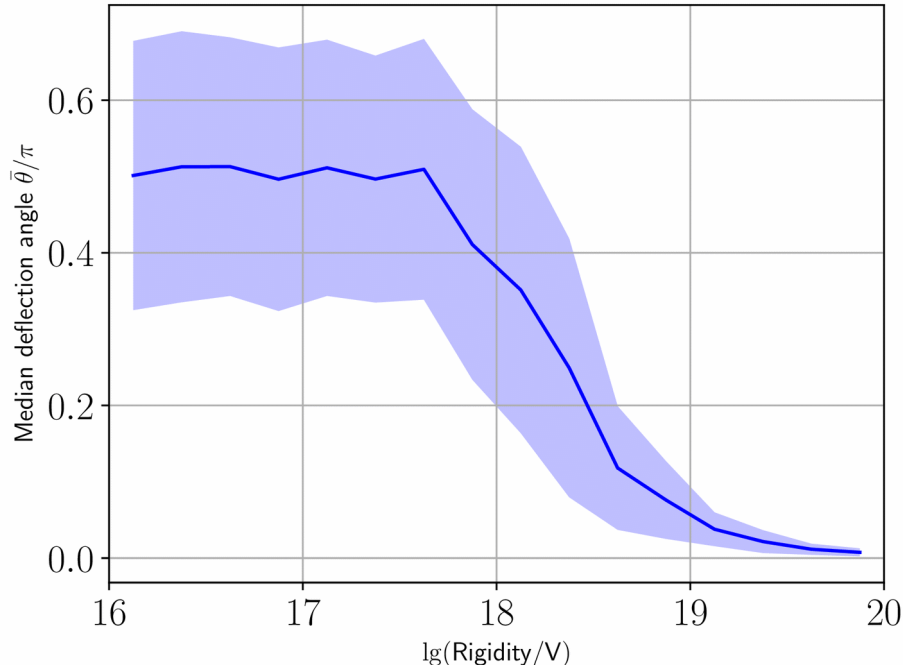
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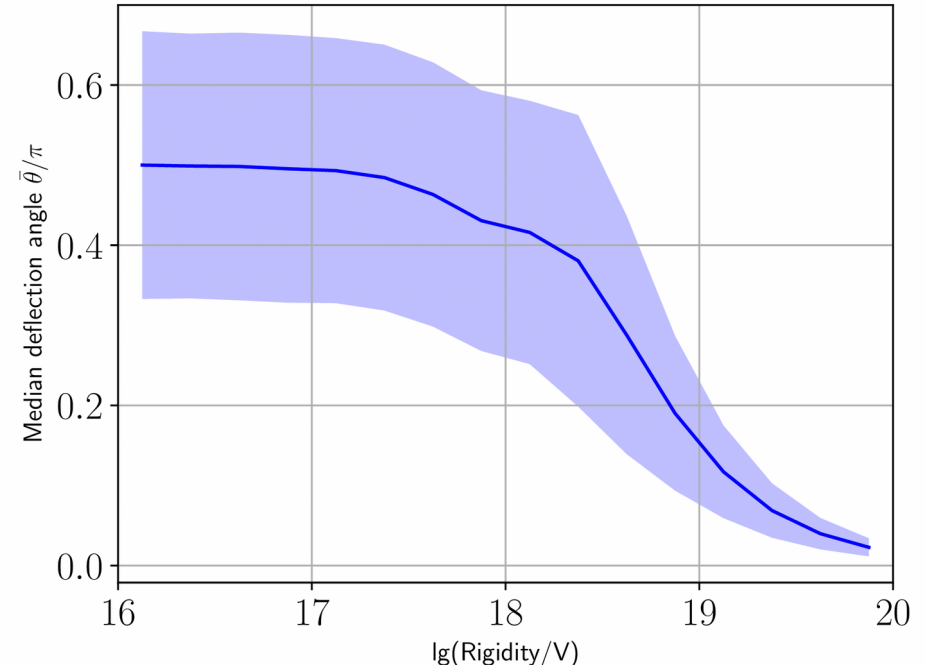


# Change of propagation regimes: Deflection angle

GCRs forward tracked to Earth



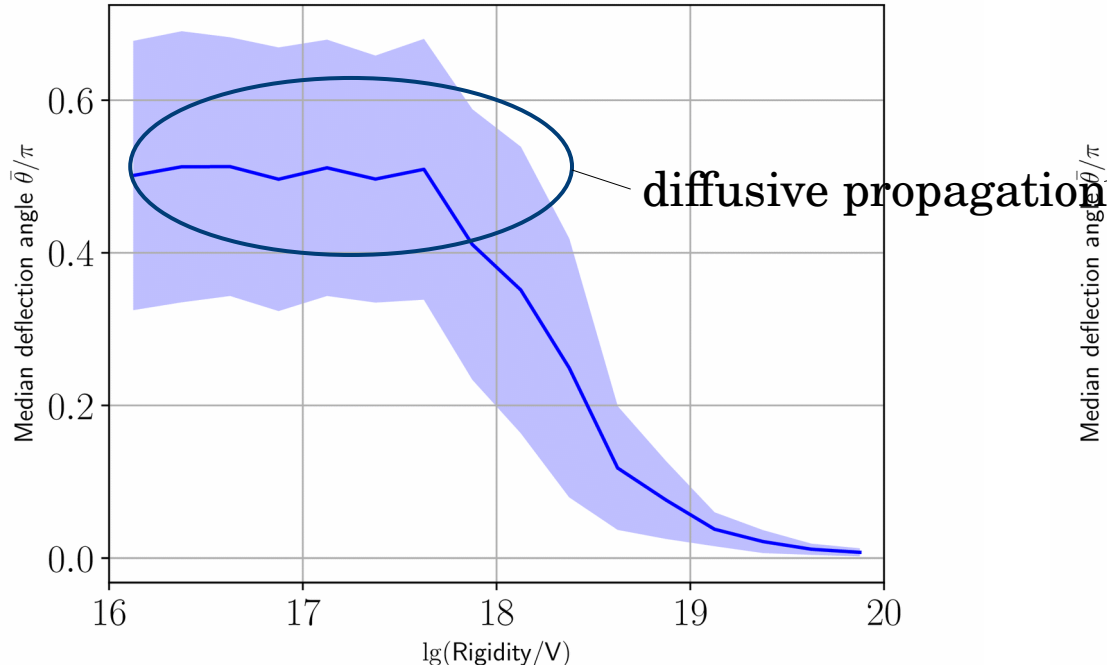
EGCRs backtracked from Earth



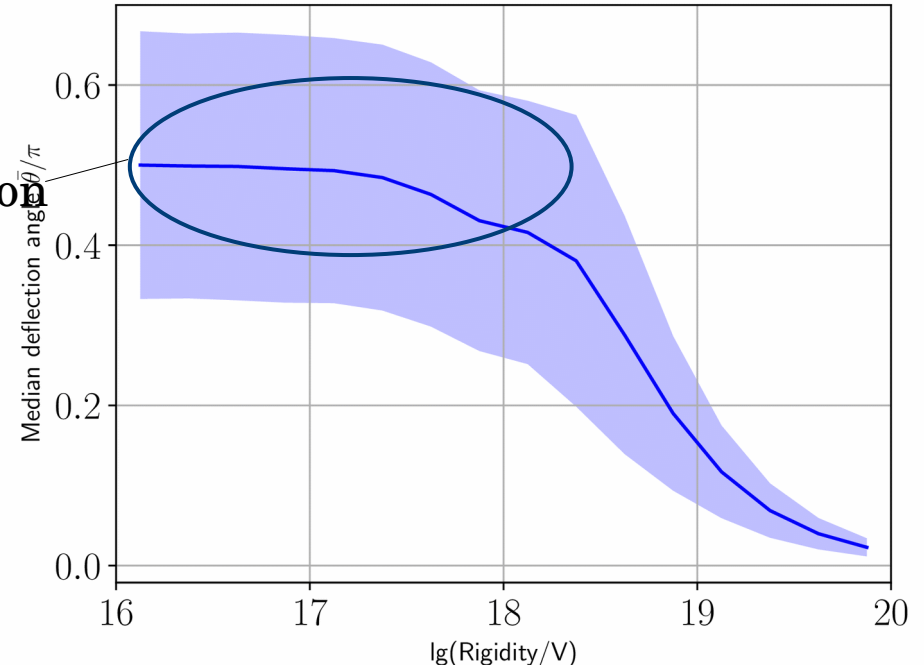
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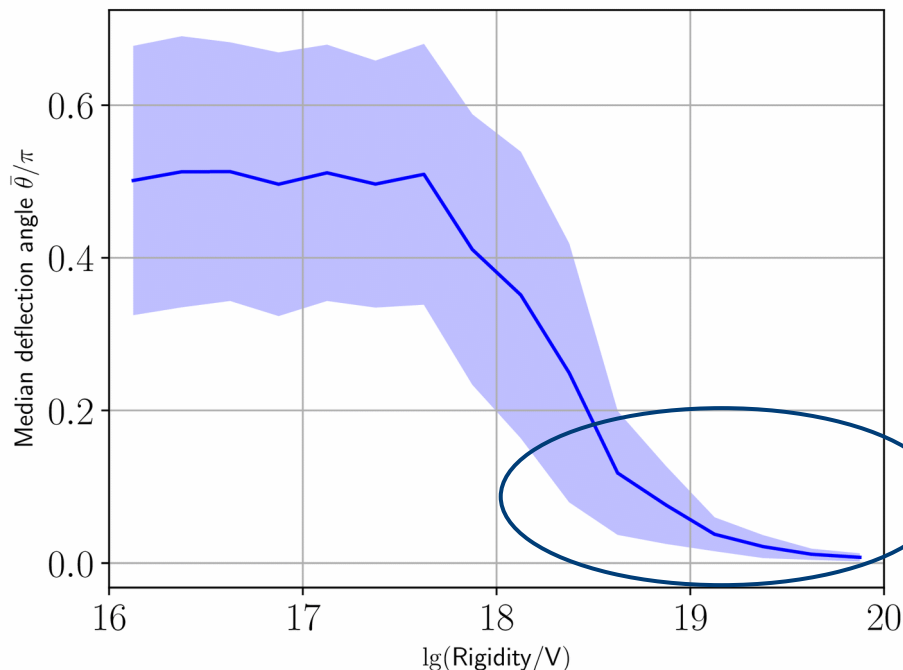
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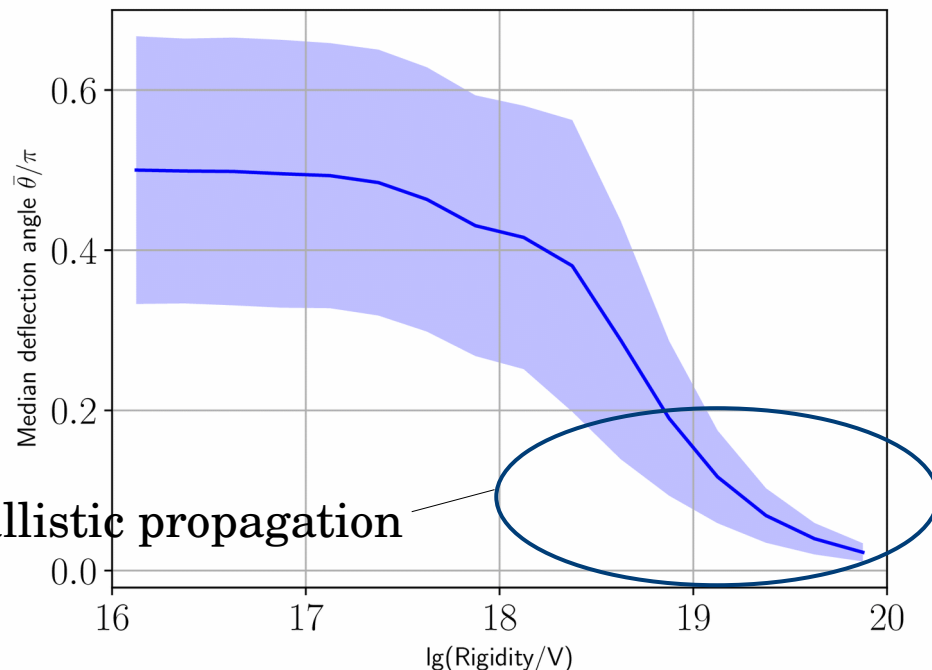
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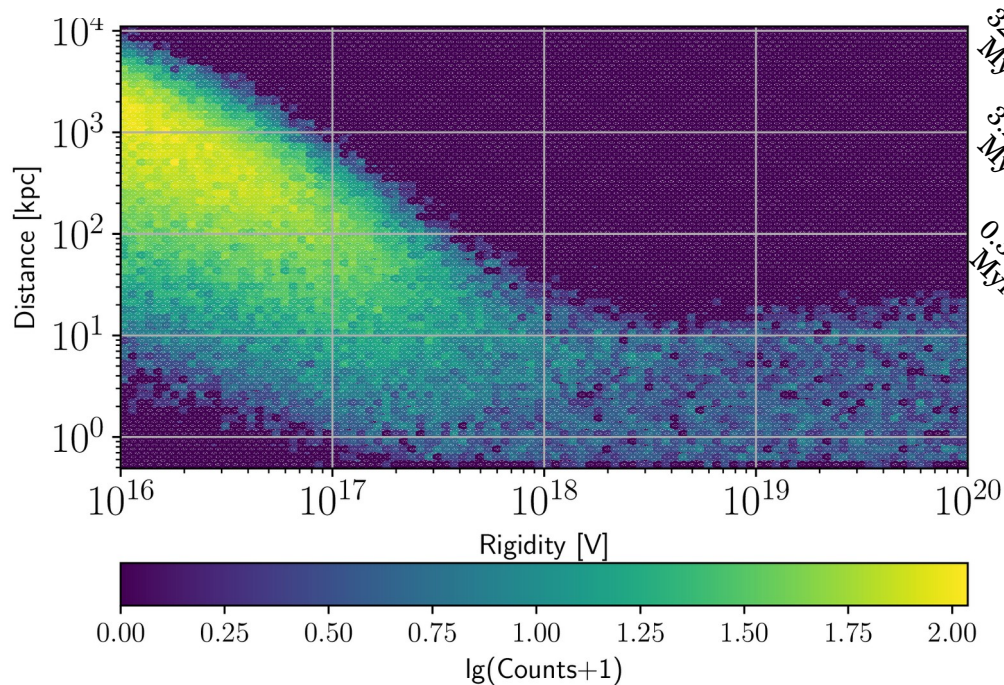
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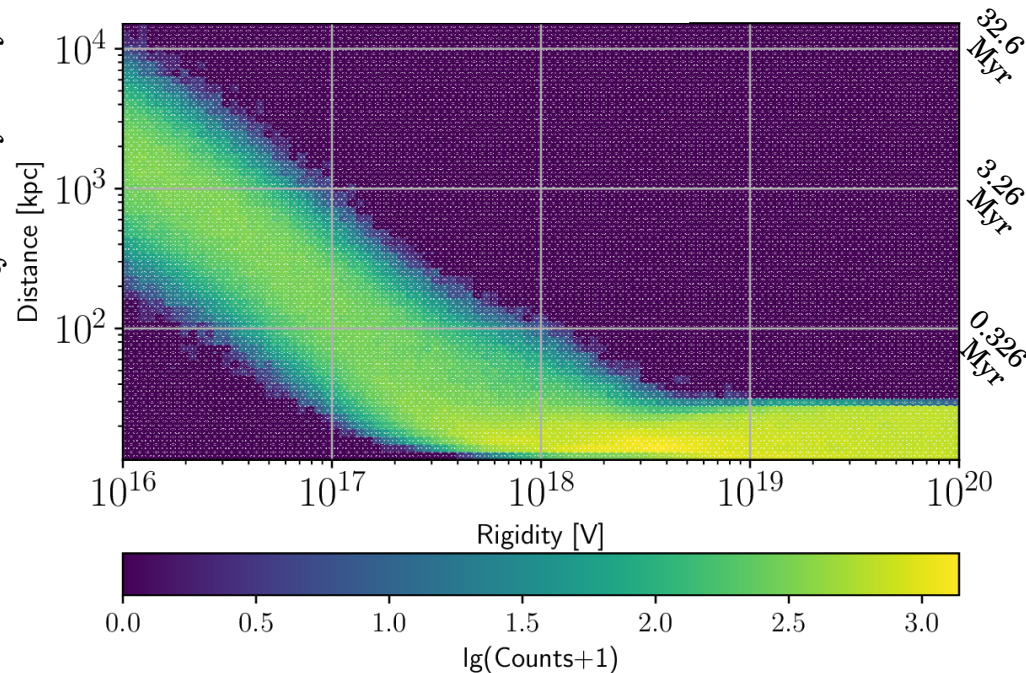
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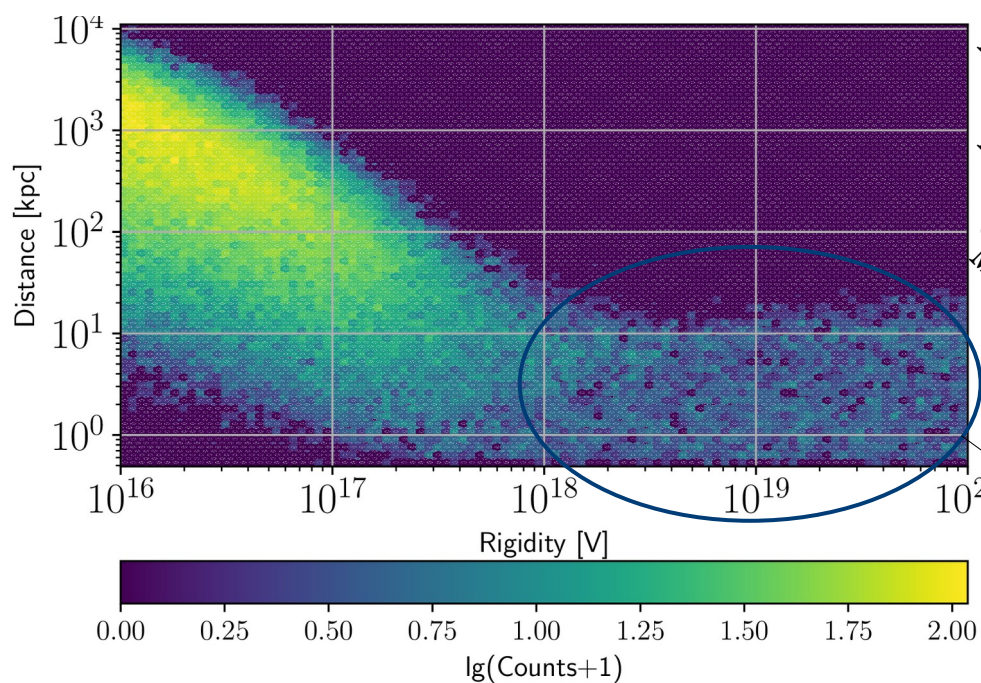


Propagation time increases below rigidities of a few EV.

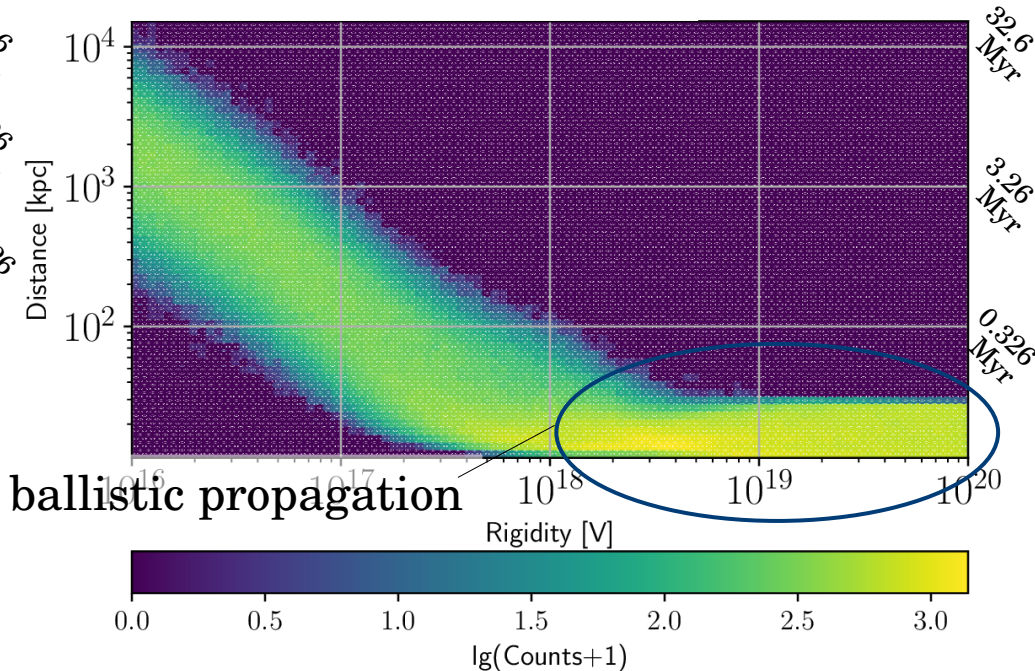


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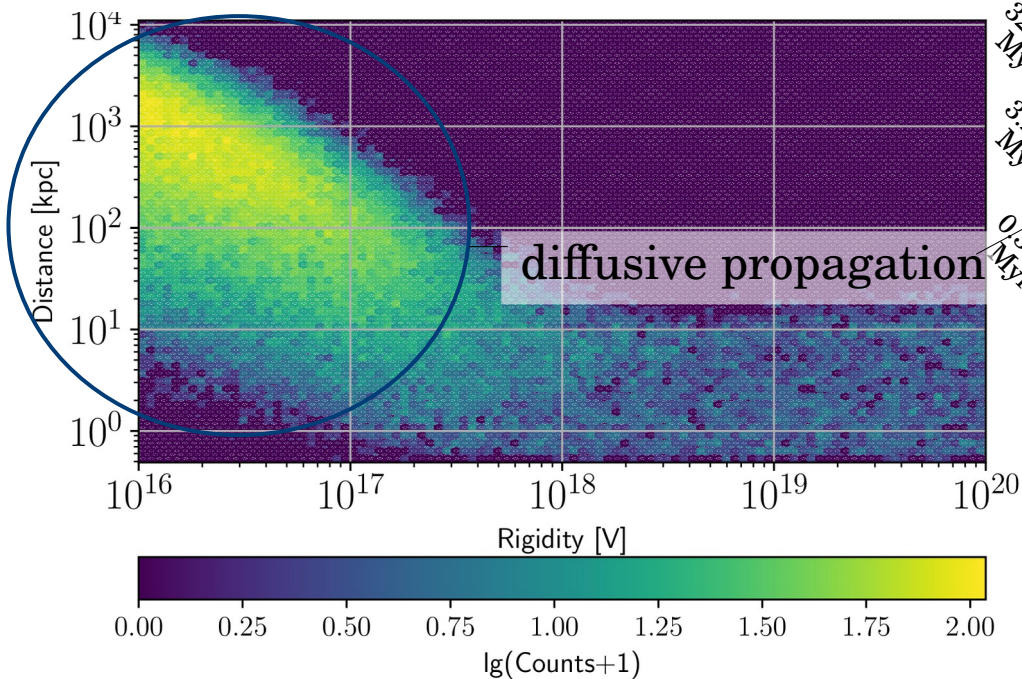
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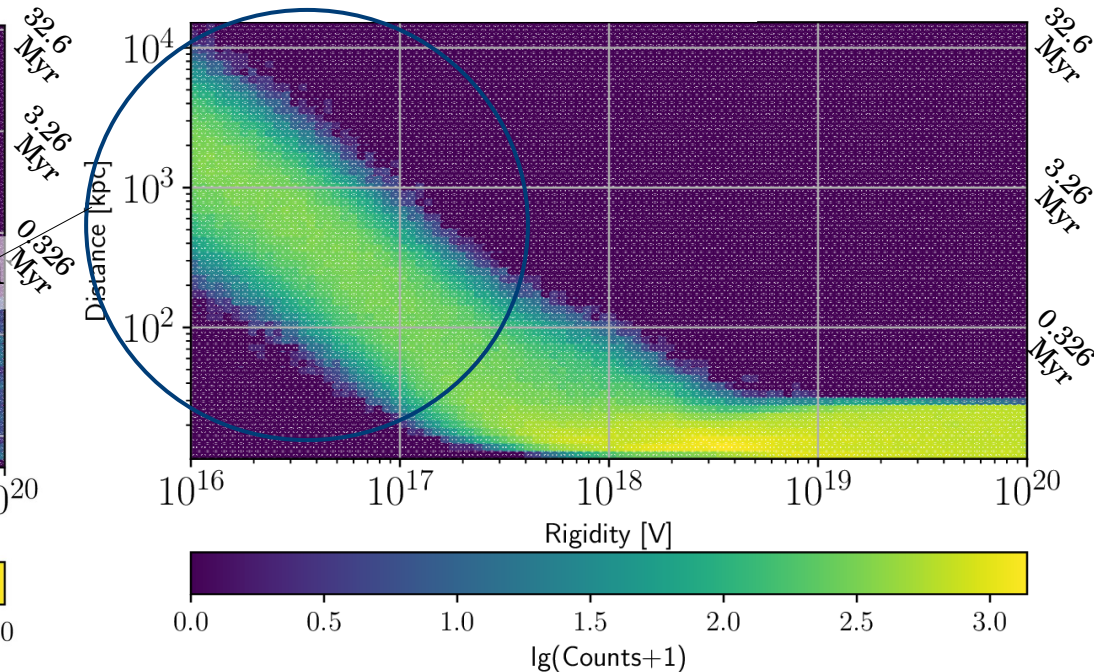
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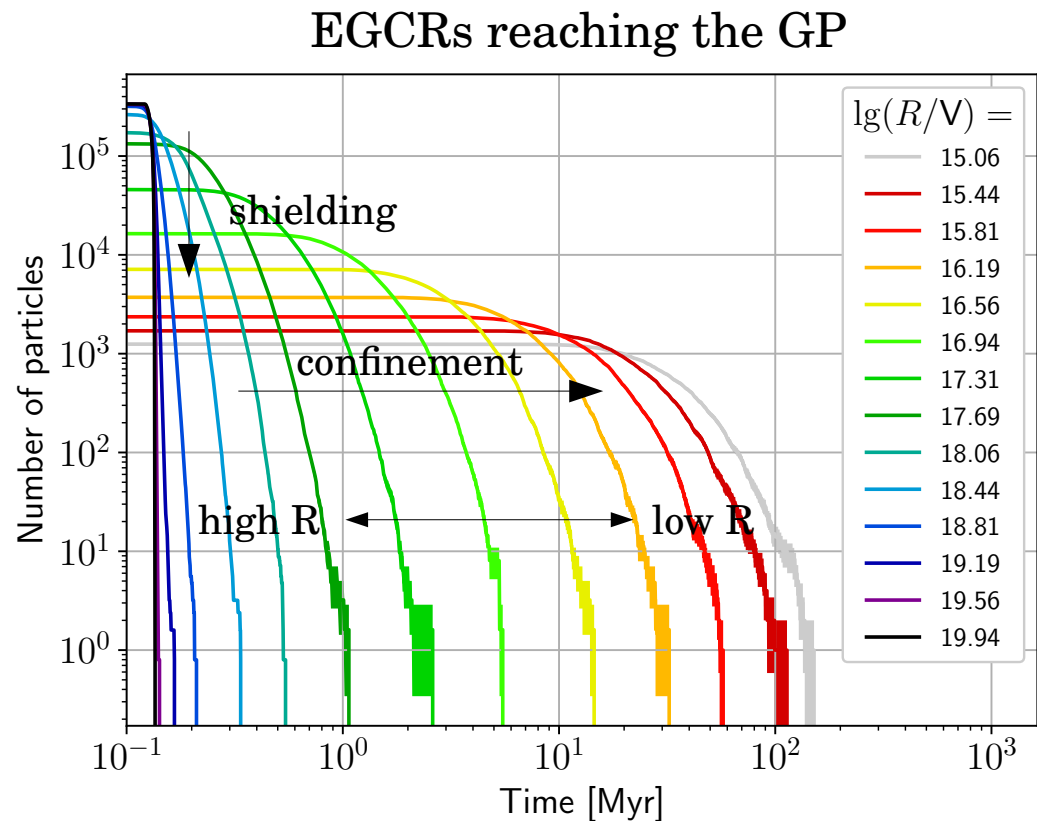
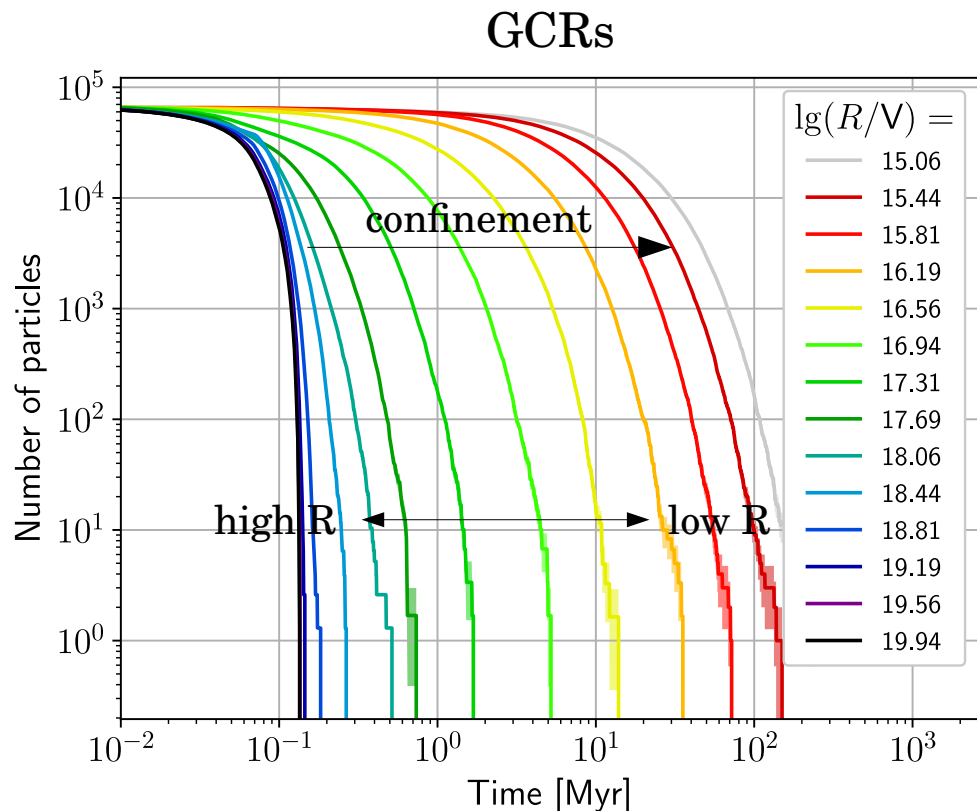
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Propagation time increases below rigidities of a few 1 EV.



# Propagation effects: Galactic residence time

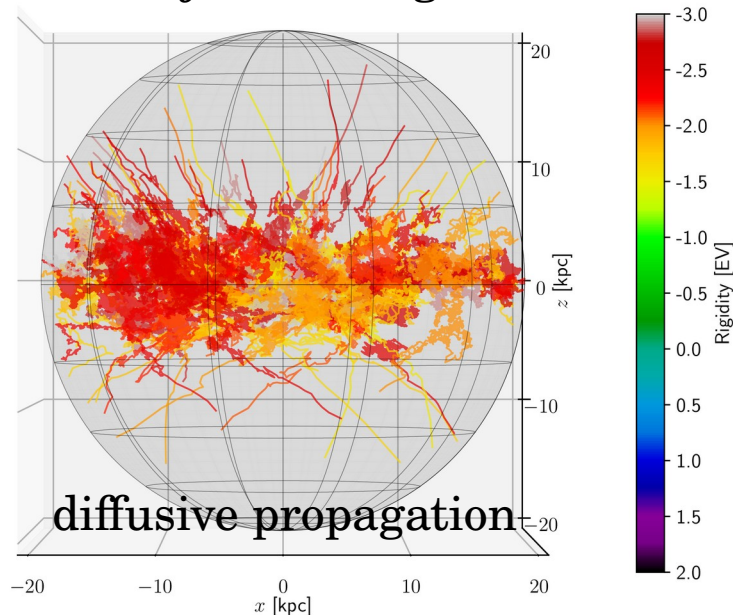


**NOTE:** Lowest-rigidity particles have residence times up to 100 Myr.



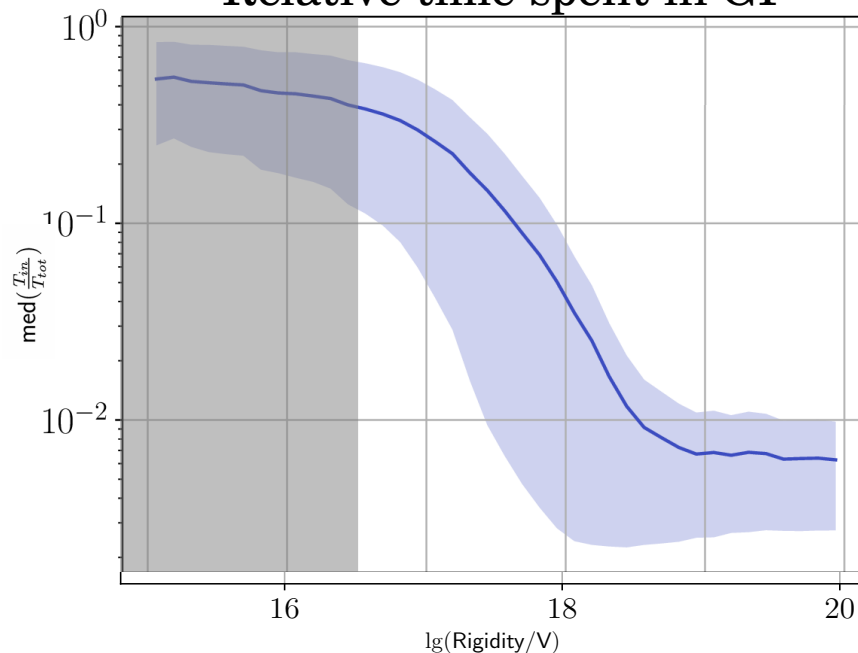
# Propagation effects: GCRs – Confinement in GP

Galactic trajectories ( $\lg(R/V) = 15 - 16.5$ )



**Decreasing confinement in GP with rigidity.**

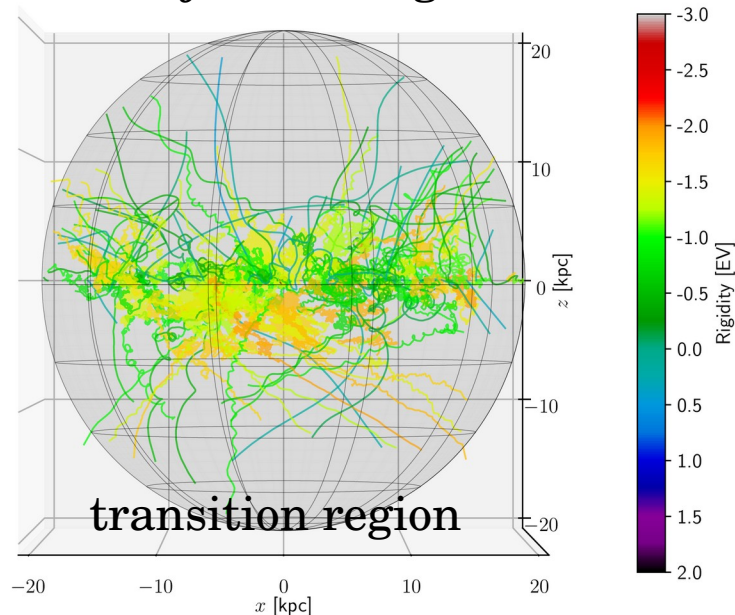
Relative time spent in GP



Relative time spent in GP decreases with rigidity; **inflection point at a few EV.**

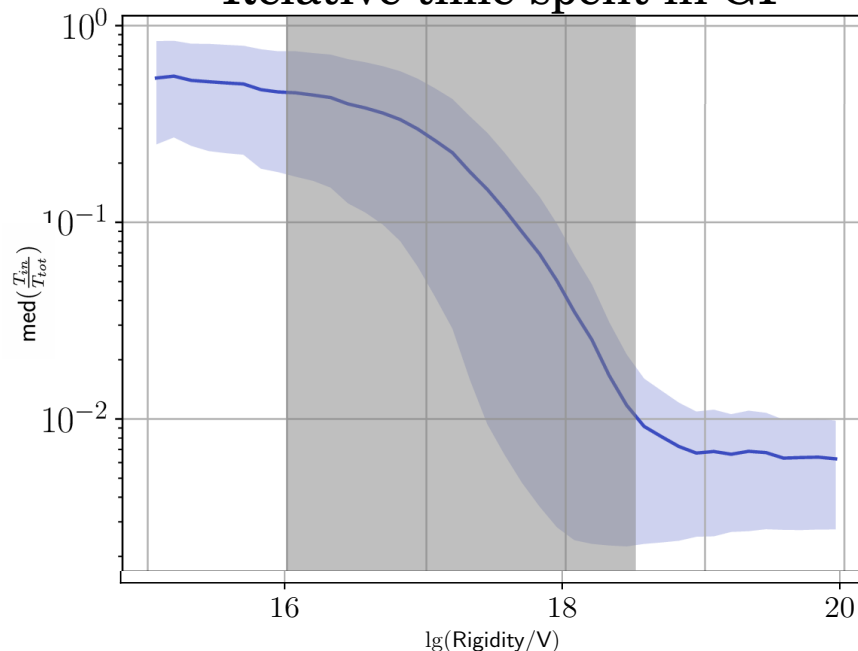
# Propagation effects: GCRs – Confinement in GP

Galactic trajectories ( $\lg(R/V) = 16 - 18.5$ )



**Decreasing confinement in GP with rigidity.**

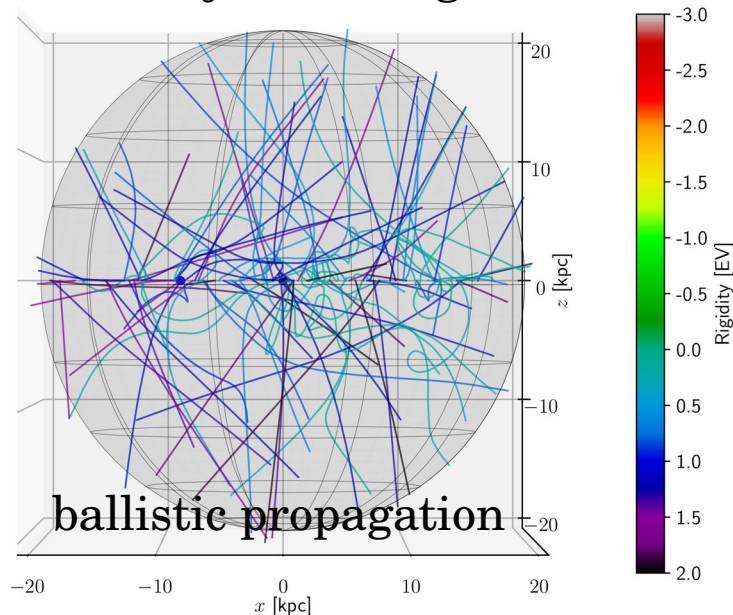
Relative time spent in GP



Relative time spent in GP decreases with rigidity; **inflection point at a few EV.**

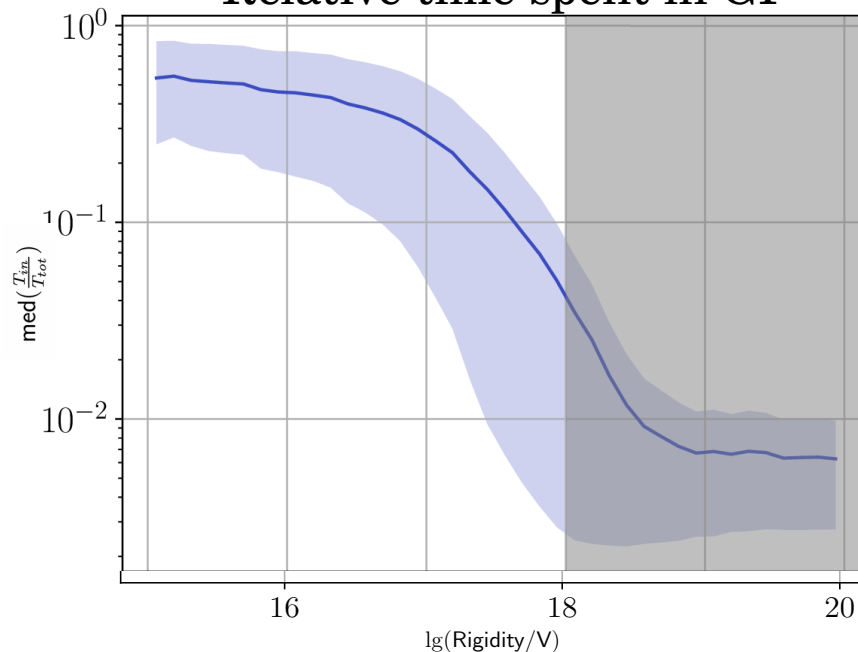
# Propagation effects: GCRs – Confinement in GP

Galactic trajectories ( $\lg(R/V) = 18 - 20$ )



**Decreasing confinement in GP with rigidity.**

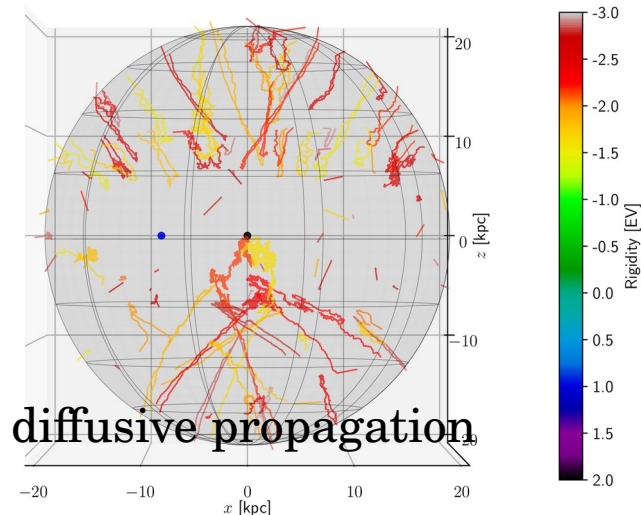
Relative time spent in GP



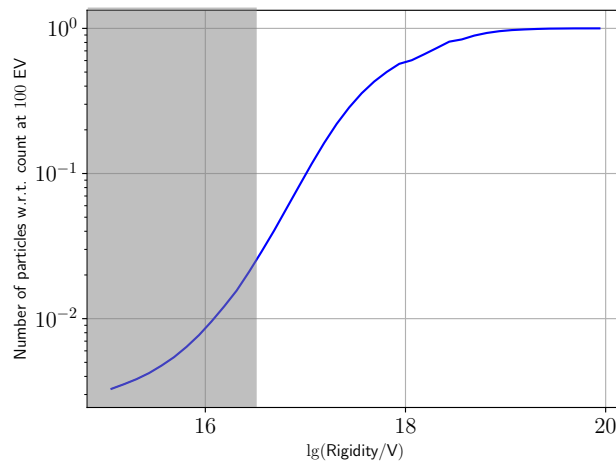
Relative time spent in GP decreases with rigidity; **inflection point at a few EV.**

# Propagation effects: EGCRs – Shielding from vs. confinement in GP

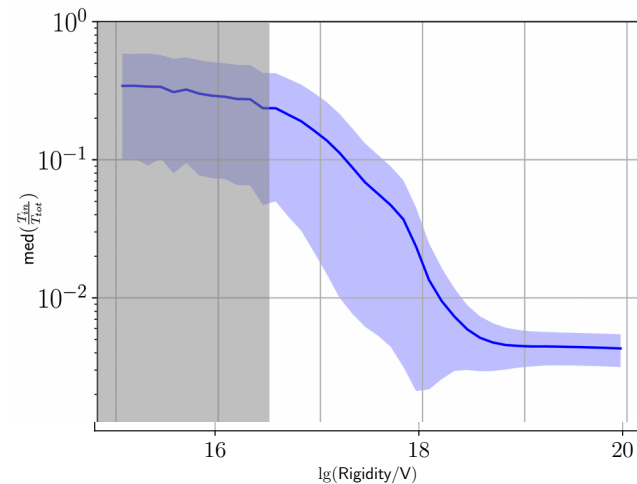
Galactic trajectories  
( $\lg(R/V) = 15 - 16.5$ )



CR count reaching GP



Relative time spent in GP



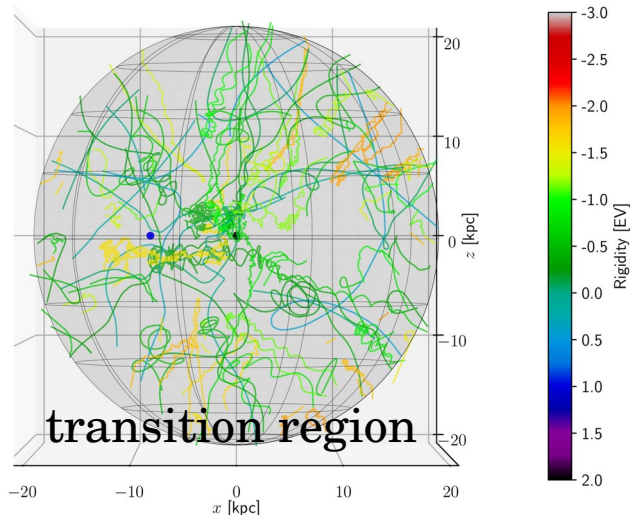
**Decreasing shielding  
from and confinement in  
GP with rigidity.**

**CR count decreases for  
smaller rigidities;  
inflection point at  
a few EV.**

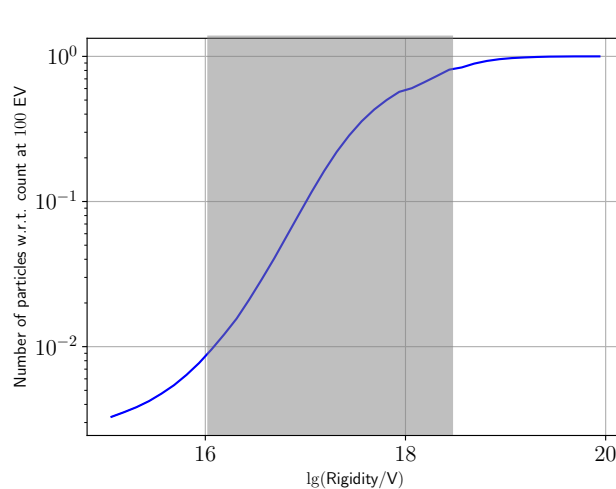
**Relative time spent in GP  
decreases with rigidity;  
inflection point at  
a few EV.**

# Propagation effects: EGCRs – Shielding from vs. confinement in GP

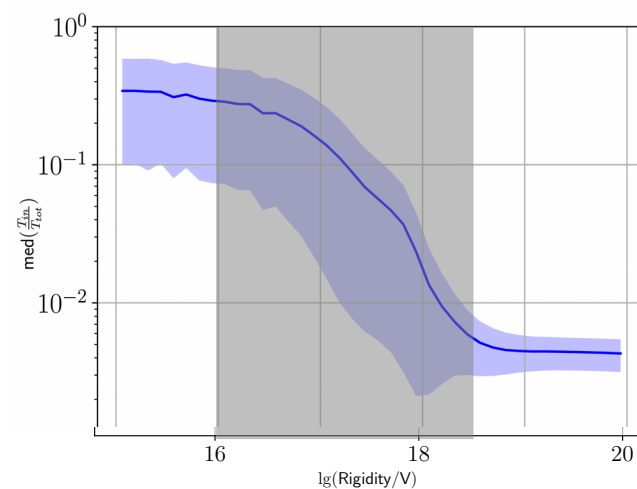
Galactic trajectories  
( $\lg(R/V) = 16 - 18.5$ )



CR count reaching GP



Relative time spent in GP



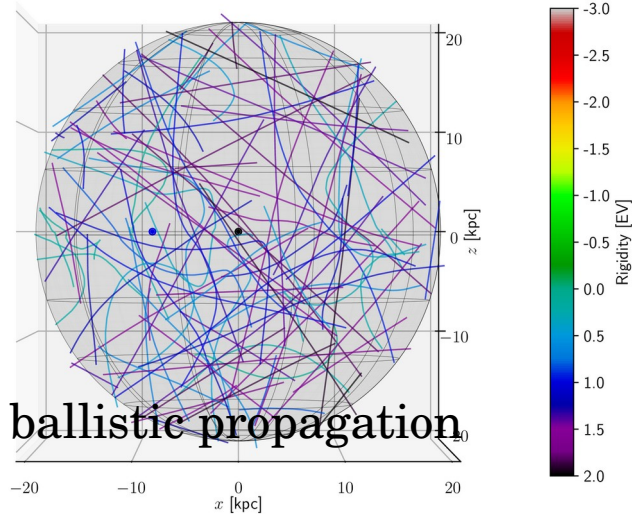
**Decreasing shielding  
from and confinement in  
GP with rigidity.**

**CR count decreases for  
smaller rigidities;  
inflection point at  
a few EV.**

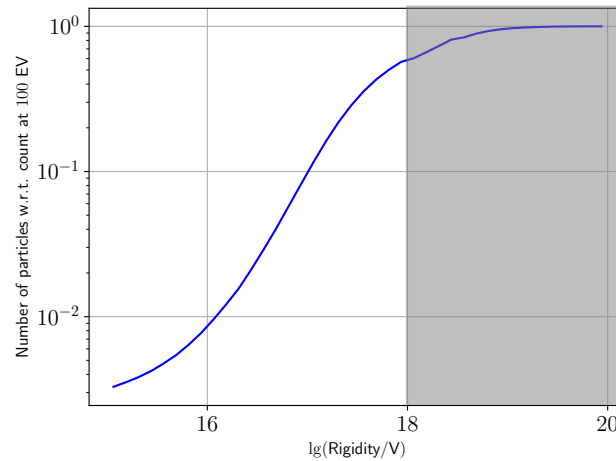
**Relative time spent in GP  
decreases with rigidity;  
inflection point at  
a few EV.**

# Propagation effects: EGCRs – Shielding from vs. confinement in GP

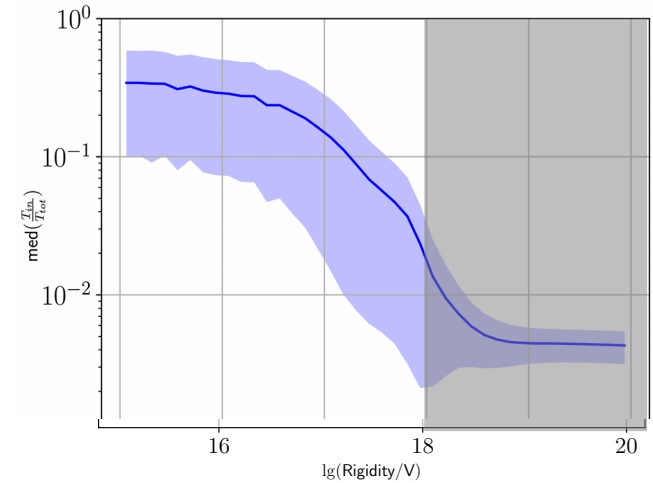
Galactic trajectories  
( $\lg(R/V) = 18 - 20$ )



CR count reaching GP



Relative time spent in GP



**Decreasing shielding  
from and confinement in  
GP with rigidity.**

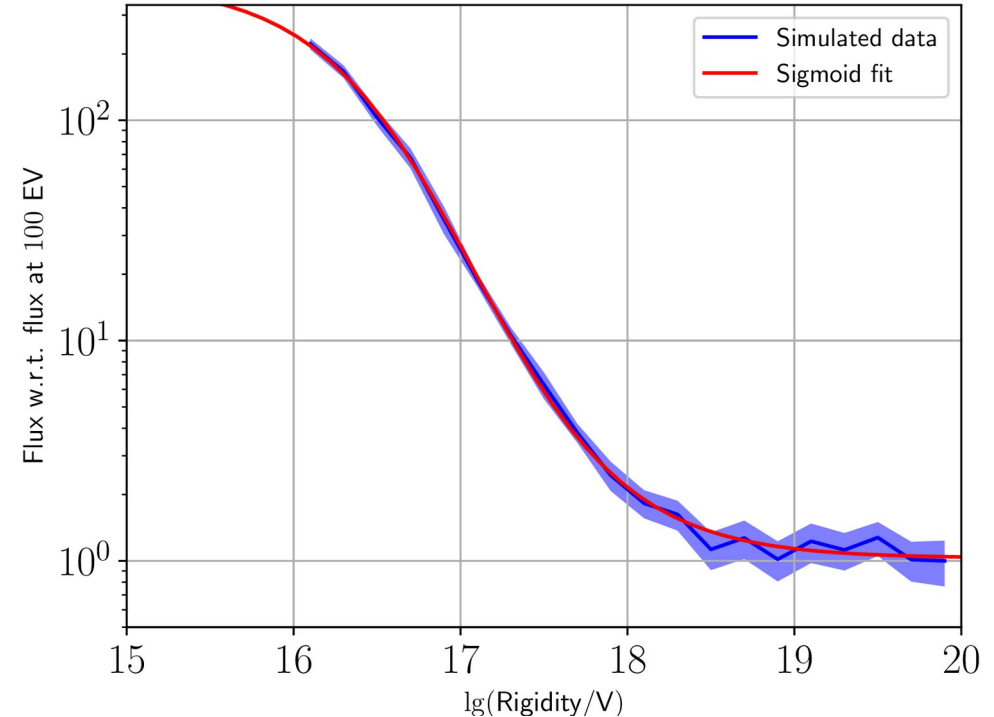
**CR count decreases for  
smaller rigidities;  
inflection point at  
a few EV.**

**Relative time spent in GP  
decreases with rigidity;  
inflection point at  
a few EV.**



# Effect on observables: GCRs – Flux suppression

Rigidity spectrum (sigmoid fit)



Decreasing confinement  
→ **flux reduction**

Mixed composition  
→ **heavier towards ‘ankle’**

Arrival direction distribution:  
**correlation with GP direction**  
above 0.1 EV

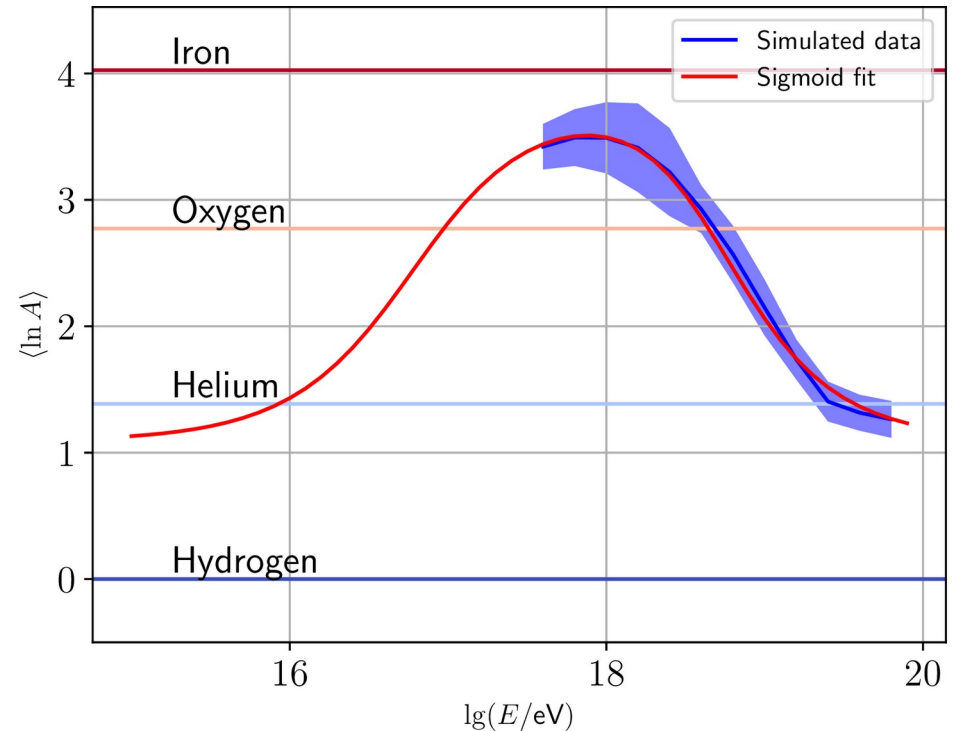
# Effect on observables: GCRs – Heavier composition

Mean logarithm of mass number (sigmoid fit)

Decreasing confinement  
→ **flux reduction**

Mixed composition  
→ **heavier towards ‘ankle’**

Arrival direction distribution:  
**correlation with GP direction**  
above 0.1 EV



**NOTE: Only propagation effects in GMF!**

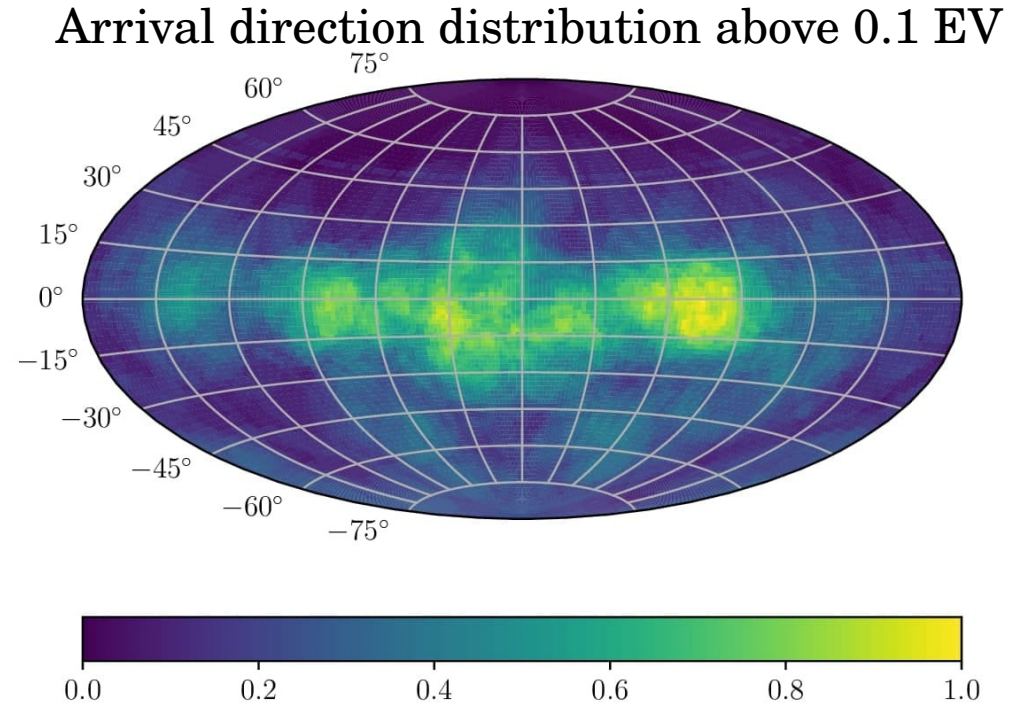


# Effect on observables: GCRs – Correlation with source direction (GP)

Decreasing confinement  
→ **flux reduction**

Mixed composition  
→ **heavier towards ‘ankle’**

Arrival direction distribution:  
**correlation with GP direction**  
above 0.1 EV



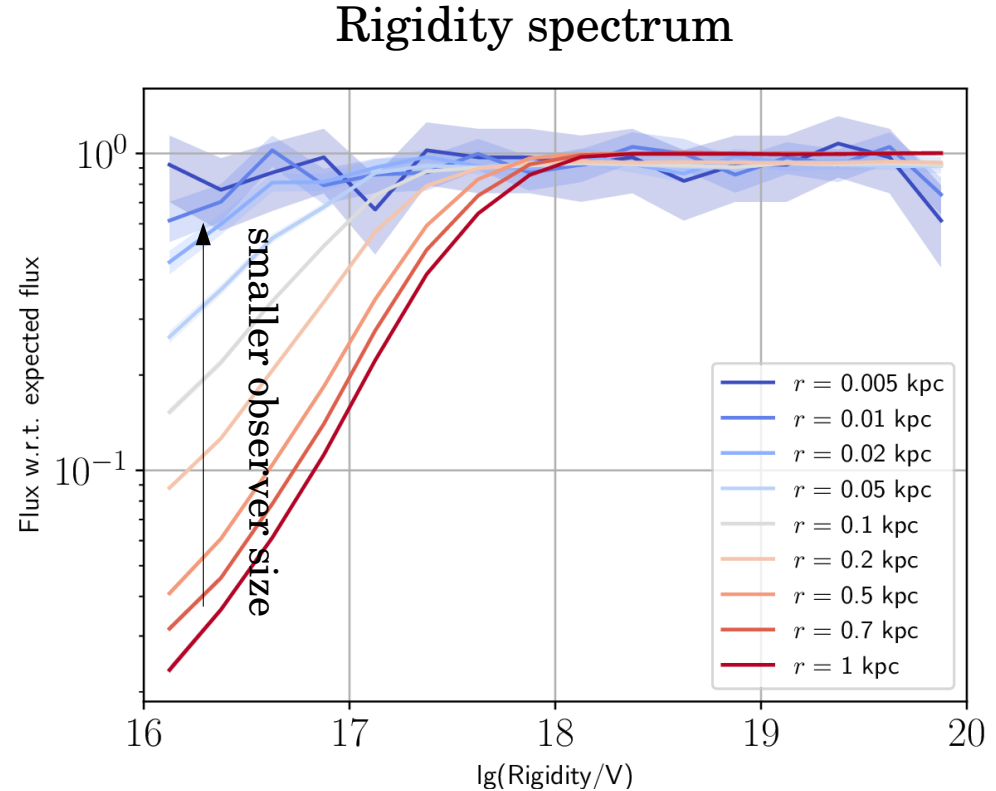
# Effect on observables: Isotropic EGCRs – Flux conservation

Apparent flux suppression for large observer sphere sizes; effect vanishes as  $r \rightarrow 0$ .

**Increased confinement in GP compensates increased shielding:**

**→ flux conservation**

Isotropic arrival direction



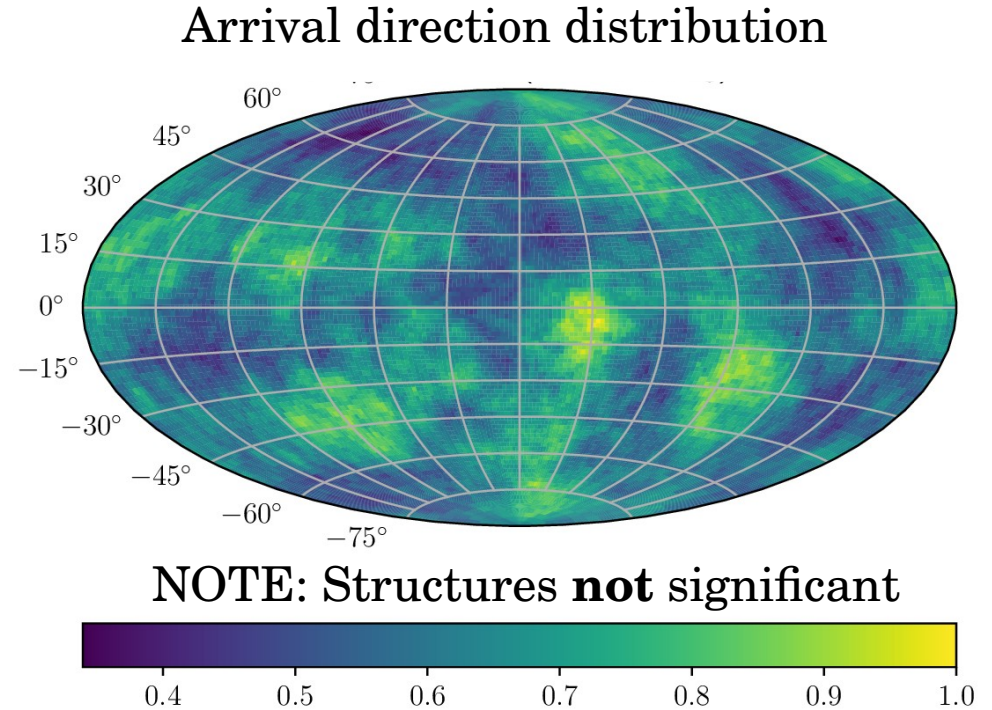
# Effect on observables: Isotropic EGCRs –Isotropic arrival direction

Apparent flux suppression for large observer sphere sizes; effect vanishes as  $r \rightarrow 0$ .

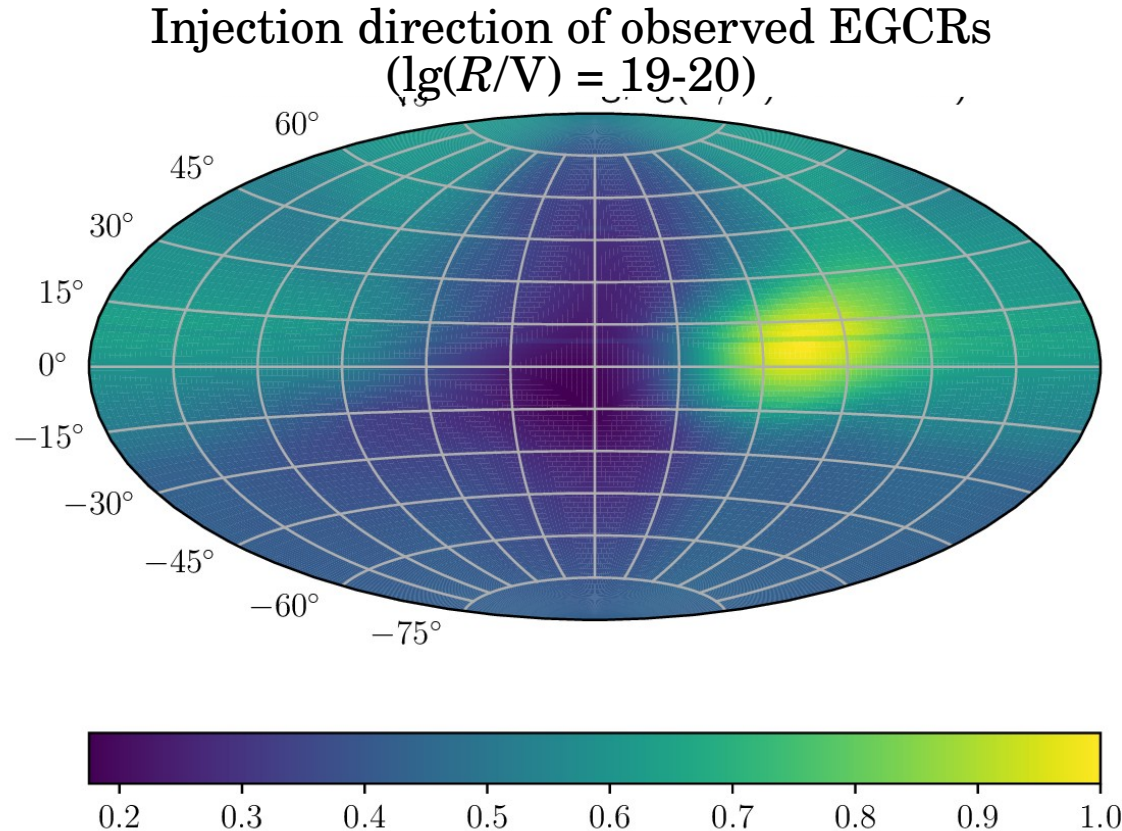
**Increased confinement in GP compensates increased shielding:**

→ **flux conservation**

**Isotropic arrival direction**



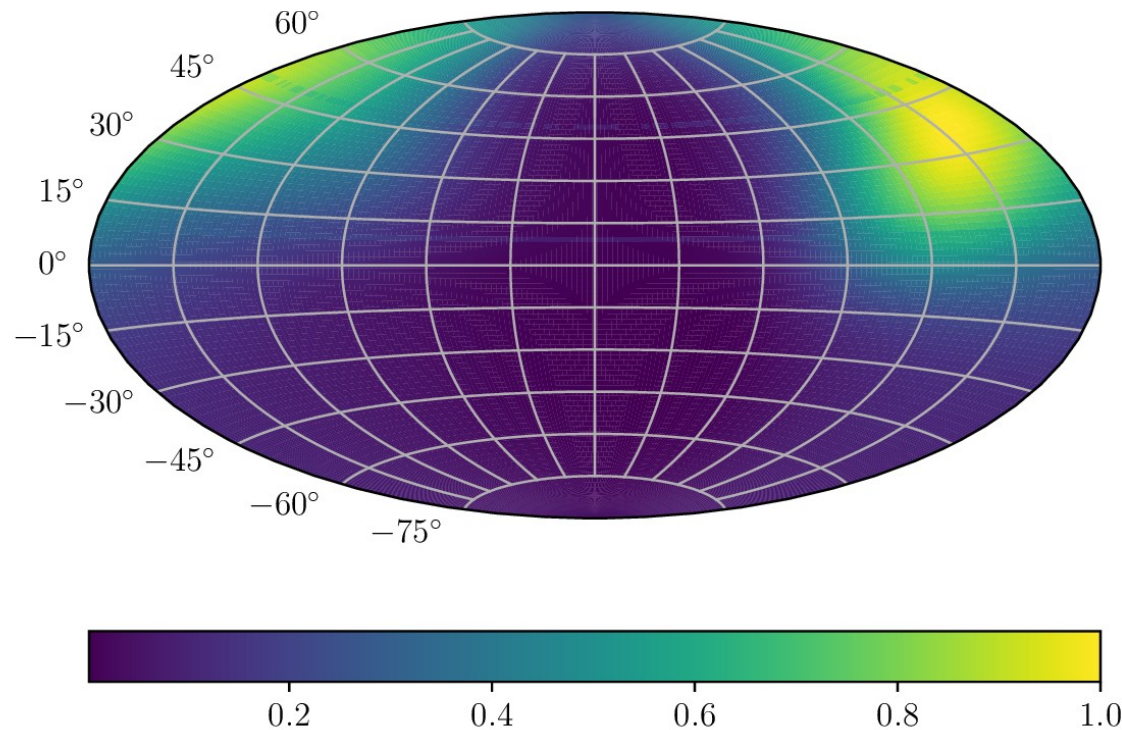
# Effect on observables: Anisotropic EGCRs – Opacity of Galaxy



- Regions of enhanced/suppressed transparency **shift with rigidity**

# Effect on observables: Anisotropic EGCRs – Opacity of Galaxy

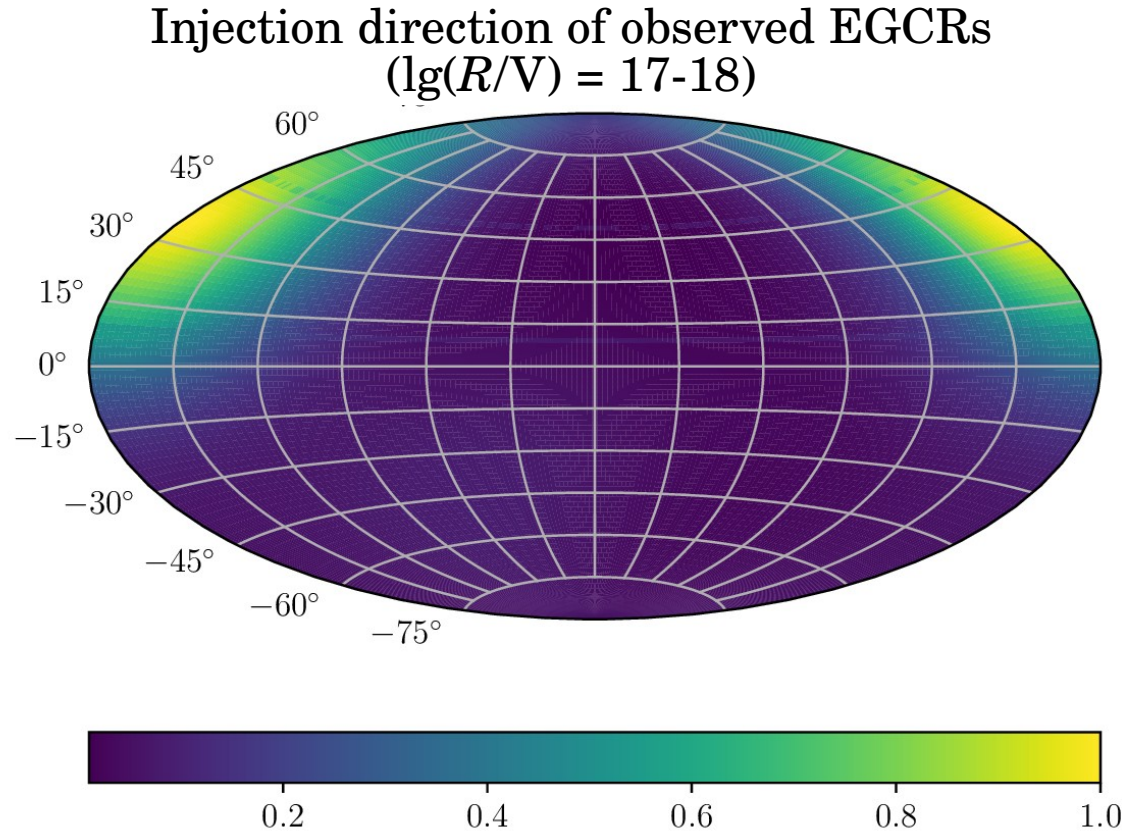
Injection direction of observed EGCRs  
( $\lg(R/V) = 18-19$ )



- Regions of enhanced/suppressed transparency **shift with rigidity**

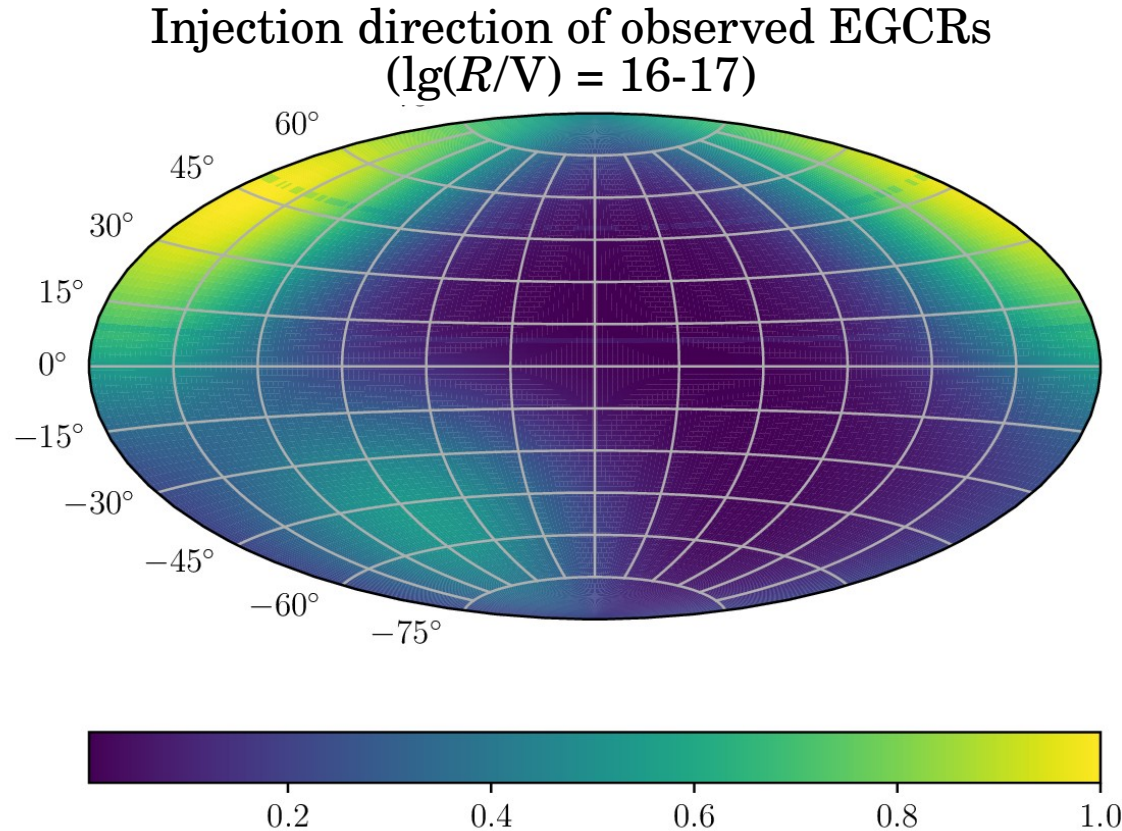


# Effect on observables: Anisotropic EGCRs – Opacity of Galaxy



- Regions of enhanced/suppressed transparency **shift with rigidity**

# Effect on observables: Anisotropic EGCRs – Opacity of Galaxy



- Regions of enhanced/suppressed transparency **shift with rigidity**

# Effect on observables: Anisotropic EGCRs – Galactic lensing

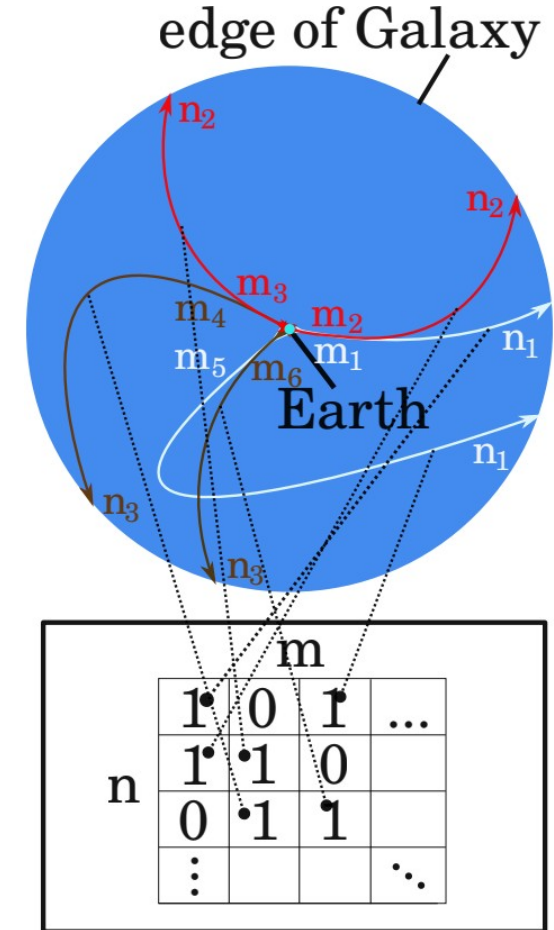
see also: [Astropart.Phys. 85 \(2016\) 54-64](#) for lensing scheme & [Eichmann, JCAP04\(2020\)047](#) for parallel work

Propagation in GMF can be quantified via lens

- distance of EG source to observer  $\gg$  size of Galaxy  
→ only injection **direction** relevant

Procedure:

- 1 **track  $N$  particles** between Earth and edge of Galaxy and **store injection direction** at edge and **arrival direction** at Earth
- 2 **discretise solid angle** range and **ascribe numbers  $n$  and  $m$**  to corresponding **injection and arrival directions**





# Effect on observables: Anisotropic EGCRs – Galactic lensing

see also: [Astropart.Phys. 85 \(2016\) 54-64](#) for lensing scheme & [Eichmann, JCAP04\(2020\)047](#) for parallel work

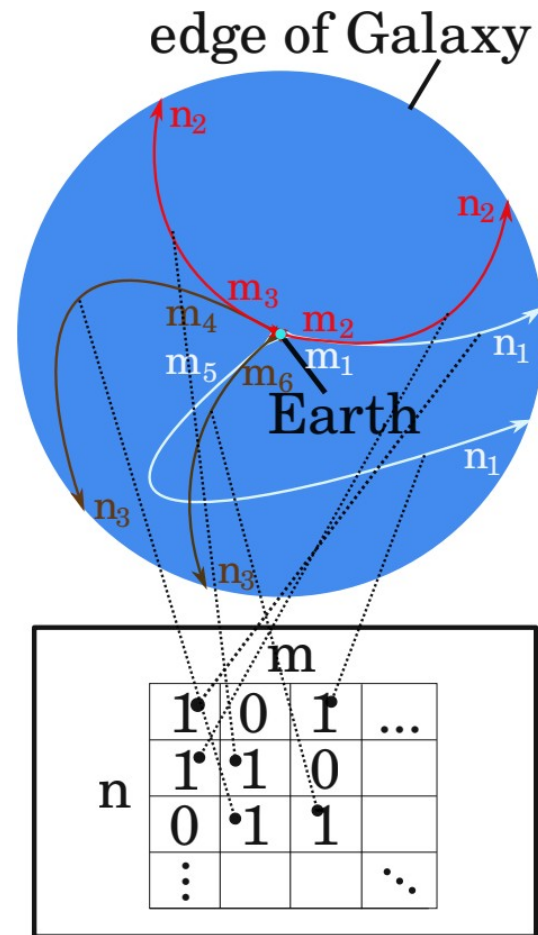
## 3 count occurrence $o$ of each injection/arrival direction pair $(n, m)$

- spans matrix  $L$  ( $l_{nm} = o$ )
- $L$  signifies **distribution of arrival directions**  $m$  at the observer point for each **injection direction**  $n$

## 4 matrix weighted by its 1-norm (= number of backtracked particles $N$ ) defines lens

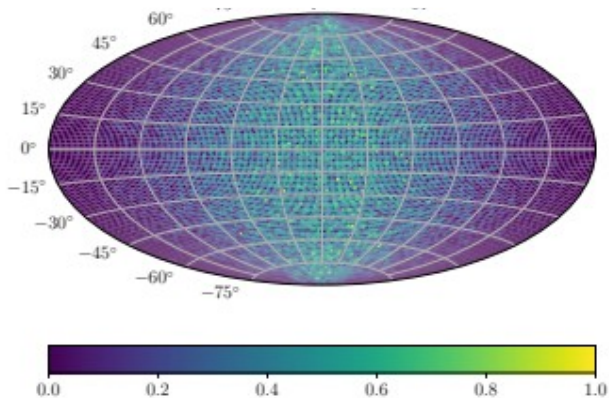
→ calculate arrival direction distribution for any injection direction distribution:

$$\vec{A} = \vec{I} \cdot \mathcal{L}$$



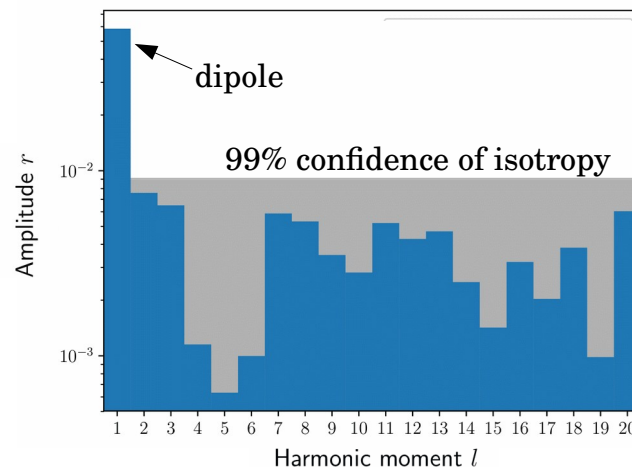
# Effect on observables: Anisotropic EGCRs – Galactic lensing

Injected flux



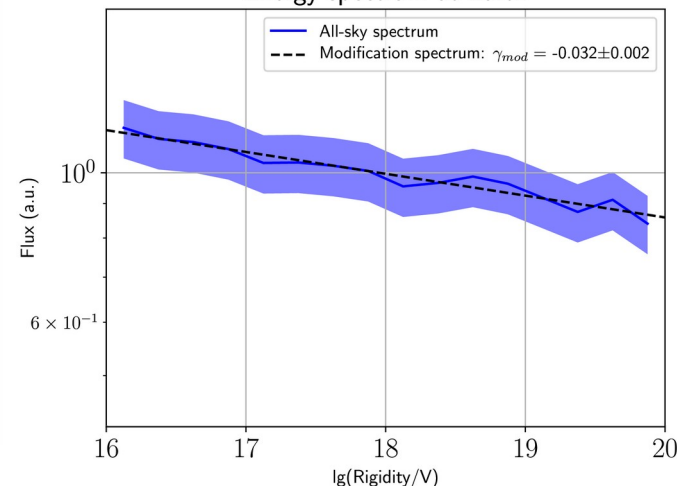
Injection direction  
distribution:  
**Pure dipole**

Distribution of moments above 1 EV



- surviving dipole in arrival direction distribution above 1 EV
- strong isotropisation by GMF at lower energies

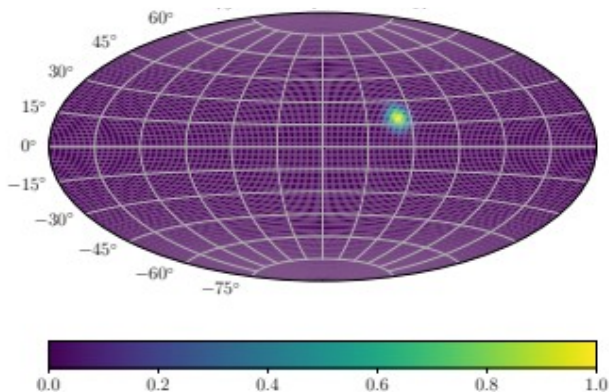
Flux at Earth  
Energy spectrum at Earth



Rigidity spectrum at  
Earth → **possible flux  
modification**

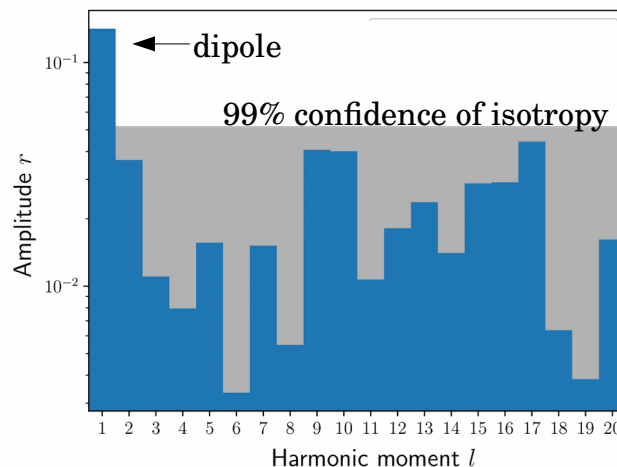
# Effect on observables: Anisotropic EGCRs – Galactic lensing

Injected flux



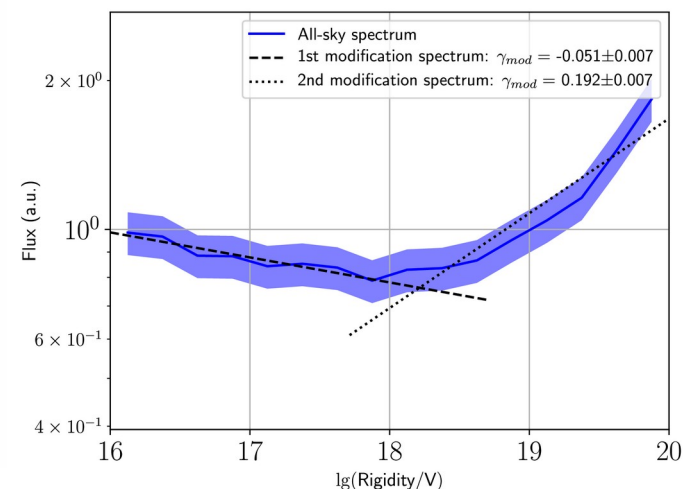
Injection direction distribution:  
**Pure single-point source (Cen A)**

Distribution of moments above 1 EV



- surviving dipole in arrival direction distribution above 1 EV
- strong isotropisation by GMF at lower energies

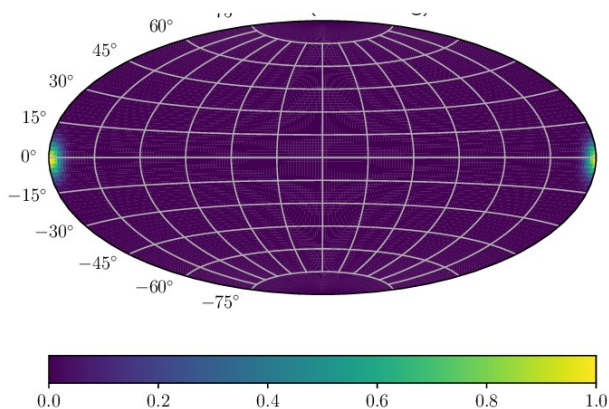
Flux at Earth



Rigidity spectrum at Earth → **possible flux modification**

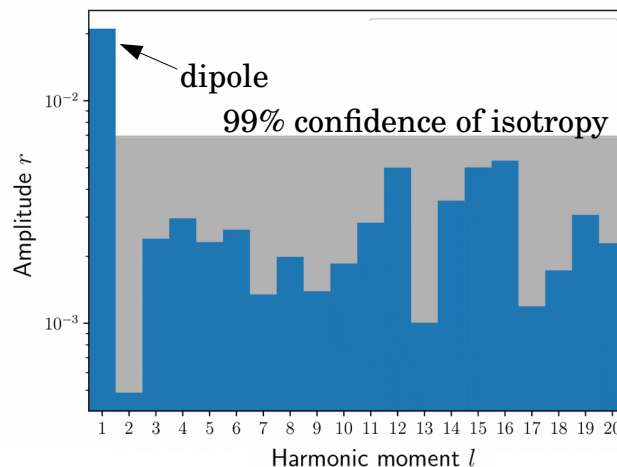
# Effect on observables: Anisotropic EGCRs – Galactic lensing

Injected flux



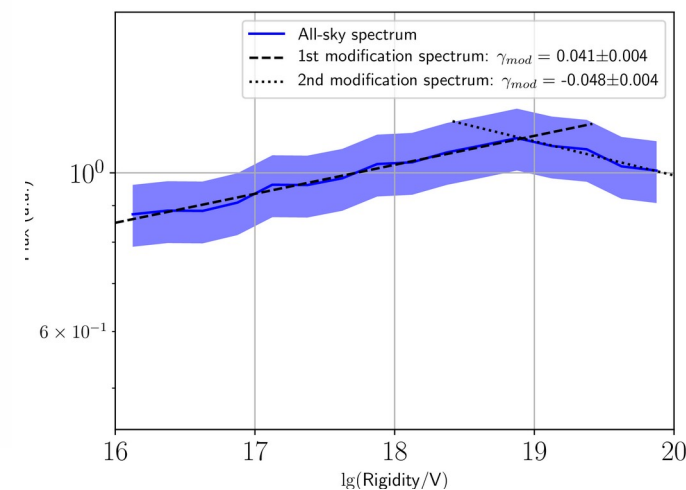
Injection direction distribution:  
**Pure single-point source** (Galactic anti-centre)

Distribution of moments above 1 EV



- surviving dipole in arrival direction distribution above 1 EV
- strong isotropisation by GMF at lower energies

Flux at Earth



Rigidity spectrum at Earth → **possible flux modification**

# Summary (1)

## Computational challenges:

- **change in propagation regimes**
  - **both propagation methods necessary**, ideally in self-consistent framework  
→ CRPropa 3
- **GMF poorly understood**
  - apply **multiple models**
  - improve measurements of observables and associated quality
  - use more input in model creation (see also IMAGINE project)

# Summary (2)

Propagation effects:

- Propagation in GMF for  $R = 10^{16-20}$  V: **change in propagation regimes from diffusive to ballistic**
- **Inflection point at a few EV** ( $r_g \sim$  width of GP) for all observed quantities

Effect on observables:

- GCRs:
  - **Flux suppression** towards higher rigidities; **heavier mixed composition** towards ‘ankle’
  - **Correlation with direction of GP** for rigidities above 0.1 EV
- EGCRs:
  - **Isotropic injection: No flux suppression and isotropic arrival direction**
  - **Anisotropic injection: Dipole and single point source  $\rightarrow$  arrival direction isotropic below 1 EV, possible flux modification**

# Summary (3)

Implications for transition:

- GCRs:
  - **Propagation in GMF** leads to ‘knee’-like feature
  - Significant contribution of **GCRs originating from GP disfavoured** at highest energies of ‘shin’ region
- EGCRs:
  - Part of ‘ankle’ may be a **propagation effect in GMF**

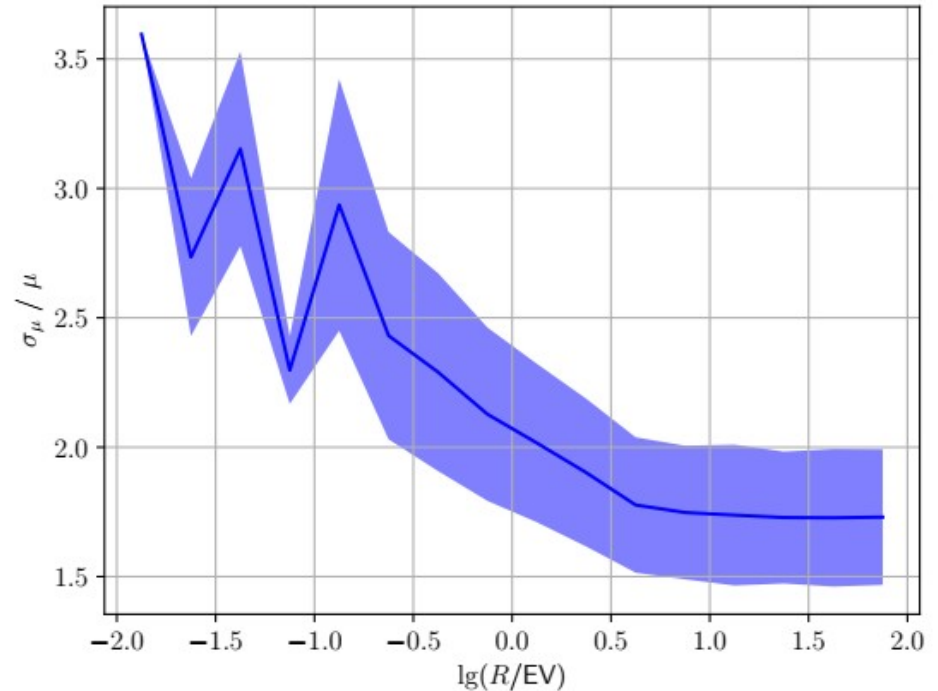


Thank you for your attention!

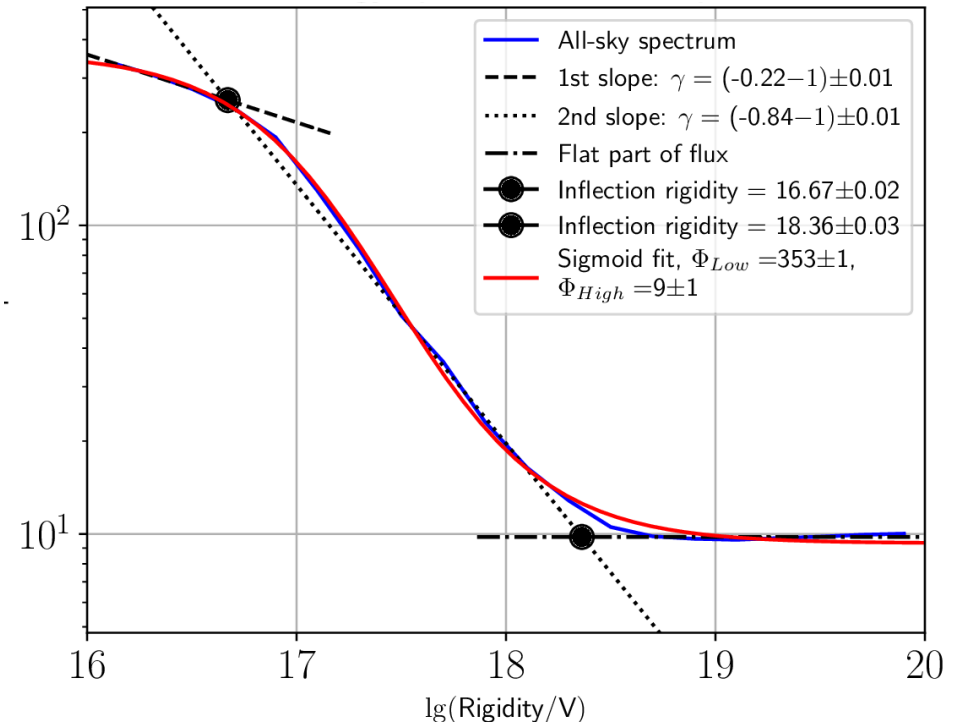
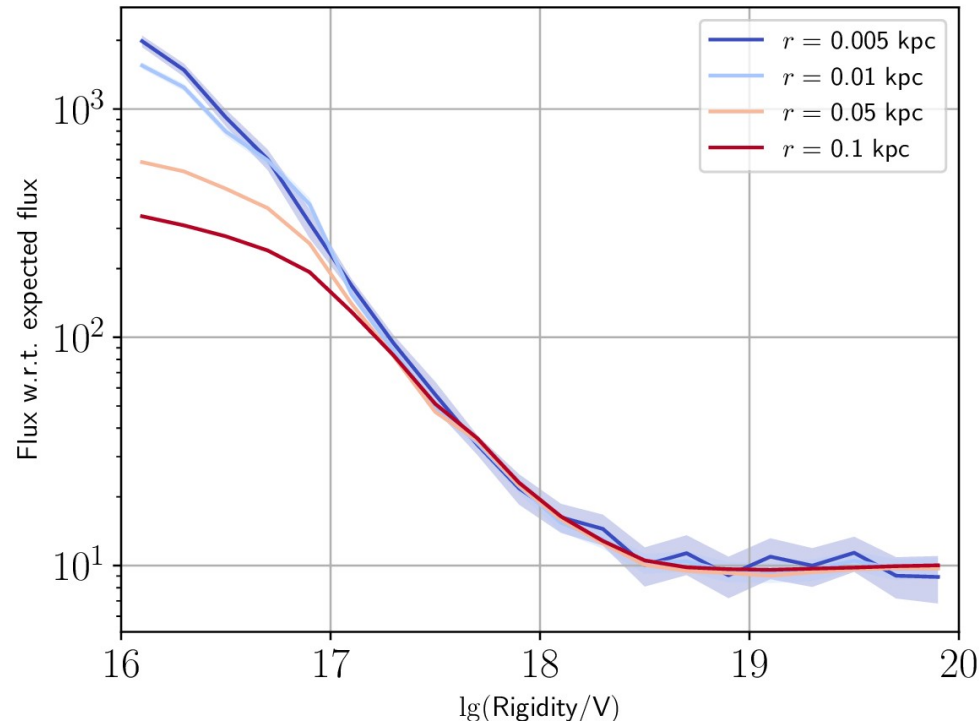
# Liouville's Theorem

- Objection to flux modification of EGCRs: **Liouville's Theorem**
  - If **phase space density is conserved, so is flux**
  - BUT: If Liouville holds, then **other quantities are conserved, i.a. first adiabatic invariant**  
~ classical magnetic moment (APJ 842:54, APJ 830:19):

$$\mu = \frac{e}{2m\pi c} \cdot I = \text{const.} \Rightarrow r_\mu = \frac{\sigma_\mu}{\langle \mu \rangle} \text{ small}$$

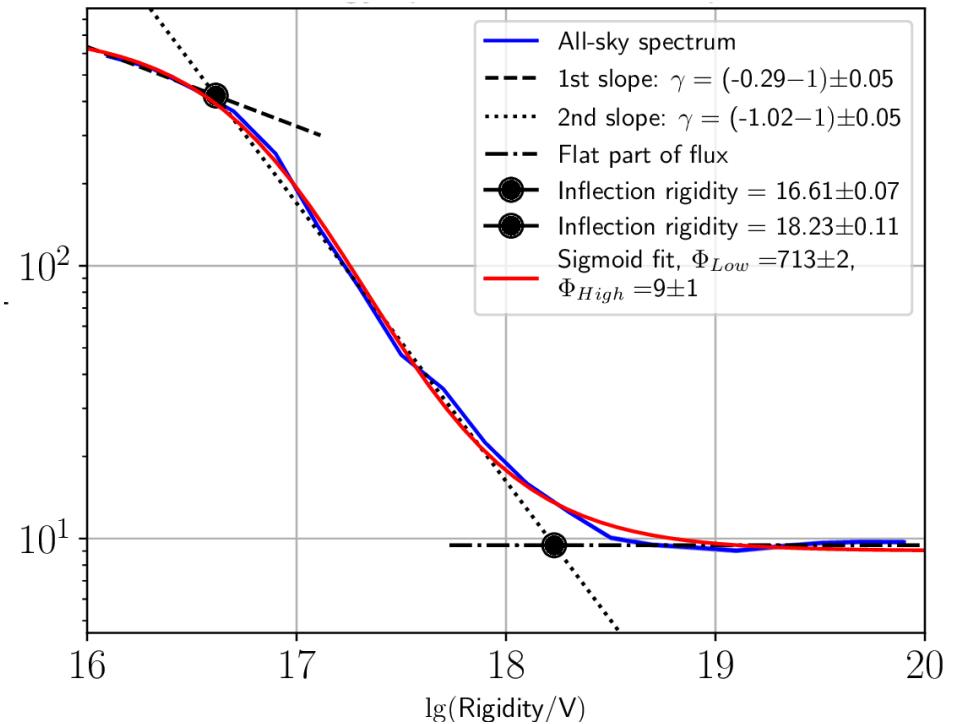
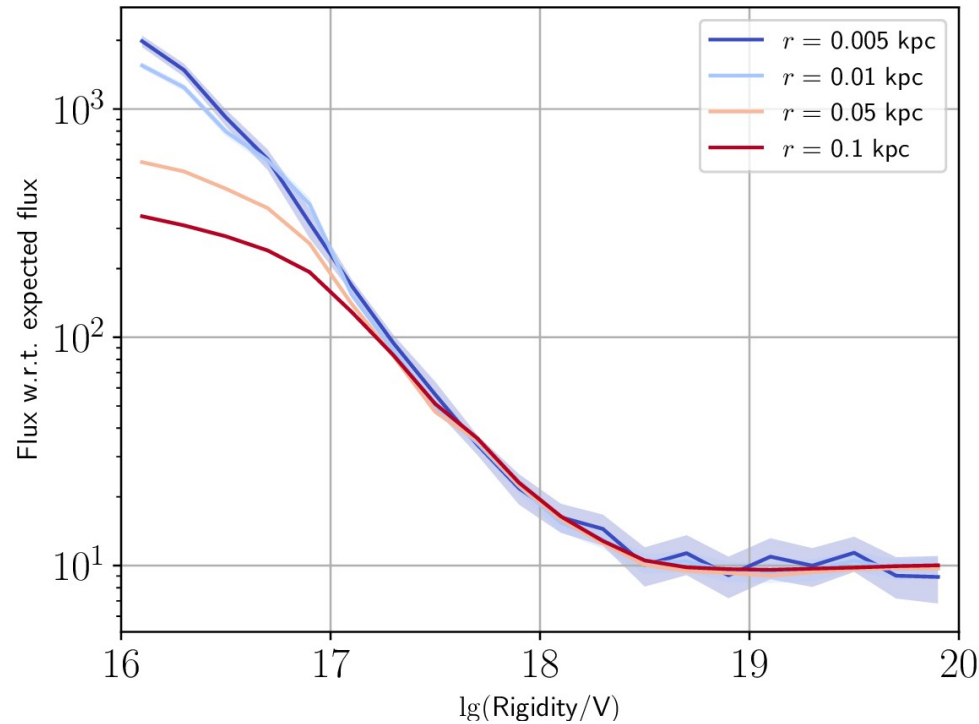


# GCRs – Sigmoid fit to flux



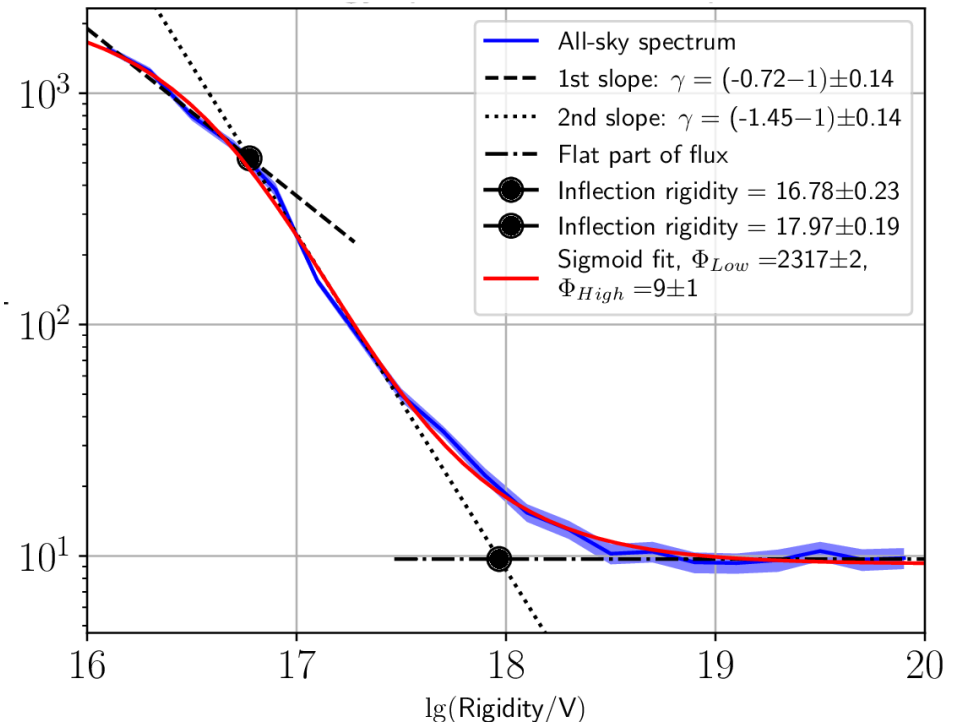
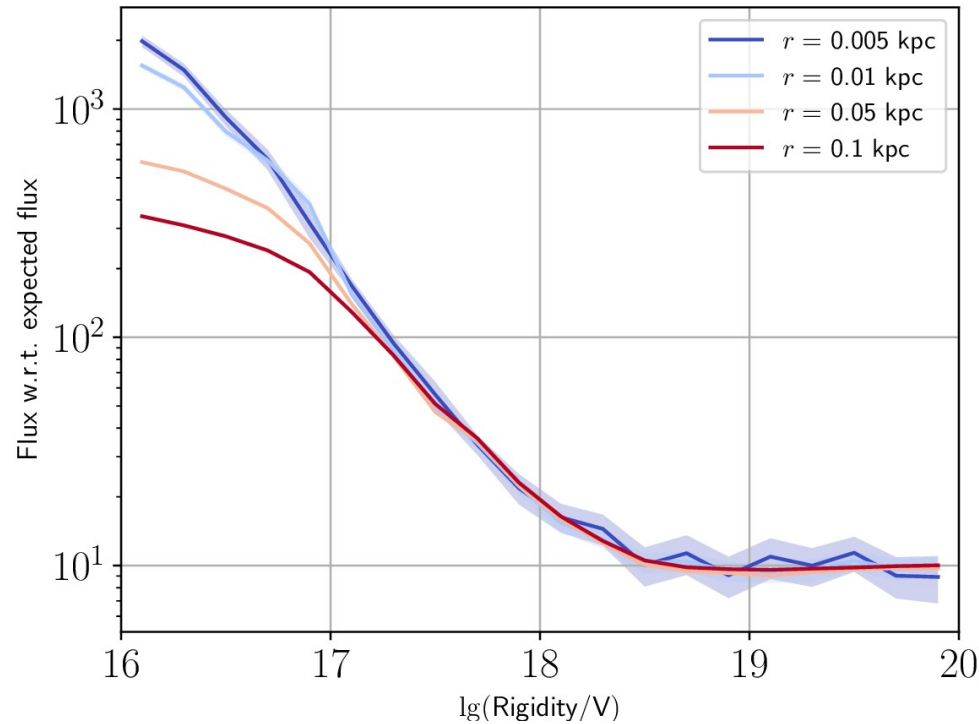
- Flux enhancement towards lower rigidities appears to flatten out  $\rightarrow$  sigmoid fit
- Advantage: wider overlapping energy range of mixed compositions

# GCRs – Sigmoid fit to flux



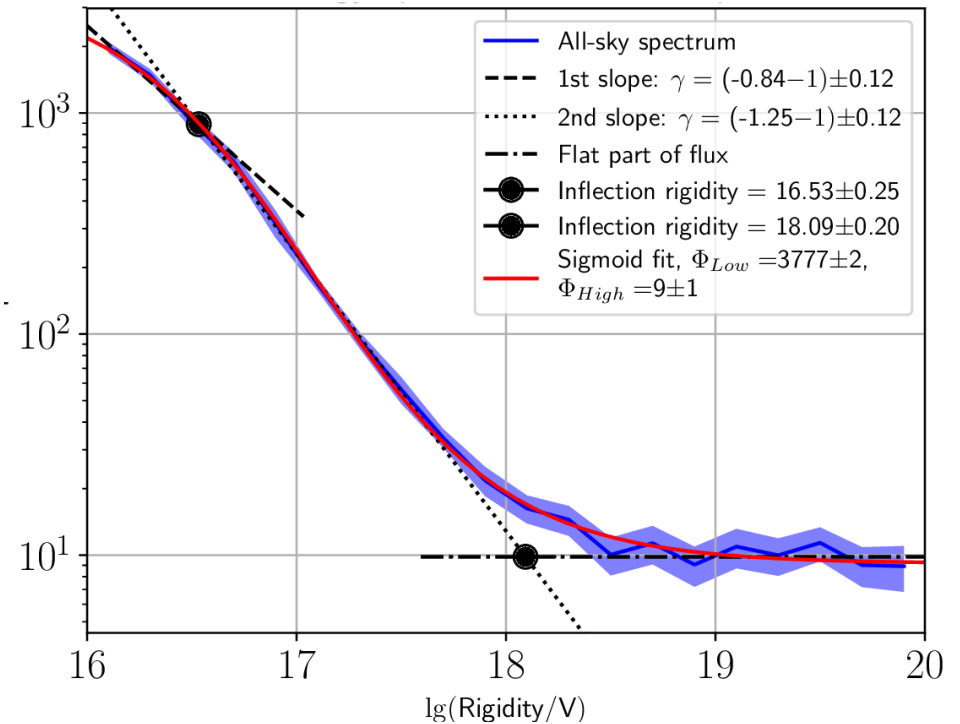
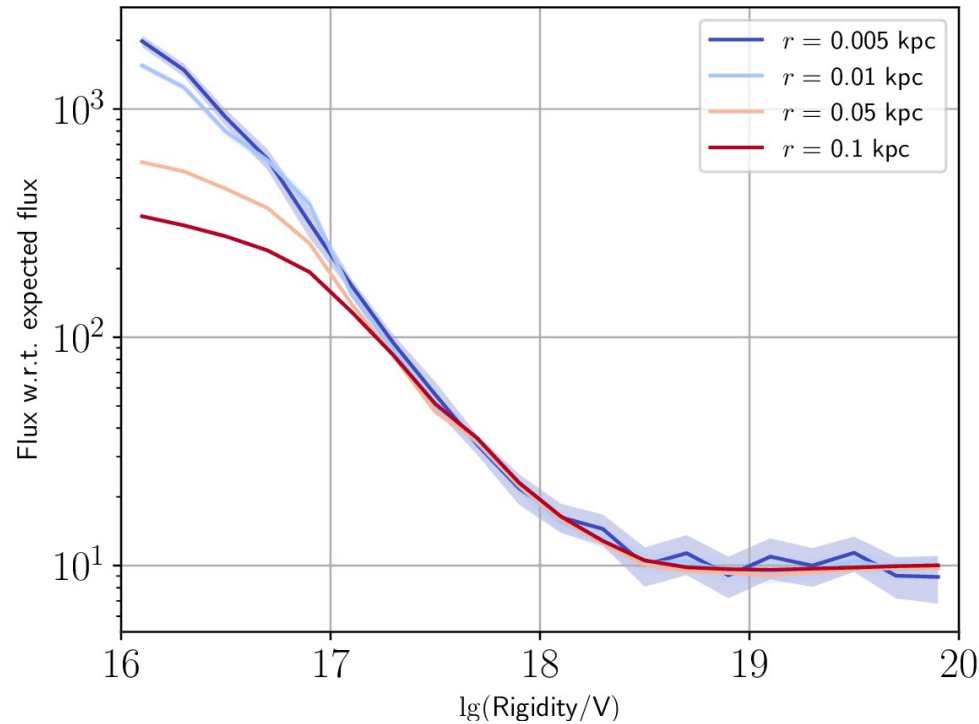
- Flux enhancement towards lower rigidities appears to flatten out  $\rightarrow$  sigmoid fit
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# GCRs – Sigmoid fit to flux



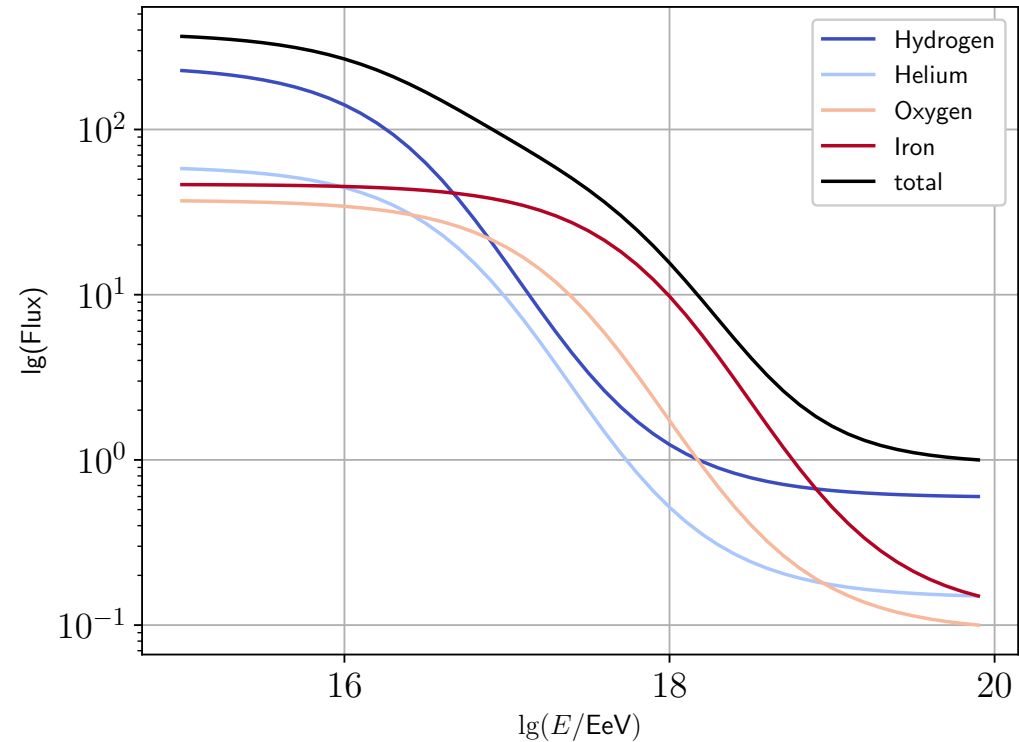
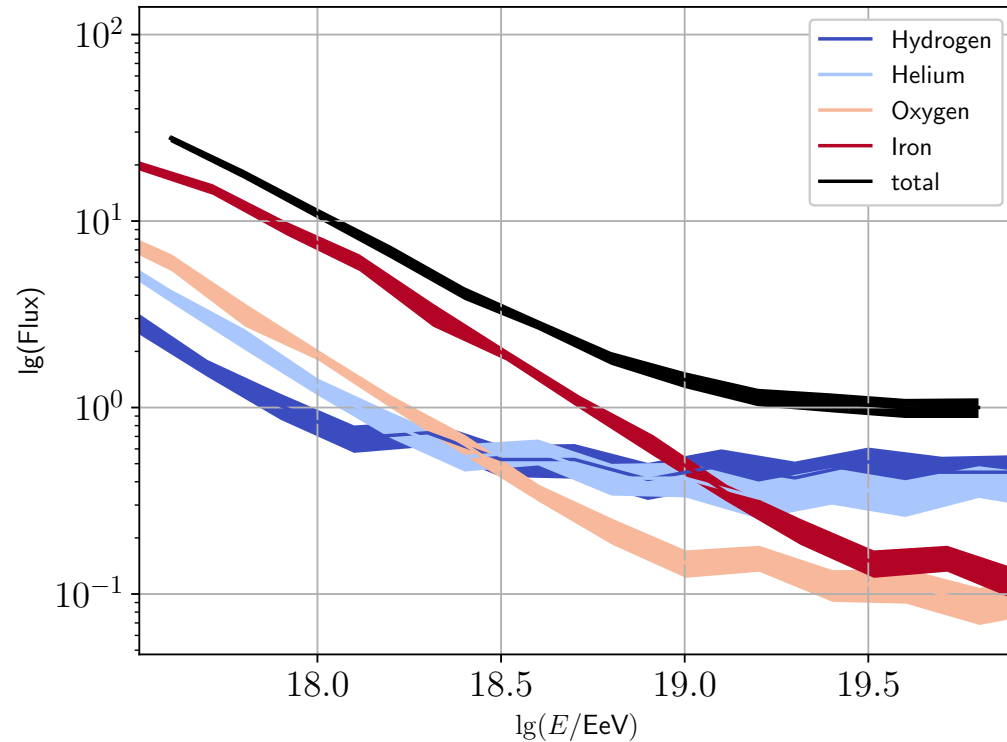
- Flux enhancement towards lower rigidities appears to flatten out  $\rightarrow$  sigmoid fit
- Advantage: wider overlapping energy range of mixed compositions

# GCRs – Sigmoid fit to flux



- Flux enhancement towards lower rigidities appears to flatten out  $\rightarrow$  sigmoid fit
- Advantage: wider overlapping energy range of mixed compositions

# GCRs – Total flux (data and sigmoid fit)

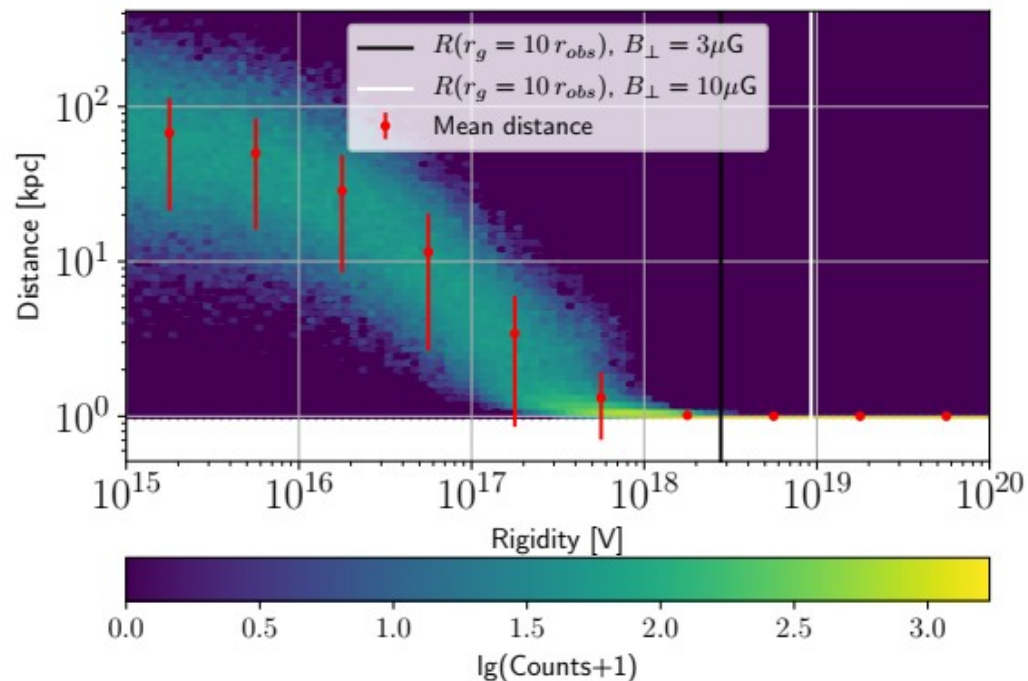


- Onset of flux suppression for mixed composition visible for sigmoid fit



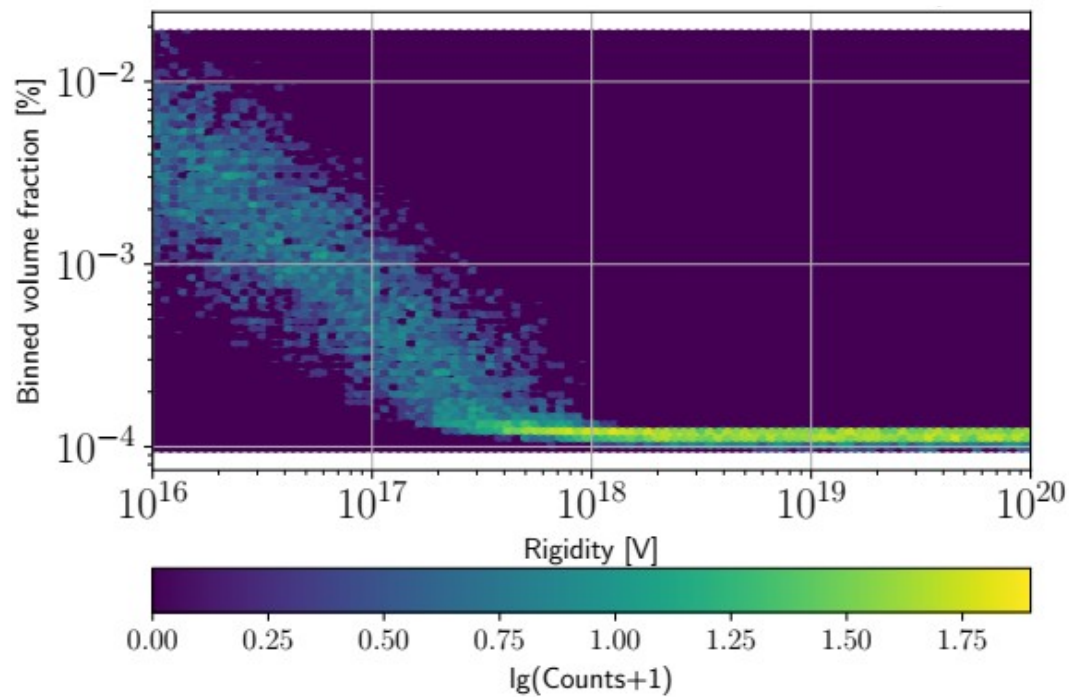
# On the modification of EGCR energy spectrum

- **Propagation time and fraction of space traversed increases to compensate shielding**



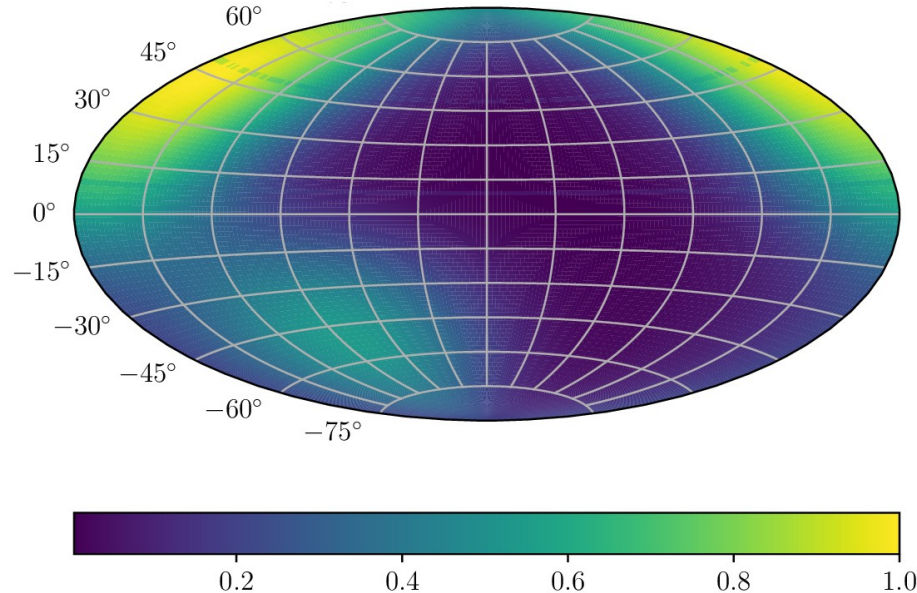
# On the modification of EGCR energy spectrum

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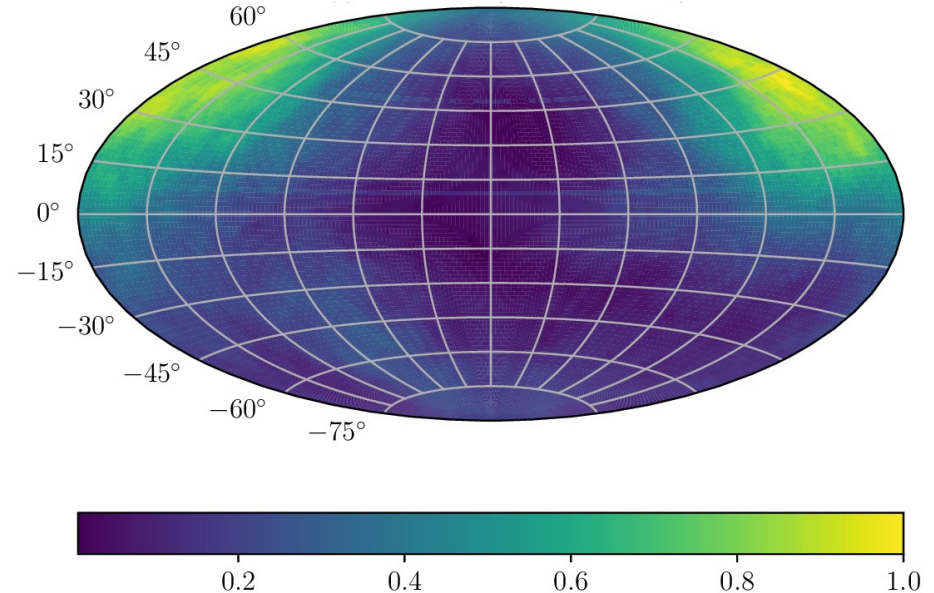


# Galactic lensing – time reversibility

Injection direction of observed EGCRs  
backtracking



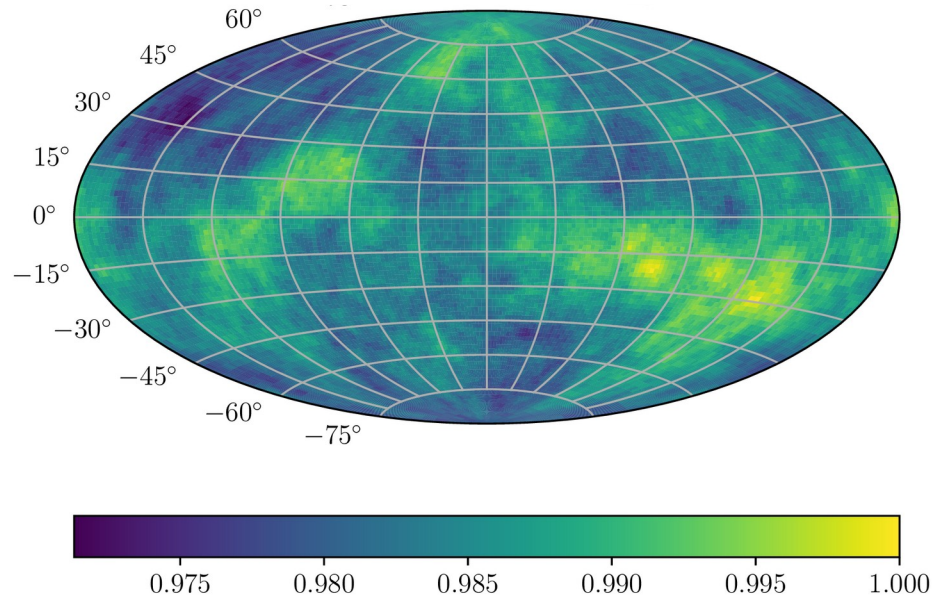
Injection direction of observed EGCRs  
forward tracking



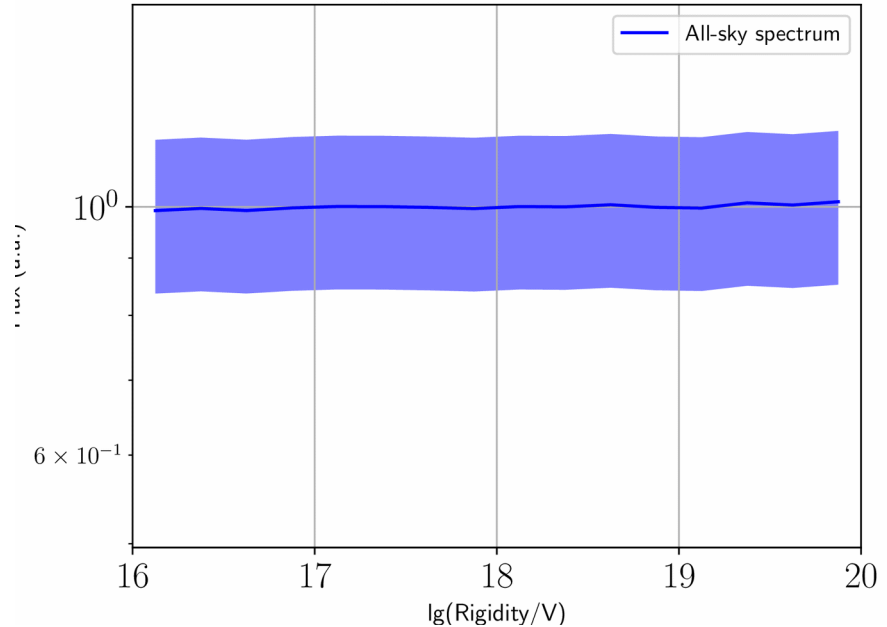
Injection direction distributions of backtracked and forward tracked protons match

# Galactic lensing – testing lens

Arrival direction of lensed isotropic injection distribution



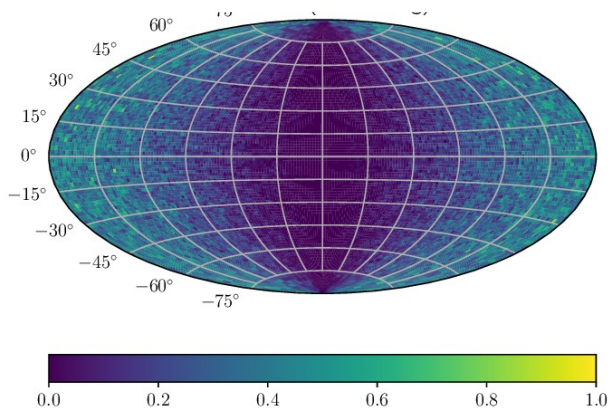
Spectrum of lensed isotropic injection distribution



Lensed arrival direction distribution and spectrum of isotropic injection distribution is as expected.

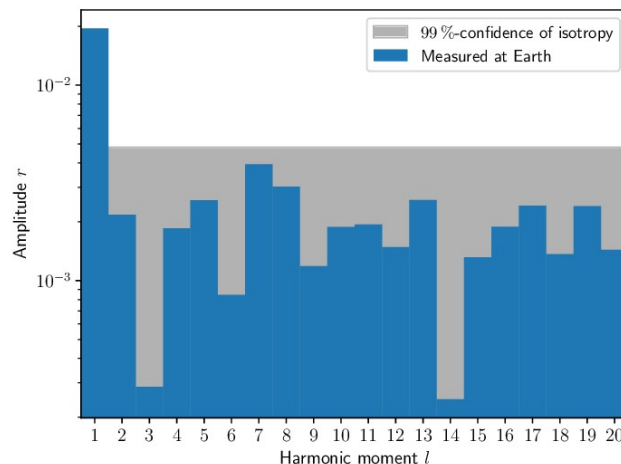
# Anisotropic EGCRs – Galactic lensing

Injected flux



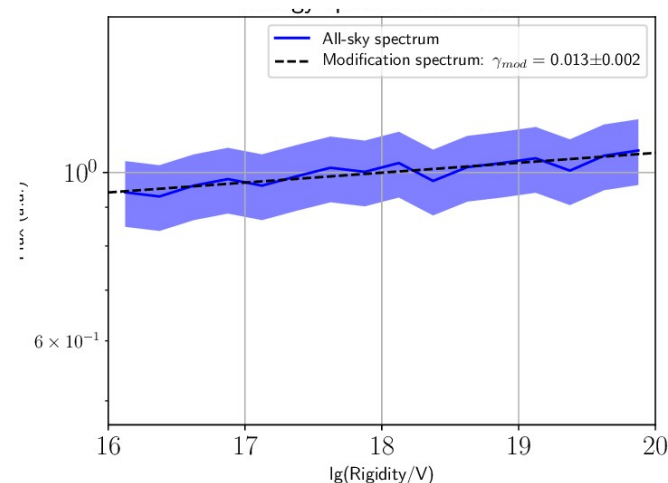
Injection direction  
distribution:  
**Pure dipole**

Distribution of moments above 1 EV



Distribution of harmonic  
moments of arrival direction  
distribution above 1 EV  
→ **strong isotropisation**  
by GMF

Flux at Earth

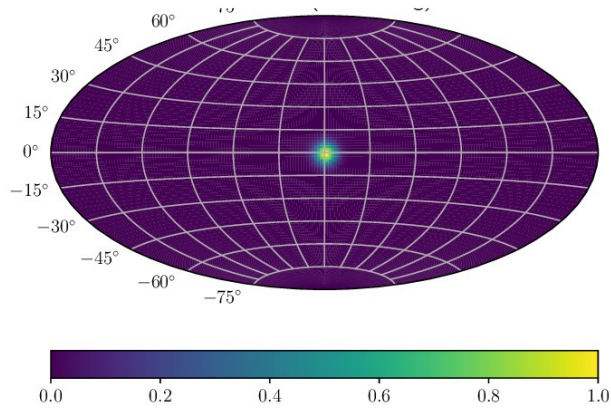


Rigidity spectrum at  
Earth → **possible flux**  
**modification**

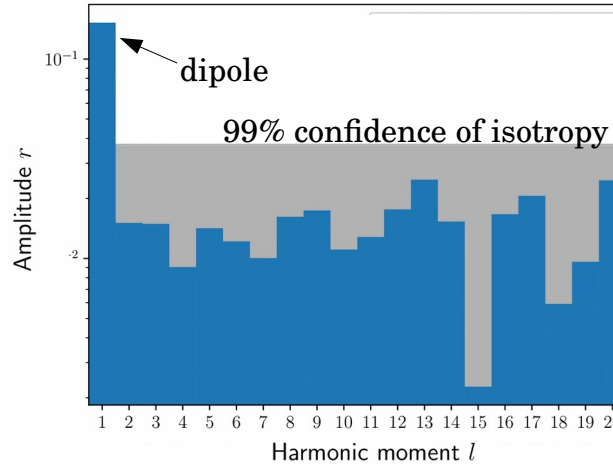


# Effect on observables: Anisotropic EGCRs – Galactic lensing

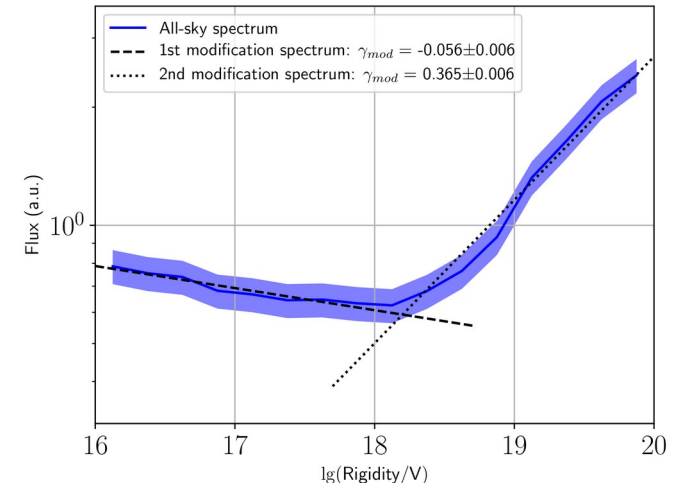
Injected flux



Distribution of moments above 1 EV



Flux at Earth



Injection direction distribution:  
**Pure single-point source** (minimum Galactic transparency; Galactic centre)

- surviving dipole in arrival direction distribution above 1 EV
- strong isotropisation by GMF at lower energies

Rigidity spectrum at Earth → **possible flux modification**

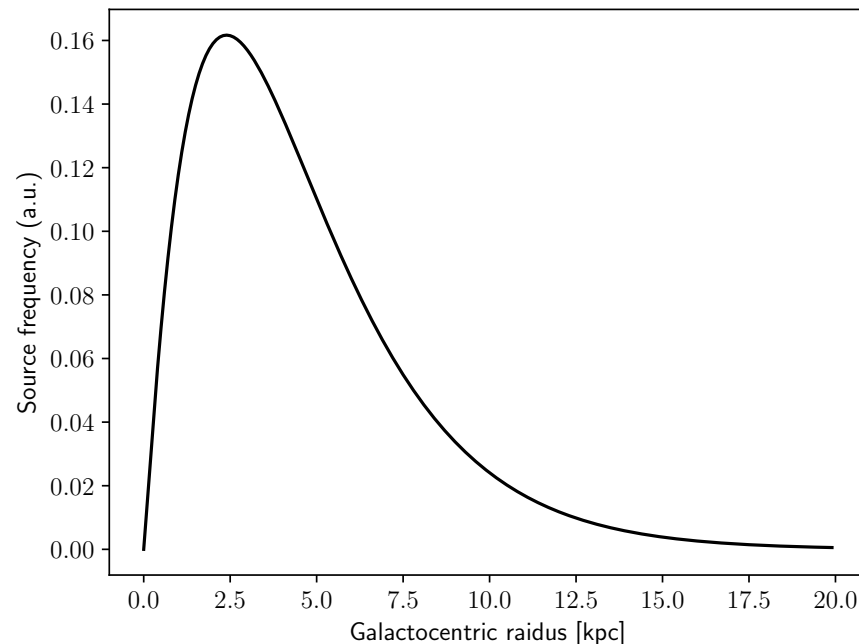


# Goal: Flux prediction

Adapt simulated rigidity spectra:

- GCRs:
  - employ **realistic source distribution**
  - include **maximum rigidity cut-off** of Galactic sources
- EGCRs:
  - apply Galactic lens to realistic injection direction distribution
    - **point sources from “Auger Starbust”**  
paper: APJ.Lett. 853 (2018) 2, L29
    - rigidity- and distance-dependent **smearing**

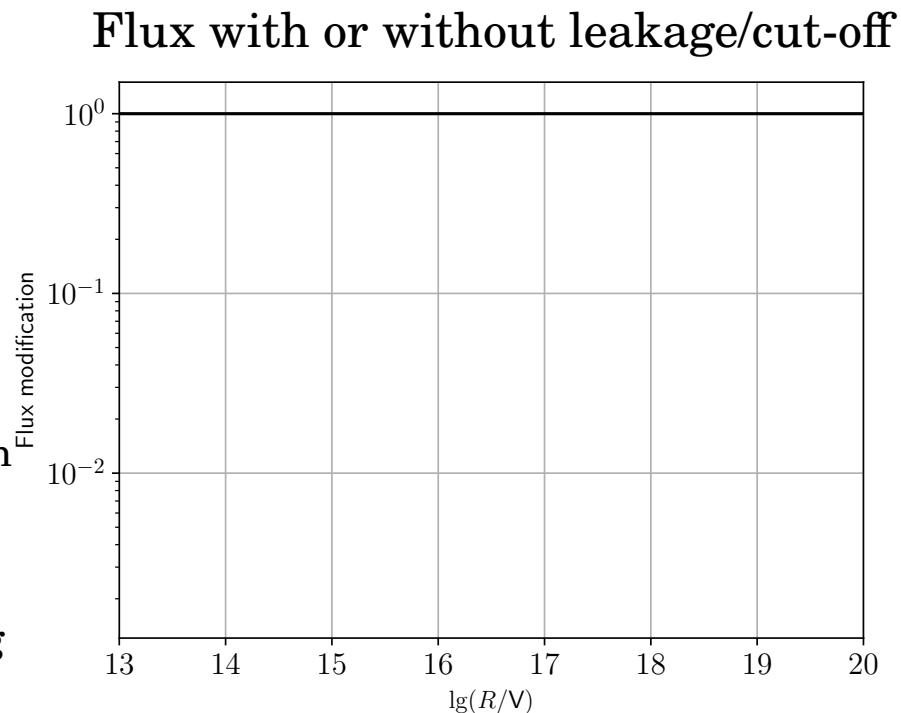
Galactocentric distribution of SNRs



# Goal: Incorporate propagation effects

Adapt simulated rigidity spectra:

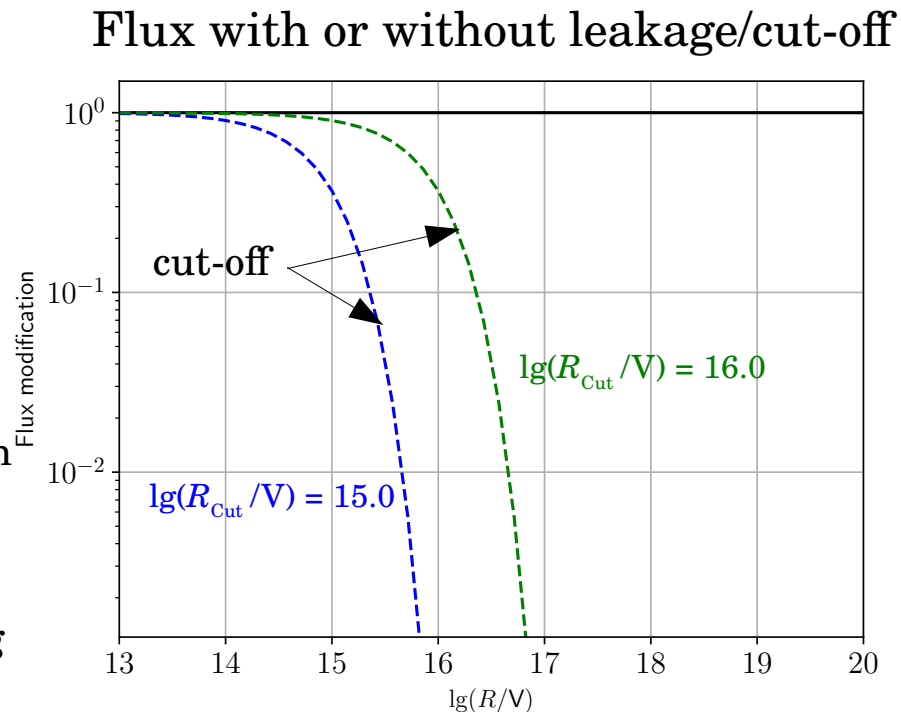
- GCRs:
  - employ **realistic source distribution**
  - include **maximum rigidity cut-off** of Galactic sources
- EGCRs:
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paper: APJ.Lett. 853 (2018) 2, L29
    - rigidity- and distance-dependent **smearing**



# Goal: Incorporate propagation effects

Adapt simulated rigidity spectra:

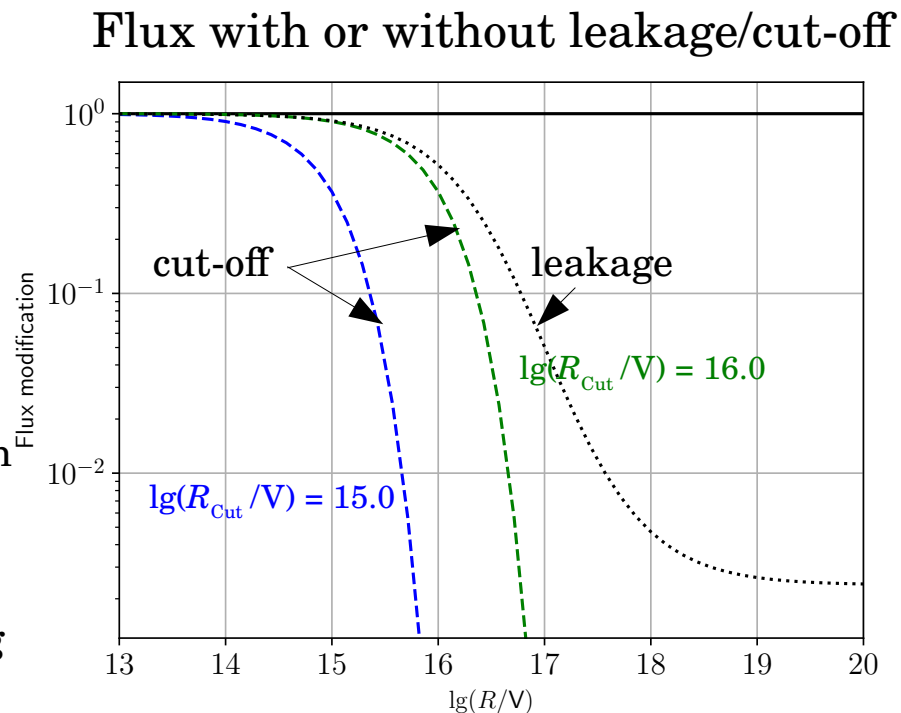
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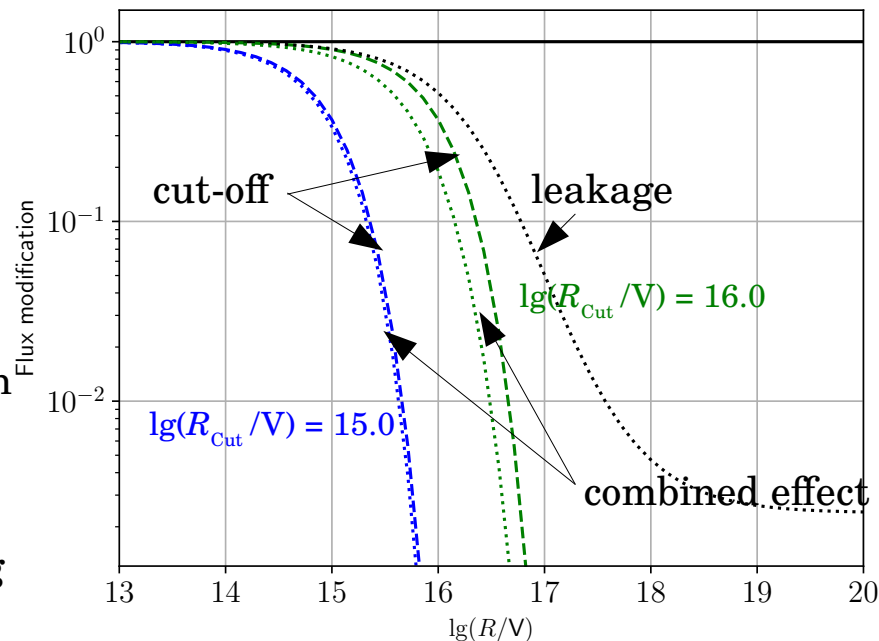


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Flux with or without leakage/cut-off

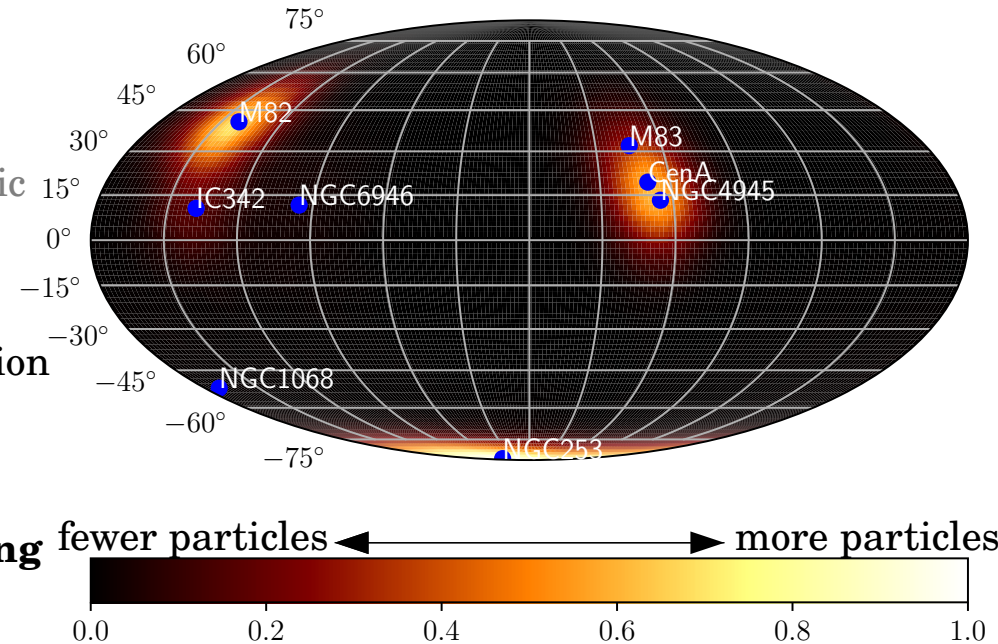


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## Injection direction distribution of EGCRs

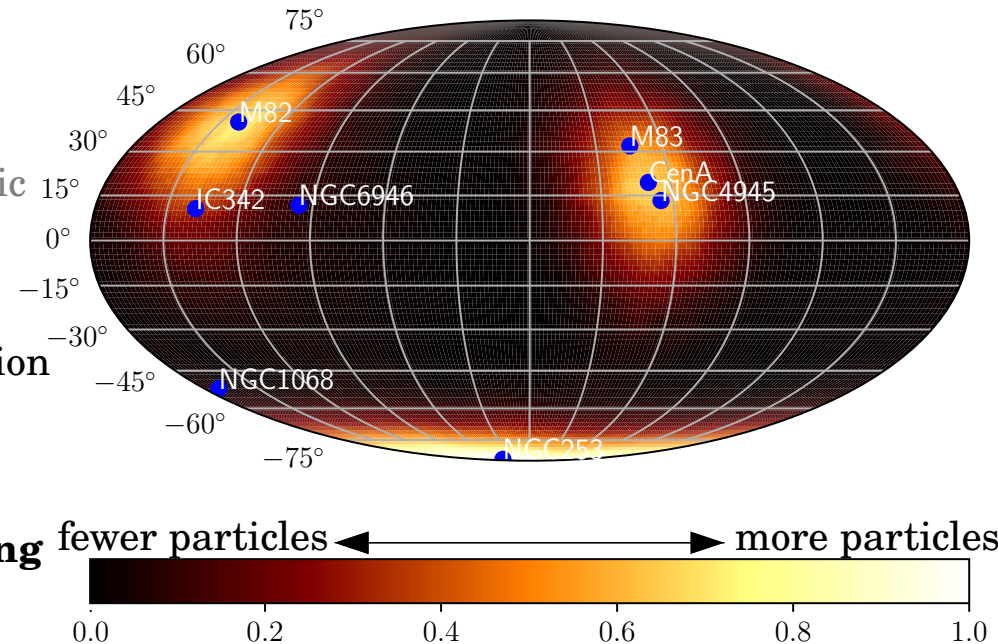


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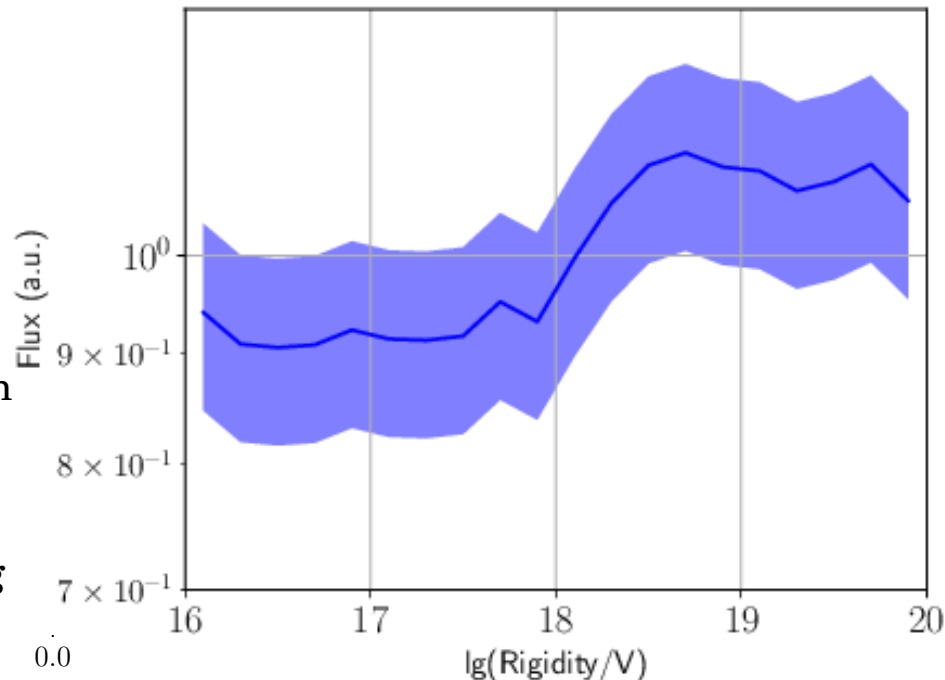


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Rigidity spectrum of lensed EGCRs flux

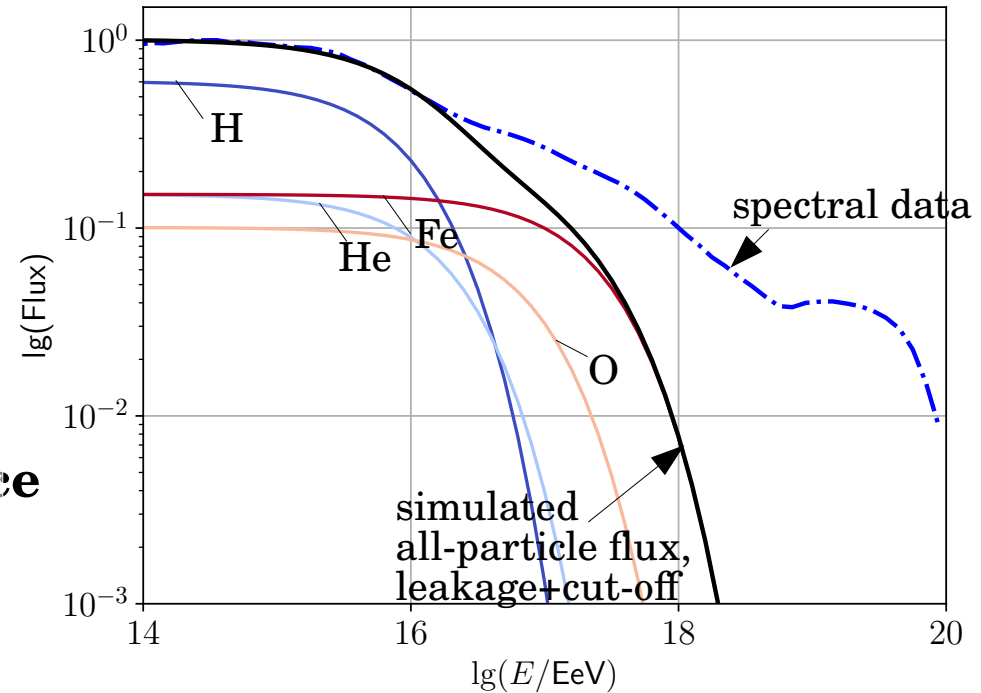


# Goal: Incorporate propagation effects

Create all-particle spectra:

- Scale rigidity spectra to **different nuclei**  
→ **energy spectra**
- Find **suitable injection spectra**:
  - 4-component composition: H, He, O, Fe
  - **GCR** component to energies around “**knee**”
  - **EGCR** component to **post-“ankle”** energies→ **all-particle spectra that reproduce data**

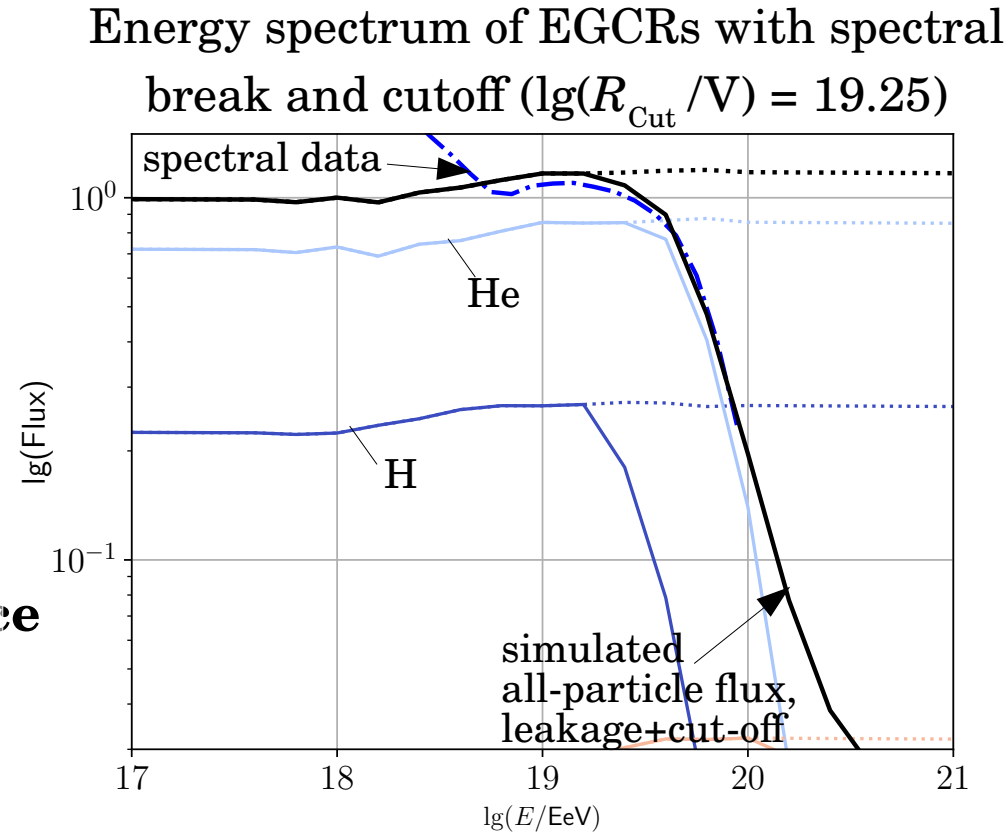
Energy spectrum of GCRs with leakage and cutoff ( $\lg(R_{\text{Cut}}/V) = 16.5$ )



# Goal: Incorporate propagation effects

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→ **energy spectra**
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# Summary

**Propagation effects in the GMF** need to be considered in the transition region!

- GCRs: **flux suppression** towards higher rigidities due to **leakage from Galaxy**
- EGCRs: **flux modifications** depending on **nature & direction of injected anisotropy**

**Incorporate propagation effects** into the total flux

- GCRs: **leakage** leads to **earlier onset of suppression**; degree dependent on  $R_{\text{Cut}}$
- EGCRs: **injected flux from SBG/AGN** leads to **spectral break**

**Total energy spectrum:** flux predictions **cannot account for flux** in transition region

# Outlook

- **comparison with composition & anisotropy data**

# Thank you for your attention!